



Maths

Teacher's Manual

Class VIII

Written by :
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Vidyalaya Prakashan

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Number System

Rational Numbers

Exercise 1A

1. (a) $\frac{3}{4} = \frac{3 \times 2}{4 \times 2} = \frac{6}{8}$; $\frac{3 \times 3}{4 \times 3} = \frac{9}{12}$; $\frac{3 \times 4}{4 \times 4} = \frac{12}{16}$
- (b) $\frac{-5}{7} = \frac{-5 \times 2}{7 \times 2} = \frac{-10}{14}$; $\frac{-5 \times 3}{7 \times 3} = \frac{-15}{21}$; $\frac{-5 \times 4}{7 \times 4} = \frac{-20}{28}$
- (c) $\frac{8}{-9} = \frac{8 \times 2}{-9 \times 2} = \frac{16}{-18}$ or $\frac{-16}{18}$ (standard form)
- $$\frac{-8 \times 3}{9 \times 3} = \frac{-24}{27}; \frac{-8 \times 4}{9 \times 4} = \frac{-32}{36}$$
- (d) $\frac{-11}{12} = \frac{-11 \times 2}{12 \times 2} = \frac{-22}{24}$; $\frac{-11 \times 3}{12 \times 3} = \frac{-33}{36}$; $\frac{-11 \times 4}{12 \times 4} = \frac{-44}{48}$

2. $\frac{21}{-8}$ as a rational number with denominator 24.

To make the denominator $24 = -8 \times -3 = 24$

$$\text{So, } \frac{21}{-8} \times \frac{-3}{-3} = \frac{-63}{24}$$

3. $\frac{-28}{84}$ as a rational number with numerator 4

To make the numerator $4 = -28 \div -7 = 4$

$$\text{So, } \frac{-28 \div (-7)}{84 \div (-7)} = \frac{4}{-12}$$

4. Add

(a) $\frac{3}{5} + \frac{1}{5} = \frac{3+1}{5} = \frac{4}{5}$

(b) $\frac{-8}{11} + \frac{(-4)}{11} = \frac{-8-4}{11} = \frac{-12}{11}$

$$(c) \frac{6}{13} + \frac{(-5)}{13} = \frac{6-5}{13} = \frac{1}{13}$$

5. Add

$$(a) -\frac{1}{6} + \frac{3}{10} \quad \text{LCM of 6 and 10} = 30$$

$$\text{So, } \frac{-1 \times 5}{6 \times 5} + \frac{3 \times 3}{10 \times 3} = \frac{-5}{30} + \frac{9}{30} = \frac{-5+9}{30} = \frac{4}{30}$$

$$(b) \frac{-5}{16} + \frac{-7}{24} \quad \text{LCM of 16 and 24} = 48$$

$$\frac{-5 \times 3}{16 \times 3} + \frac{-7 \times 2}{24 \times 2} = \frac{-15}{48} - \frac{14}{48} = \frac{-15-14}{48} = \frac{-29}{48}$$

$$(c) 3\frac{3}{4} + 4\frac{1}{3} = \frac{15}{4} + \frac{13}{3} \quad \text{LCM of 4 and 3} = 12$$

$$\frac{15 \times 3}{4 \times 3} + \frac{13 \times 4}{3 \times 4} = \frac{45}{12} + \frac{52}{12} = \frac{45+52}{12} = \frac{97}{12} = 8\frac{1}{12}$$

$$6. (a) \frac{13}{14} + \frac{9}{-7} \quad \text{LCM of 14 and 7 is} = 14$$

$$\frac{13}{14} - \frac{9}{7} = \frac{13 \times 1}{14 \times 1} - \frac{9 \times 2}{7 \times 2} = \frac{13}{14} - \frac{18}{14} = \frac{13-18}{14} = \frac{-5}{14}$$

$$(b) \frac{6}{15} + \frac{-7}{24} = \frac{6}{15} - \frac{7}{24} \quad \text{LCM of 15 and 24 is 120}$$

$$\frac{6 \times 8}{15 \times 8} - \frac{7 \times 5}{24 \times 5} = \frac{48}{120} - \frac{35}{120} = \frac{48-35}{120} = \frac{13}{120}$$

$$(c) \frac{-16}{9} + \frac{-5}{12} = \frac{-16}{9} - \frac{5}{12} \quad \text{LCM of 9 and 12 is 36}$$

$$\frac{-16 \times 4}{9 \times 4} - \frac{5 \times 3}{12 \times 3} = \frac{-64}{36} - \frac{15}{36} = \frac{-64-15}{36} = \frac{-79}{36}$$

$$(d) \frac{7}{9} + \frac{3}{-4} = \frac{7}{9} - \frac{3}{4} \quad \text{LCM of 9 and 4 is 36}$$

$$\frac{7 \times 4}{9 \times 4} - \frac{3 \times 9}{4 \times 9} = \frac{28}{36} - \frac{27}{36} = \frac{28-27}{36} = \frac{1}{36}$$

$$(e) 0 + \frac{-3}{5} = \frac{0-3}{5} = \frac{-3}{5}$$

7. Additive inverse of

$$(a) \frac{3}{5} = \frac{-3}{5}$$

$$(b) \frac{17}{9} = \frac{-17}{9}$$

$$(c) \frac{3}{-11} = \frac{3}{11}$$

$$(d) \frac{8}{-29} = \frac{8}{29}$$

$$(e) 0 = 0$$

$$(f) \frac{-11}{-21} = \frac{-11}{21}$$

8. Find the sum

$$(a) \frac{2}{3} + \frac{-3}{5} + \frac{1}{3} + \frac{-2}{5}$$

$$\left(\frac{2}{3} + \frac{1}{3}\right) + \left(\frac{-3}{5} - \frac{2}{5}\right) = \frac{3}{3} - \frac{5}{5} = 1 - 1 = 0$$

$$(b) \frac{3}{5} + \frac{5}{3} + \frac{-11}{5} + \frac{-2}{3}$$

$$\left(\frac{3}{5} - \frac{11}{5}\right) + \left(\frac{5}{3} - \frac{2}{3}\right) = \left(\frac{3-11}{5}\right) + \left(\frac{5-2}{3}\right)$$

$$= \frac{-8}{5} + \frac{3}{3} = \frac{-8}{5} + 1 = \frac{-8+5}{5} = \frac{-3}{5}$$

$$(c) \frac{4}{3} + \frac{3}{5} + \frac{-2}{3} + \frac{-11}{5}$$

$$\left(\frac{4}{3} - \frac{2}{3}\right) + \left(\frac{3}{5} - \frac{11}{5}\right) = \left(\frac{4-2}{3}\right) + \left(\frac{3-11}{5}\right)$$

$$= \frac{2}{3} - \frac{8}{5} = \frac{10-24}{15} = -\frac{14}{15}$$

$$(d) \frac{3}{5} + \frac{7}{3} + \frac{9}{5} + \frac{-13}{15} + \frac{-7}{3}$$

$$\left(\frac{3}{5} + \frac{9}{5}\right) + \left(\frac{7}{3} - \frac{7}{3}\right) - \frac{13}{15} = \left(\frac{3+9}{5}\right) + 0 - \frac{13}{15}$$

$$= \frac{12}{5} - \frac{13}{15} = \frac{36-13}{15} = \frac{23}{15} \text{ or } 1\frac{8}{15}$$

$$(e) \frac{5}{3} + \frac{11}{2} + \frac{-9}{4} + \frac{-8}{3} + \frac{-7}{2}$$

$$\left(\frac{5}{3} - \frac{8}{3}\right) + \left(\frac{11}{2} - \frac{7}{2}\right) - \frac{9}{4} = \left(\frac{5-8}{3}\right) + \left(\frac{11-7}{2}\right) - \frac{9}{4}$$

$$= \left(\frac{-3}{3}\right) + \left(\frac{4}{2}\right) - \frac{9}{4} = \frac{-1}{1} + \frac{2}{1} - \frac{9}{4}$$

$$= \frac{-4+8-9}{4} = -\frac{5}{4} \text{ or } -1\frac{1}{4}$$

$$(f) \frac{-3}{10} + \frac{7}{15} + \frac{3}{-20} + \frac{-9}{10} + \frac{13}{15} + \frac{-13}{20}$$

$$\left(\frac{-3}{10} - \frac{9}{10}\right) + \left(\frac{7}{15} + \frac{13}{15}\right) + \left(\frac{-3}{20} - \frac{13}{20}\right)$$

$$\left(\frac{-3-9}{10}\right) + \left(\frac{7+13}{15}\right) + \left(\frac{-3-13}{20}\right)$$

$$= \frac{-12}{10} + \frac{20}{15} - \frac{16}{20} = \frac{-72+80-48}{60} = \frac{-40}{60} = \frac{-2}{3}$$

Exercise 1B

1. Subtract

$$(a) \frac{7}{8} - \frac{2}{3} = \frac{7 \times 3 - 2 \times 8}{24} = \frac{21-16}{24} = \frac{5}{24}$$

$$(b) \frac{-3}{7} - \left(\frac{-5}{9}\right) = \frac{-3}{7} + \frac{5}{9} = \frac{(-3 \times 9) + (7 \times 5)}{63} = \frac{-27+35}{63} = \frac{8}{63}$$

$$(c) \frac{5}{6} - \frac{3}{4} = \frac{5 \times 2 - 3 \times 3}{12} = \frac{10-9}{12} = \frac{1}{12}$$

$$(d) \frac{-5}{7} - \left(\frac{-3}{8}\right) = \frac{-5}{7} + \frac{3}{8} = \frac{(-5 \times 8) + (3 \times 7)}{56}$$

$$= \frac{-40+21}{56} = \frac{-19}{56}$$

2. Evaluate

$$(a) \frac{3}{5} - \frac{1}{5} = \frac{3-1}{5} = \frac{2}{5}$$

$$(b) \frac{-1}{6} - \frac{4}{9} = \frac{(-1 \times 3) - (4 \times 2)}{18} = \frac{-3-8}{18} = \frac{-11}{18}$$

$$(c) \frac{3}{10} - \left(\frac{-4}{15}\right) = \frac{3}{10} + \frac{4}{15} = \frac{3 \times 3 + 4 \times 2}{30} = \frac{9+8}{30} = \frac{17}{30}$$

$$(d) \frac{4}{5} - \left(\frac{3}{-4}\right) = \frac{4}{5} + \frac{3}{4} = \frac{(4 \times 4) + (3 \times 5)}{20} = \frac{16+15}{20} = \frac{31}{20}$$

3. The sum of rational numbers = -3

$$\text{One number} = \frac{-11}{5}$$

$$\begin{aligned} \text{Second number} &= \frac{-3}{1} - \left(\frac{-11}{5}\right) = \frac{-3}{1} + \frac{11}{5} \\ &= \frac{-3 \times 5 + 11 \times 1}{5} = \frac{-15+11}{5} = \frac{-4}{5} \end{aligned}$$

4. The sum of numbers = $\frac{-3}{5}$

$$\text{One number} = \frac{-9}{20}$$

$$\begin{aligned} \text{Other number} &= \frac{-3}{5} - \left(\frac{-9}{20}\right) = \frac{-3}{5} + \frac{9}{20} \\ &= \frac{(-3 \times 4) + (9 \times 1)}{20} = \frac{-12+9}{20} = \frac{-3}{20} \end{aligned}$$

5. Number added should be

$$\frac{5}{9} - \left(\frac{-5}{8}\right) = \frac{5}{9} + \frac{5}{8} = \frac{(8 \times 5) + (5 \times 9)}{72} = \frac{40+45}{72} = \frac{85}{72}$$

6. Number added should be

$$\frac{5}{9} - \left(\frac{-4}{7}\right) = \frac{5}{9} + \frac{4}{7} = \frac{(5 \times 7) + (4 \times 9)}{63} = \frac{35+36}{63} = \frac{71}{63}$$

7. The number subtracted should be

$$\frac{-7}{11} - \left(\frac{-2}{1} \right) = \frac{-7}{11} + \frac{2}{1} = \frac{-7+22}{11} = \frac{15}{11}$$

8. The number subtracted should be

$$\frac{-3}{4} - \frac{5}{6} = \frac{(-3 \times 6) - (5 \times 4)}{24} = \frac{-18 - 20}{24} = \frac{-38}{24} = \frac{-19}{12}$$

9. Simplify:

$$(a) \frac{3}{7} + \frac{-6}{11} + \frac{8}{21} + \frac{-5}{22}$$

$$\begin{aligned} \left(\frac{3}{7} + \frac{8}{21} \right) - \left(\frac{6}{11} + \frac{5}{22} \right) &= \left(\frac{3 \times 3 + 8 \times 1}{21} \right) - \left(\frac{6 \times 2 + 5 \times 1}{22} \right) \\ &= \left(\frac{9+8}{21} \right) - \left(\frac{12+5}{22} \right) = \frac{17}{21} - \frac{17}{22} \\ &= \frac{17 \times 22 - 17 \times 21}{462} = -\frac{374 - 357}{462} = \frac{17}{462} \end{aligned}$$

$$(b) \frac{2}{5} + \frac{8}{3} - \frac{12}{15} + \frac{4}{5} - \frac{2}{3}$$

$$\begin{aligned} &= \left(\frac{2}{5} + \frac{4}{5} \right) + \left(\frac{8}{3} - \frac{2}{3} \right) - \frac{12}{15} = \frac{6}{5} + \frac{6}{3} - \frac{12}{15} \\ &= \frac{(6 \times 3) + (6 \times 5) - (12 \times 1)}{15} = \frac{18 + 30 - 12}{15} = \frac{48 - 12}{15} = \frac{36}{15} \end{aligned}$$

$$(c) \frac{-7}{4} + \frac{5}{3} + \frac{-5}{6} + \frac{1}{3} + \frac{-1}{2}$$

$$\begin{aligned} &= \frac{-7}{4} + \left(\frac{5}{3} + \frac{1}{3} \right) - \frac{5}{6} - \frac{1}{2} = \frac{-7}{4} + \frac{6}{3} - \frac{5}{6} - \frac{1}{2} \\ &= \frac{(-7 \times 3) + (6 \times 4) - (5 \times 2) - (1 \times 6)}{12} \\ &= \frac{-21 + 24 - 10 - 6}{12} = \frac{-37 + 24}{12} = \frac{-13}{12} \end{aligned}$$

$$\begin{aligned}
 \text{(d)} \quad \frac{6}{7} - \frac{2}{1} + \frac{-7}{9} + \frac{19}{21} &= \frac{6}{7} - \frac{2}{1} - \frac{7}{9} + \frac{19}{21} \\
 &= \frac{(6 \times 9) - (2 \times 63) - (7 \times 7) + (19 \times 3)}{63} \\
 &= \frac{54 - 126 - 49 + 57}{63} = \frac{-175 + 111}{63} = \frac{-64}{63}
 \end{aligned}$$

Exercise 1C

1. Multiply:

$$\text{(a)} \quad \frac{3}{4} \times \frac{5}{7} = \frac{15}{28}$$

$$\text{(b)} \quad \frac{3}{7} \times \frac{-4}{5} = \frac{-12}{35}$$

$$\text{(c)} \quad \frac{-5}{9} \times \frac{4}{1} = \frac{-20}{9}$$

$$\text{(d)} \quad \frac{-36}{7} \times \frac{-28}{9} = 16$$

2. Simplify:

$$\text{(a)} \quad \frac{-8}{7} \times \frac{14}{5} = \frac{-16}{5}$$

$$\text{(b)} \quad \frac{13}{6} \times \frac{-18}{91} = \frac{-3}{7}$$

$$\text{(c)} \quad \frac{-5}{9} \times \frac{72}{-125} = \frac{8}{25}$$

$$\text{(d)} \quad \frac{-22}{9} \times \frac{-51}{-88} = \frac{-51}{36}$$

$$\text{(e)} \quad \left(\frac{-16}{5} \times \frac{20}{8} \right) - \left(\frac{15}{5} \times \frac{-35}{3} \right) = -8 + 35 = 27$$

$$\text{(f)} \quad \left(\frac{-3}{2} \times \frac{4}{5} \right) + \left(\frac{9}{5} \times \frac{-10}{3} \right) - \left(\frac{1}{2} \times \frac{3}{4} \right)$$

$$= \frac{-6}{5} + (-6) - \left(\frac{3}{8} \right) = \frac{-6}{5} - \frac{6}{1} - \frac{3}{8}$$

$$= \frac{-6 \times 8 - 6 \times 40 - 3 \times 5}{40} = \frac{-48 - 240 - 15}{40} = \frac{-303}{40}$$

3. Reciprocal of:

$$\text{(a)} \quad 7 = \frac{1}{7}$$

$$\text{(b)} \quad -11 = -\frac{1}{11}$$

$$\text{(c)} \quad \frac{2}{5} = \frac{5}{2}$$

$$\text{(d)} \quad \frac{-7}{15} = \frac{-15}{7}$$

$$(e) \frac{5}{12} = \frac{-12}{5}$$

4. Reciprocal or multiplicative inverse of:

$$(a) \frac{2}{5} \times \frac{4}{9} = \frac{8}{45} = \frac{45}{8}$$

$$(b) \frac{-3}{8} \times \frac{-7}{13} = \frac{21}{104} = \frac{104}{21}$$

$$(c) \frac{-5}{8} \times \frac{16}{15} = \frac{-2}{3} = \frac{-3}{2}$$

$$(d) \frac{-2}{1} \times \frac{-3}{5} = \frac{6}{5} = \frac{5}{6}$$

$$5. x = \frac{-3}{5}, y = \frac{7}{8}, z = \frac{-4}{9}$$

To verify

$$(a) x \times y = y \times x$$

$$\text{LHS } \frac{-3}{5} \times \frac{7}{8} = \frac{-21}{40}$$

$$\text{RHS } \frac{7}{8} \times \frac{-3}{5} = \frac{-21}{40}$$

$$(b) x \times (y \times z) = (x \times y) \times z$$

$$\text{LHS } \frac{-3}{5} \times \left(\frac{7}{8} \times \frac{-4}{9} \right) = \frac{-3}{5} \times \frac{-7}{18} = \frac{7}{30}$$

$$\text{RHS } (x \times y) \times z = \left(\frac{-3}{5} \times \frac{7}{8} \right) \times \frac{-4}{9} = \frac{-21}{40} \times \frac{-4}{9} = \frac{7}{30}$$

$$(c) x \times (y + z) = (x \times y) + (x \times z)$$

$$\text{LHS } \frac{-3}{5} \times \left(\frac{7}{8} + \frac{4}{9} \right) = \frac{-3}{5} \times \left(\frac{7 \times 9 + 4 \times 8}{72} \right)$$

$$= \frac{-3}{5} \times \left(\frac{63 + 32}{72} \right) = \frac{-3 \times 95}{5 \times 72} = \frac{-95}{360}$$

RHS $x \times y + x \times z$

$$\begin{aligned} \left(\frac{-3}{5} \times \frac{7}{8}\right) + \left(\frac{-3}{5} \times \frac{-4}{9}\right) &= \frac{-21}{40} + \frac{12}{45} \\ &= \frac{-21 \times 9 + 12 \times 8}{360} = \frac{-189 + 96}{360} = \frac{-93}{360} \end{aligned}$$

(d) $(x \times y)^{-1} = x^{-1} \times y^{-1}$

$$\text{LHS} \quad \left(\frac{-3}{5} \times \frac{7}{8}\right)^{-1} = \left(\frac{-21}{40}\right)^{-1} = \frac{40}{-21}$$

RHS $x^{-1} = y^{-1}$

$$\left(\frac{-3}{5}\right)^{-1} \times \left(\frac{7}{8}\right)^{-1} = \frac{5}{-3} \times \frac{8}{7} = \frac{40}{-21}$$

$$6. \quad \text{(a)} \quad \frac{7}{4} \times \left(\frac{5}{8} + \frac{1}{3}\right) = \left(\frac{7}{4} \times \frac{5}{8}\right) + \left(\frac{7}{4} \times \frac{1}{3}\right) = \frac{35}{32} + \frac{7}{12}$$

$$= \frac{35 \times 3 + 7 \times 8}{96} = \frac{105 + 56}{96} = \frac{161}{96}$$

$$\text{(b)} \quad \frac{-3}{8} \times \left(\frac{7}{16} - \frac{21}{4}\right) = \left(\frac{3}{8} \times \frac{7}{16}\right) - \left(\frac{-3}{8} \times \frac{21}{4}\right) = \frac{-21}{128} + \frac{63}{32}$$

$$= \frac{-21 \times 1 + 63 \times 4}{128} = \frac{-21 + 252}{128} = \frac{231}{128}$$

$$\text{(c)} \quad \frac{3}{4} \times \left(\frac{8}{9} - \frac{30}{1}\right) = \left(\frac{3}{4} \times \frac{8}{9}\right) - \left(\frac{3}{4} \times \frac{30}{1}\right) = \frac{2}{3} - \frac{45}{2}$$

$$= \frac{2 \times 2 - 45 \times 3}{6} = \frac{4 - 135}{6} = \frac{-131}{6}$$

7. Multiplicative inverse (reciprocal) of 6 :

$$\text{(a)} \quad 5 = \frac{1}{5}$$

$$\text{(b)} \quad -21 = \frac{1}{-21}$$

$$\text{(c)} \quad \frac{15}{32} = \frac{32}{15}$$

$$\text{(d)} \quad \frac{-17}{13} = \frac{13}{-17}$$

$$(e) \frac{11}{-5} = \frac{-5}{11}$$

$$(f) \frac{-7}{-8} = \frac{7}{8} = \frac{8}{7}$$

$$(g) -1 \times \frac{-5}{12} = \frac{5}{12} = \frac{12}{5}$$

$$(h) \frac{4}{5} \times \frac{15}{8} = \frac{3}{2} = \frac{2}{3}$$

$$(i) 0 \times \frac{2}{3} = 0 = \infty$$

8. (a) Existence of multiplicative inverse
(b) Multiplication by 0
(c) Existence of multiplicative identity
(d) Existence of multiplicative inverse
(e) Commutativity
(f) Distributivity of multiplication over addition
(g) Distributivity of multiplication over addition

Exercise 1D

1. Divide

$$(a) \frac{5}{9} \div \frac{25}{1} = \frac{5}{9} \times \frac{1}{25} = \frac{1}{45}$$

$$(b) \frac{7}{18} \div \frac{-28}{51} = \frac{7}{18} \times \frac{51}{-28} = \frac{-17}{24}$$

$$(c) \frac{20}{33} \div \frac{4}{-11} = \frac{20}{33} \times \frac{-11}{4} = \frac{-5}{3}$$

$$(d) \frac{-8}{9} \div \frac{4}{3} = \frac{-8}{9} \times \frac{3}{4} = \frac{-2}{3}$$

$$(e) \frac{-8}{13} \div \frac{3}{-26} = \frac{-8}{13} \times \frac{-26}{3} = \frac{16}{3}$$

$$(f) \frac{-24}{50} \div \frac{-4}{75} = \frac{24}{50} \times \frac{75}{4} = 9$$

2. Evaluate

$$(a) \left(\frac{5}{18} \div \frac{45}{72} \right) \div \left(\frac{-15}{18} \right) = \left(\frac{5}{18} \times \frac{72}{45} \right) \div \left(\frac{-15}{18} \right)$$

$$\frac{4}{9} \div \left(\frac{-15}{18} \right) = \frac{4}{9} \times \frac{18}{-15} = \frac{8}{-15}$$

$$(b) \left(\frac{-5}{23} \div \frac{15}{69} \right) \div \frac{-1}{5} = \left(\frac{-5}{23} \times \frac{69}{15} \right) \div \frac{-1}{5} = 1 \times \frac{5}{1} = 5$$

3. Product of rational numbers = -12

One number = 8

$$\text{Other number} = -12 \div -8 = \frac{12}{8} = \frac{3}{2} \text{ or } 1\frac{1}{2}$$

$$4. \frac{1}{17} \div \frac{-7}{85} = \frac{1}{17} \times \frac{85}{-7} = \frac{5}{-7} \text{ or } \frac{-5}{7}$$

$$5. 24 \div \frac{-8}{13} = 24 \times \frac{13}{-8} = -39$$

6. Sum of $\frac{3}{8}$ and $\frac{-5}{12}$

$$\frac{3}{8} - \frac{5}{12} = \frac{3 \times 3 - 5 \times 2}{24} = \frac{9 - 10}{24} = \frac{-1}{24}$$

$$\text{Reciprocal of } \frac{-15}{8} \times \frac{16}{27} = \frac{-10}{9} = \frac{-9}{10}$$

$$\frac{-1}{24} \div \frac{-9}{10} = \frac{1}{24} \times \frac{10}{9} = \frac{5}{108}$$

7. Cost of $\frac{63}{5}$ kg mango is = ₹ $\frac{1323}{4}$

$$\text{Cost of 1 kg mango is} = \frac{1323}{4} \times \frac{5}{63} = \frac{105}{4} = ₹ 26\frac{1}{4}$$

8. In 1 hour the train covers = $80\frac{4}{5}$ km or $\frac{404}{5}$ km

$$\text{In } 4\frac{3}{4} = \frac{19}{4} \text{ hour the train covers} = \frac{404}{5} \times \frac{19}{4} = \frac{1919}{5} = 383\frac{4}{5} \text{ km}$$

9. Area of rectangle = $45\frac{5}{16} = \frac{725}{16} \text{ cm}^2$

$$\text{Length} = \frac{25}{4} \text{ cm}$$

$$\text{Breadth} = \left(\frac{725}{16} \div \frac{25}{4} \right) = \frac{725}{16} \times \frac{4}{25} = \frac{29}{4} = 7\frac{1}{4} \text{ cm}$$

Exercise 1E

1. Rational number between -2 and 6 is $= \frac{-2+6}{2} = \frac{4}{2} = 2$

2. Two rational numbers between -2 and 2 =

$$\frac{-2+2}{2} = 0 \text{ and } \frac{0-2}{2} = -1$$

So, numbers are $-1, 0$.

3. Rational number between $\frac{1}{3}$ and $\frac{1}{4}$

$$= \frac{1}{3} + \frac{1}{4} = \frac{4+3}{12} = \frac{7}{12} \times \frac{1}{2} = \frac{7}{24}$$

4. Three rational numbers between -2 and 5

$$\frac{2+5}{2} = \frac{3}{2}$$

$$\frac{-2}{1} + \frac{3}{2} = \frac{-4+3}{2} = \frac{-1}{2} \times \frac{1}{2} = \frac{-1}{4}$$

$$\frac{5}{1} + \frac{3}{2} = \frac{10+3}{2} = \frac{13}{2} \times \frac{1}{2} = \frac{13}{4}$$

So, numbers are $\frac{3}{2}, \frac{-1}{4}, \frac{13}{4}$

5. Four rational numbers between $\frac{1}{6}$ and $\frac{1}{3}$

$$\frac{1}{6} + \frac{1}{3} = \frac{1+2}{6} = \frac{3}{6} \times \frac{1}{2} = \frac{3}{12}$$

$$\frac{1}{6} + \frac{3}{12} = \frac{2+3}{12} = \frac{5}{12} \times \frac{1}{2} = \frac{5}{24}$$

$$\frac{3}{12} + \frac{1}{3} = \frac{3+4}{12} = \frac{7}{12} \times \frac{1}{2} = \frac{7}{24}$$

$$\frac{1}{6} + \frac{5}{24} = \frac{4+5}{24} = \frac{9}{24} \times \frac{1}{2} = \frac{9}{48}$$

So, numbers are; $\frac{3}{12}, \frac{5}{24}, \frac{7}{24}$ and $\frac{9}{48}$

7. Ten rational numbers between $\frac{1}{4}$ and $\frac{1}{2}$

By adopting the same procedure in sums 6 we can get the numbers as

$$\frac{3}{8}, \frac{5}{16}, \frac{7}{16}, \frac{9}{32}, \frac{13}{32}, \frac{15}{32}, \frac{17}{64}, \frac{19}{64}, \frac{25}{64}, \frac{27}{64}$$

8. Ten rational numbers between $\frac{2}{5}$ and $\frac{1}{2}$

we have $\frac{1}{20}, \frac{-7}{40}, \frac{-23}{80}, \frac{-5}{80}, \frac{11}{40}, \frac{13}{80}, \frac{31}{80}, \frac{53}{160}, \frac{71}{180}, \frac{115}{320}$

Check Your Mental Math IQ

A. Fill in the blanks :

- | | | | |
|--------------------------------|---------------------------------|---------------------|----------------------|
| 1. $\frac{-4}{15}$ | 2. $\frac{-3}{4}$ | 3. $\frac{-5}{12}$ | 4. Negative |
| 5. Negative | 6. 1 | 7. No | 8. -1 |
| 9. a | 10. $\frac{-8}{17}$ | 11. $\frac{-5}{13}$ | 12. $\frac{1}{3}$ |
| 13. $\frac{3}{4}, \frac{1}{2}$ | 14. $\frac{5}{7}, \frac{-3}{4}$ | 15. 1 | 16. $\frac{-6}{13}$ |
| 17. $\frac{-11}{15}$ | 18. 1 | 19. $\frac{-7}{13}$ | 20. $\frac{-11}{23}$ |

- B. 1. Zero 2. 1, -1 3. 0

- C. 1. True 2. True 3. True 4. False 5. True

Multiple Choice Questions

- | | | | |
|--------|---------|---------|--------|
| 1. (d) | 2. (a) | 3. (c) | 4. (b) |
| 5. (a) | 6. (c) | 7. (b) | 8. (a) |
| 9. (b) | 10. (b) | 11. (d) | |

Exercise 2A

1.	Number	Base	Exponent
(a)	5^7	5	7
(b)	3^{-8}	3	-8
(c)	$(-5)^9$	-5	9
(d)	$(\sqrt{2})^3$	$\sqrt{2}$	3
(e)	15	15	1
(f)	$\left(\frac{-4}{5}\right)^3$	$\frac{-4}{5}$	3
(g)	$\left(\frac{-3}{2}\right)^6$	$\frac{-3}{2}$	6
(h)	$(\sqrt{2})^0$	$\sqrt{2}$	0

2. In exponential form :

(a) $8 \times 8 \times 8 \times 8 \times 8 = 8^5$

(b) $(-9) \times (-9) \times (-9) = (-9)^3$

(c) $ab \times ab \times ab \times ab \times ab = (ab)^5$

(d) $3^2 \times 3^2 \times 3^2 \times 3^2 = (3^2)^4 = 3^8$

(e) $\sqrt{3} \times \sqrt{3} \times \sqrt{3} \times \sqrt{3} = (\sqrt{3})^4$

(f) $\frac{1}{5} \times \frac{1}{5} \times \frac{1}{5} = \left(\frac{1}{5}\right)^3$

(g) $\frac{1}{8 \times 8 \times 8} = \left(\frac{1}{8}\right)^3$

(h) $\left(\frac{2}{5}\right)^{-2} \times \left(\frac{2}{5}\right)^{-2} \times \left(\frac{2}{5}\right)^{-2} = \left(\frac{2}{5}\right)^{-6}$

3. In exponential form (Simplify)

(a) $9^{-3} \times 9^{-2} = 9^{-3-2} = 9^{-5}$ (b) $\frac{(3)^9}{(3)^5} = (3)^{9-5} = 3^4$

(c) $\{(-3)^5 \times 7^5\} = (-3 \times 7)^5 = (-21)^5$

(d) $\frac{x^{-3}}{x^{-5}} = (x)^{-3+5} = (x)^2$

(e) $\left(\frac{-3}{8}\right)^2 \times \left(\frac{-3}{8}\right)^5 \times \left(\frac{-3}{8}\right)^6 = \left(\frac{3}{8}\right)^{2+5+6} = \left(\frac{-3}{8}\right)^{13}$

(f) $(\sqrt{5})^3 \times (\sqrt{5})^{-1} \times (\sqrt{5})^2 = (\sqrt{5})^{3-1+2} = (\sqrt{5})^4$

(g) $(2^4)^{-3} = 2^{-12}$

4. Which is greater?

(a) 3^2 or 2^3

$$3^2 = 3 \times 3 = 9$$

$$2^3 = 2 \times 2 \times 2 = 8$$

So, $3^2 > 2^3$

(b) 3^4 or 4^3

$$3^4 = 3 \times 3 \times 3 \times 3 = 81$$

$$4^3 = 4 \times 4 \times 4 = 64$$

So, $3^4 > 4^3$

(c) 5^3 or 3^7

$$5^3 = 5 \times 5 \times 5 = 125$$

$$3^7 = 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 = 2187$$

So, $3^7 > 5^3$

5. (a) Expressing 625 as a power of 5

$$625 = 5 \times 5 \times 5 \times 5 = 5^4$$

(b) 343 as a power of 7

$$343 = 7 \times 7 \times 7 = 7^3$$

(c) 1024 as a power of -2

$$1024 = -2 \times -2 \times -2 \times -2 \times -2 \times -2 \times -2 \times -2 \times -2 \times -2$$

$$=(-2)^{10}$$

6. Reciprocal of

(a) $\frac{27}{64} = \frac{64}{27}$ or $\frac{4}{3} \times \frac{4}{3} \times \frac{4}{3} = \left(\frac{4}{3}\right)^3$

(b) $\frac{-16}{125} = \frac{125}{-16}$

(c) $\left(\frac{-3}{8}\right)^3 = \left(\frac{-8}{3}\right)^3$ or $\left(\frac{-3}{8}\right)^{-3}$

(d) $\left(\frac{-7}{3}\right)^2 = \left(\frac{3}{-7}\right)^2$ or $\left(\frac{-7}{3}\right)^{-2}$

7. (a) True (b) True (c) True (d) False
(e) False (f) True

8. Simplify :

(a) $\left(\frac{5}{7}\right)^3 \times \left(\frac{5}{7}\right)^{-5} = \left(\frac{5}{7}\right)^{3-5} = \left(\frac{5}{7}\right)^{-2} = \left(\frac{7}{5}\right)^2$

(b) $\left(\frac{-7}{9}\right)^8 \times \left(\frac{-7}{9}\right)^{-11} \times \left(\frac{-7}{9}\right)^1 = \left(\frac{-7}{9}\right)^{8-11+1} = \left(\frac{-7}{9}\right)^{-2} = \left(\frac{-9}{7}\right)^2$

(c) $\left(\frac{3}{11}\right)^4 \div \left(\frac{3}{11}\right)^{-3} = \left(\frac{3}{11}\right)^{4+3} = \left(\frac{3}{11}\right)^7$

(d) $\left(\frac{-5}{9}\right)^{-6} \div \left(\frac{-5}{9}\right)^5 = \left(\frac{-5}{9}\right)^{-6-5} = \left(\frac{-5}{9}\right)^{-11}$ or $\left(\frac{-9}{5}\right)^{11}$

(e) $\left(\frac{-4}{7}\right)^{-4} \div \left(\frac{-4}{7}\right)^{-10} = \left(\frac{-4}{7}\right)^{-4+10} = \left(\frac{-4}{7}\right)^6$

9. Simplify :

(a) $\left[\left(\frac{2}{5}\right)^{-3}\right]^4 = \left(\frac{2}{5}\right)^{-12} = \left(\frac{5}{2}\right)^{12}$

(b) $\left[\left(\frac{-6}{11}\right)^{-5}\right]^{-3} = \left(\frac{-6}{11}\right)^{15}$

$$(c) \left(\frac{5}{7}\right)^{-1} \times \left(\frac{7}{3}\right)^{-1} = \frac{7}{5} \times \frac{3}{7} = \frac{3}{5}$$

$$(d) [4^{-1} \div 3^{-1}]^{-2} = \left[\frac{1}{4} \div \frac{1}{3}\right]^{-2} = \left[\frac{1}{4} \times \frac{3}{1}\right]^{-2} \\ \left[\frac{3}{4}\right]^{-2} \text{ or } \left[\frac{4}{3}\right]^2 \text{ or } \frac{16}{9}$$

$$(e) (5^{-1} \times 3^{-1}) \div 6^{-1} = \left(\frac{1}{5} \times \frac{1}{3}\right) \div \frac{1}{6} = \frac{1}{15} \times \frac{6}{1} = \frac{2}{5}$$

$$(f) \frac{4^{-3} \times a^{-5} \times b^{-4}}{4^{-5} \times a^{-8} \times b^3} = 4^{-3+5} \times a^{-5+8} \times b^{-4-3} = 4^2 \times a^3 \times b^{-7} = \frac{16a^3}{b^7}$$

$$(g) (a^3 \times a^{-2} \times a^4)^{-2} = (a^3 \times \frac{1}{a^2} \times a^4)^{-2} \\ = (a^{3+4-2})^{-2} = (a^5)^{-2} = a^{-10} = \frac{1}{a^{10}}$$

10. Solve:

$$(a) 7^x = 343$$

$$7^x = 7 \times 7 \times 7 = 7^3$$

$$\text{So, } x = 3$$

$$(b) 3^{3x} = \frac{1}{27} = \frac{1}{3 \times 3 \times 3} = \left(\frac{1}{3}\right)^3 \text{ or } 3^{-3}$$

$$3x = -3$$

$$x = \frac{-3}{3} = -1$$

$$(c) (\sqrt{2})^x = 2^8 = (2^{1/2})^x = 2^8 = (2)^{x/2} = 2^8$$

$$\frac{x}{2} = 8 = x = 8 \times 2 = 16$$

$$(d) 3^{2x+1} \div 9 = 27$$

$$3^{2x+1} \div 3^2 = 27$$

$$3^{2x+1-2} = 3^3$$

$$3^{2x-1} = 3^3$$

$$2x - 1 = 3$$

$$2x = 3 + 1 = 4$$

$$x = \frac{4}{2} = 2$$

$$(e) 5^{2x} \div 5^{-3} = 5^5$$

$$5^{2x+3} = 5^5$$

$$2x + 3 = 5$$

$$2x = 5 - 3 = 2$$

$$x = \frac{2}{2} = 1$$

$$11. \left(\frac{5}{7}\right)^{-3} \times \left(\frac{5}{7}\right)^{-11} = \left(\frac{5}{7}\right)^{7x}$$

$$\left(\frac{5}{7}\right)^{-3-11} = \left(\frac{5}{7}\right)^{7x}$$

$$\left(\frac{5}{7}\right)^{-14} = \left(\frac{5}{7}\right)^{7x}$$

$$12. \left(\frac{2}{9}\right)^3 \times \left(\frac{2}{9}\right)^{-6} = \left(\frac{2}{9}\right)^{2m-1}$$
$$-14 = 7x = x = \frac{-14}{7} = -2$$

$$\left(\frac{2}{9}\right)^{3-6} = \left(\frac{2}{9}\right)^{2m-1}$$

$$\left(\frac{2}{9}\right)^{-3} = \left(\frac{2}{9}\right)^{2m-1}$$

$$2m - 1 = -3 \Rightarrow 2m = -3 + 1 \Rightarrow -2 = m = \frac{-2}{2} = -1$$

$$\begin{aligned}
 13. \quad x &= \left(\frac{3}{2}\right)^2 \times \left(\frac{2}{3}\right)^{-4} \\
 x &= \left(\frac{3}{2}\right)^2 \times \left(\frac{3}{2}\right)^4 \\
 x &= \left(\frac{3}{2}\right)^{2+4} \\
 x &= \left(\frac{3}{2}\right)^6 \\
 x^{-2} &= \left[\left(\frac{3}{2}\right)^6\right]^{-2} \\
 x^{-2} &= \left(\frac{3}{2}\right)^{-12} \quad \text{or} \quad \left(\frac{2}{3}\right)^{12}
 \end{aligned}$$

$$\begin{aligned}
 14. \quad \left(\frac{5}{4}\right)^{-2} \div \left(\frac{1}{2}\right)^{-3} &= \left(\frac{4}{5}\right)^2 \div (2)^3 = \left(\frac{4}{5} \times \frac{4}{5}\right) \div (8) \\
 \frac{16}{25} \times \frac{1}{8} &= \frac{2}{25}
 \end{aligned}$$

Check Your Mental Maths

$$1. \quad 5^x \div 5^{-3} = 5^5$$

$$5^{x+3} = 5^5$$

$$x + 3 = 5$$

$$x = 5 - 3 = 2$$

$$2. \quad \left(\frac{-3}{4}\right)^{-2} = \left(\frac{4}{-3}\right)^2 = \frac{4}{-3} \times \frac{4}{-3} = \frac{16}{9}$$

$$3. \quad \frac{16}{81} = \frac{2 \times 2 \times 2 \times 2}{3 \times 3 \times 3 \times 3} = \left(\frac{2}{3}\right)^4$$

$$4. \quad \left(\frac{x}{y}\right)^0 = 1$$

$$5. \quad (-5)^{-1} = \frac{-1}{5}$$

$$6. \quad \left(\frac{5}{6}\right)^7 \times \left(\frac{5}{6}\right)^{-9} = \left(\frac{5}{6}\right)^{2m}$$

$$\left(\frac{5}{6}\right)^{7-9} = \left(\frac{5}{6}\right)^{2m}$$

$$\left(\frac{5}{6}\right)^{-2} = \left(\frac{5}{6}\right)^{2m}$$

$$2m = -2$$

$$m = \frac{-2}{2} = -1$$

7. $(-3)^7 \div (-3)^2 = (-3)^{7-2} = (-3)^5$

8. $\left[\left(\frac{-3}{7}\right)^{-3}\right]^2 = \left(\frac{-3}{7}\right)^{-3 \times 2} = \left(\frac{-3}{7}\right)^{-6}$ or $\left(\frac{-7}{3}\right)^6$

Multiple Choice Questions

1. $11^x = \frac{1}{121} = \left(\frac{1}{11}\right)^2$

$$11^x = (11)^{-2}$$

$$x = -2 \quad (\text{b})$$

2. $(1^3 + 2^3 + 3^3 + 4^3) = ?$

$$(1 + 8 + 27 + 64) = 100 \quad (\text{d})$$

3. $27^{4/3} \div 27^{1/3} = ?$

$$27^{4/3 - 1/3} = 27^{4-1/3} = 27^{3/3} = 27^1 = 27 \quad (\text{c})$$

4. $(x^3)^{-3} = x^{-9} \quad (\text{a})$

5. $\left(\frac{-3}{7}\right)^3 = \frac{-3}{7} \times \frac{-3}{7} \times \frac{-3}{7} = \frac{-27}{343} \quad (\text{c})$

6. $\left[\left(\frac{3}{5}\right)^0\right]^3 = \left(\frac{3}{5}\right)^0 = 1 \quad (\text{c})$

7. $\left(\frac{1}{3}\right)^0 + \left(\frac{1}{5}\right)^0 + \left(\frac{1}{7}\right)^0 = 1 + 1 + 1 = 3 \quad (\text{a})$

$$8. \left(\frac{a}{b}\right)^0 \times \left(\frac{b}{c}\right)^0 \times \left(\frac{c}{a}\right)^0 = 1 \times 1 \times 1 = 1 \quad (\text{b})$$

$$9. 3^{-1} \div 4^{-1} = \frac{1}{3} \div \frac{1}{4} = \frac{1}{3} \times \frac{4}{1} = \frac{4}{3} \quad (\text{a})$$

10. (c)

3

Square and Square Roots

Exercise 3A

1. Number which are perfect squares :

$$\begin{array}{r|l}
 \text{(a)} & 2 \quad 256 \\
 \hline
 & 2 \quad 128 \\
 \hline
 & 2 \quad 64 \\
 \hline
 & 2 \quad 32 \\
 \hline
 & 2 \quad 16 \\
 \hline
 & 2 \quad 8 \\
 \hline
 & 2 \quad 4 \\
 \hline
 & 2
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 2 \times 2 \times 2 \times 2 \\
 & = 2 \times 2 \times 2 \times 2 = 16 \\
 & \text{So, 256 is a perfect square.}
 \end{aligned}$$

$$\begin{array}{r|l}
 \text{(b)} & 5 \quad 625 \\
 \hline
 & 5 \quad 125 \\
 \hline
 & 5 \quad 25 \\
 \hline
 & 5
 \end{array}$$

$$\begin{aligned}
 & 5 \times 5 \times 5 \times 5 \\
 & = 5 \times 5 = 25 \\
 & \text{So, 625 is a perfect square.}
 \end{aligned}$$

$$\begin{array}{r|l}
 (c) & 2 \quad 576 \\
 \hline
 & 2 \quad 288 \\
 \hline
 & 2 \quad 144 \\
 \hline
 & 2 \quad 72 \\
 \hline
 & 2 \quad 36 \\
 \hline
 & 2 \quad 18 \\
 \hline
 & 3 \quad 9 \\
 \hline
 & 3
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \\
 = & 2 \times 2 \times 2 \times 3 = 24 \\
 & \text{So, 516 is a perfect square.}
 \end{aligned}$$

$$\begin{array}{r|l}
 (d) & 2 \quad 1296 \\
 \hline
 & 2 \quad 648 \\
 \hline
 & 2 \quad 324 \\
 \hline
 & 2 \quad 162 \\
 \hline
 & 3 \quad 81 \\
 \hline
 & 3 \quad 27 \\
 \hline
 & 3 \quad 9 \\
 \hline
 & 3
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \\
 = & 2 \times 2 \times 3 \times 3 = 36 \\
 & \text{So, 1296 is a perfect square}
 \end{aligned}$$

$$\begin{array}{r|l}
 (e) & 2 \quad 2500 \\
 \hline
 & 2 \quad 1250 \\
 \hline
 & 5 \quad 625 \\
 \hline
 & 5 \quad 125 \\
 \hline
 & 5 \quad 25 \\
 \hline
 & 5
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 5 \times 5 \times 5 \times 5 \\
 = & 2 \times 5 \times 5 = 50 \\
 & \text{So, 2500 is a perfect square}
 \end{aligned}$$

$$\begin{array}{r|l}
 (f) & 2 \quad 2116 \\
 \hline
 & 2 \quad 1058 \\
 \hline
 & 23 \quad 529 \\
 \hline
 & 23
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 2 \times 23 \times 23 \\
 = & 2 \times 23 = 46 \\
 & \text{So, 2116 is a perfect square.}
 \end{aligned}$$

$$\begin{array}{r|l}
 2. (a) & 2 \quad 36 \\
 \hline
 & 2 \quad 18 \\
 \hline
 & 3 \quad 9 \\
 \hline
 & 3
 \end{array}$$

$$\begin{aligned}
 & 2 \times 2 \times 3 \times 3 \\
 = & 2 \times 3 = 6 \text{ is an even number}
 \end{aligned}$$

$$(b) \begin{array}{r|l} 7 & 49 \\ \hline & 7 \end{array} = 7 \times 7$$

= 7 is an odd number

$$(c) \begin{array}{r|l} 2 & 324 \\ \hline 2 & 162 \\ \hline 3 & 81 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline & 3 \end{array}$$

$2 \times 2 \times 3 \times 3 \times 3 \times 3$
 = $2 \times 3 \times 3 = 18$ is an even number

$$(d) \begin{array}{r|l} 17 & 289 \\ \hline & 17 \end{array} = 17 \times 17$$

= 17 is an odd number

$$(e) \begin{array}{r|l} 3 & 441 \\ \hline 3 & 147 \\ \hline 7 & 49 \\ \hline & 7 \end{array} = 3 \times 3 \times 7 \times 7$$

= $3 \times 7 = 21$ is an odd number

$$(f) \begin{array}{r|l} 3 & 1089 \\ \hline 3 & 363 \\ \hline 11 & 121 \\ \hline & 11 \end{array} = 3 \times 3 \times 11 \times 11$$

= $3 \times 11 = 33$ is an odd number

3. (a) $\begin{array}{r|l} 2 & 1800 \\ \hline 2 & 900 \\ \hline 3 & 450 \\ \hline 3 & 150 \\ \hline 2 & 50 \\ \hline 5 & 25 \\ \hline & 5 \end{array}$

$2 \times 2 \times 3 \times 3 \times 2 \times 5 \times 5$
 To make it a perfect square it must be multiplied by 2

$$\begin{array}{r|l}
 2 & 2904 \\
 \hline
 2 & 1452 \\
 \hline
 2 & 726 \\
 \hline
 3 & 363 \\
 \hline
 11 & 121 \\
 \hline
 & 11
 \end{array}$$

$$2 \times 2 \times 2 \times 3 \times 11 \times 11$$

To make it a perfect square it must be multiplied by 6

$$\begin{array}{r|l}
 3 & 1323 \\
 \hline
 3 & 441 \\
 \hline
 3 & 147 \\
 \hline
 7 & 49 \\
 \hline
 & 7
 \end{array}$$

$$3 \times 3 \times 3 \times 7 \times 7$$

So, it must be multiplied by 3

$$\begin{array}{r|l}
 2 & 35280 \\
 \hline
 2 & 17640 \\
 \hline
 2 & 8820 \\
 \hline
 3 & 4410 \\
 \hline
 3 & 1470 \\
 \hline
 7 & 490 \\
 \hline
 7 & 70 \\
 \hline
 2 & 10 \\
 \hline
 & 5
 \end{array}$$

$$2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7 \times 7 \times 5$$

So, to make it a perfect square it must be multiplied by 5

$$\begin{array}{r|l}
 2 & 17640 \\
 \hline
 2 & 8820 \\
 \hline
 2 & 4410 \\
 \hline
 3 & 2205 \\
 \hline
 3 & 735 \\
 \hline
 5 & 245 \\
 \hline
 7 & 49 \\
 \hline
 & 7
 \end{array}$$

$$2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 7 \times 7$$

So, to make it a perfect square it must be multiplied by $2 \times 5 = 10$

$$\begin{array}{r|l}
 2 & 180 \\
 \hline
 2 & 90 \\
 \hline
 3 & 45 \\
 \hline
 3 & 15 \\
 \hline
 & 5
 \end{array}$$

$$2 \times 2 \times 3 \times 3 \times 5$$

To make it a perfect square
it must be divided by 5

$$\begin{array}{r|l}
 3 & 1575 \\
 \hline
 3 & 525 \\
 \hline
 5 & 175 \\
 \hline
 5 & 35 \\
 \hline
 & 7
 \end{array}$$

$$3 \times 3 \times 5 \times 5 \times 7$$

To make it a perfect square it
must be divided by 7

$$\begin{array}{r|l}
 2 & 3174 \\
 \hline
 3 & 1587 \\
 \hline
 23 & 529 \\
 \hline
 & 23
 \end{array}$$

$$2 \times 2 \times 3 \times 23 \times 23$$

So, it must be divided by $2 \times 3 = 6$

$$\begin{array}{r|l}
 2 & 6912 \\
 \hline
 2 & 3456 \\
 \hline
 2 & 1728 \\
 \hline
 2 & 864 \\
 \hline
 2 & 432 \\
 \hline
 2 & 216 \\
 \hline
 2 & 108 \\
 \hline
 2 & 54 \\
 \hline
 3 & 27 \\
 \hline
 3 & 9 \\
 \hline
 & 3
 \end{array}$$

$$2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3$$

= So, it must be divided by 3

$$\begin{array}{r|l}
 2 & 16652 \\
 \hline
 2 & 8326 \\
 \hline
 & 4163
 \end{array}$$

$$2 \times 2 \times 4163$$

it must be divided by 4163

5. (a)
$$\begin{array}{r|l} 3 & 35943 \\ \hline & 11981 \end{array}$$
 It is not a perfect square because it does not make complete pairs.
- (b)
$$\begin{array}{r|l} 2 & 57323 \\ \hline & 28661 \end{array}$$
 It does not make complete pairs.
- (c)
$$\begin{array}{r|l} 2 & 333222 \\ \hline & 166611 \end{array}$$
 It does not make complete pairs.
- (d)
$$\begin{array}{r|l} 3 & 23805 \\ \hline 3 & 7935 \\ \hline 5 & 2645 \\ \hline 23 & 529 \\ \hline & 23 \end{array}$$
 $3 \times 3 \times 5 \times 23 \times 23$
It does not make complete pairs

6. Pythagorean triplets obey the following relation

$$(2m)^2 + (m^2 - 1)^2 = (m^2 + 1)^2$$

- (a) For a given natural number ' m ' other than 1, we get a triplet such as $(2m)$, $(m^2 - 1)$, $(m^2 + 1)$

One member is 8 means $2m = 8$

$$\text{So } m = \frac{8}{2} = 4$$

$$(2m), (m^2 - 1), (m^2 + 1)$$

$$(2 \times 4), (4^2 - 1), (4^2 + 1)$$

$$8, 15, 17$$

$$8^2 + 15^2 = 17^2$$

$$64 + 225 = 289$$

So, other members of triplet are 15 and 17.

- (b) Here $2m = 12$, $m = 6$

$$\text{So } (m^2 - 1) = (6^2 - 1) = 35$$

$$\text{and } (m^2 + 1) = (6^2 + 1) = 37$$

$$12^2 + 35^2 = 37^2$$

$$144 + 1225 = 1369 \quad \text{So, 35 and 37}$$

(c) Here $2m = 10$, $m = 5$
 So $(m^2 - 1) = 5^2 - 1 = 24$
 and $m^2 + 1 = 5^2 + 1 = 26$
 $(10)^2 + (24)^2 = (26)^2$
 $100 + 576 = 676$ So, 24 and 26

(d) Here $2m = 14$, $m = 7$
 So, $(m^2 - 1) = 7^2 - 1 = 48$
 and $(m^2 + 1) = 7^2 + 1 = 50$
 $(14)^2 + (48)^2 = (50)^2$
 $196 + 2304 = 2500$

So, 48 and 50

(e) Here $2m = 16$; $m = 8$
 So, $(m^2 - 1) = 8^2 - 1 = 63$
 and $(m^2 + 1) = 8^2 + 1 = 65$
 $(16)^2 + (63)^2 = (65)^2$
 $256 + 3969 = 4225$

So, 63 and 65

7. (a) As we know,
 Sum of first 5 odd numbers $= (5)^2 = 25$
 So, $1 + 3 + 5 + 7 + 9 = 25$
 (b) Sum of first 6 odd numbers $= (6)^2 = 36$
 So, $1 + 3 + 5 + 7 + 9 + 11 = 36$
 (c) Sum of first 7 odd numbers $= (7)^2 = 49$
 So, $1 + 3 + 5 + 7 + 9 + 11 + 13 = 49$
 (d) Sum of first 8 odd numbers $= (8)^2 = 64$
 So, $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 = 64$

8. Given Pattern is :

$$1^2 = 1$$

$$11^2 = 121$$

$$111^2 = 12321$$

So (a) $(1111)^2 = 1234321$

(b) $111111^2 = 12345654321$

9. Given pattern is

$$11^2 = 121$$

$$101^2 = 10201$$

$$1001^2 = 1002001$$

$$10001^2 = 100020001$$

$$100001^2 = 10000200001$$

Exercise 3B

1. (a) Prime factorization of

2	144	
2	72	
2	36	
2	18	
		$2 \times 2 \times 2 \times 2 \times 3 \times 3$
3	9	
		Square root = $2 \times 2 \times 3 = 12$
3	3	
	1	

(b) 225 =	3	225	
	3	75	
	5	25	
			$3 \times 3 \times 5 \times 5$
	5	5	
			Square root = $3 \times 5 = 15$
		1	

(c) 324 =	2	324	
	2	162	
	3	81	
			$2 \times 2 \times 3 \times 3 \times 3 \times 3$
	3	27	
			square root = $2 \times 3 \times 3 = 18$
	3	9	
	3	3	
		1	

(d) $729 =$

3	729
3	243
3	81
3	27
3	9
3	3
	1

$3 \times 3 \times 3 \times 3 \times 3 \times 3$
square root $= 3 \times 3 \times 3 = 27$

(e) 1296

Prime factors of 1296 $= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$

Square root $= 2 \times 2 \times 3 \times 3 = 36$

(f) 2304

Prime factors of 2304 $= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3$

Square root $= 2 \times 2 \times 2 \times 2 \times 3 = 48$

(g) 7056

Prime factors of 7056 $= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7 \times 7$

Square root $= 2 \times 2 \times 3 \times 7 = 84$

(h) 11025

Prime factors of 11025 $= 3 \times 3 \times 5 \times 5 \times 7 \times 7$

Square root $= 3 \times 5 \times 7 = 105$

(i) 24336

Prime factors of 24336 $= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 13 \times 13$

Square root $= 2 \times 2 \times 3 \times 13 = 156$

(j) 30625

Prime factors of 30625 $= 5 \times 5 \times 5 \times 5 \times 7 \times 7$

Square root $= 5 \times 5 \times 7 = 175$

2. Prime factors of 396 are

2	396
2	198
3	99
3	33
	11

$396 = 2 \times 2 \times 3 \times 3 \times 11$

To make it perfect square,
we should multiply it by 11

Now, square root $= 2 \times 3 \times 11 = 66$

3. Prime factors of 1152

2	1152
2	576
2	288
2	144
2	72
2	36
2	18
3	9
	3

$$2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3$$

So, to make it a perfect square, we should divide it by 2

$$\text{Square root} = 2 \times 2 \times 2 \times 3 = 24$$

4. Square root of 1296 = $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 = 36$

So, number of rows = 36 and number of plants in each row = 36.

5. Square root of 202500

2	202500
2	101250
3	5625
3	1875
5	625
5	125
5	25
	5

$$2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 5 \times 5$$

$$= 2 \times 3 \times 5 \times 5 = 150$$

So, strength of the class = 150

6. First, we will take the LCM of 6, 8, 16

2	6, 8, 16
2	3, 4, 8
2	3, 2, 4
	3, 1, 2

$$2 \times 2 \times 2 \times 3 \times 2 = 48$$

To make it a perfect square we should multiply it by 3

So, least square number which is exactly divisible by each of

the numbers 6, 8, 16 = $48 \times 3 = 144$

7. LCM of 12, 15 and 20

2	12, 15, 20	$2 \times 2 \times 3 \times 5$ To make it perfect square we should multiply it by $3 \times 5 = 15$
2	6, 15, 10	
3	3, 15, 5	
5	1, 5, 5	
	1, 5, 5	

So, Least square number which is exactly divisible by each of the numbers 12, 15, and 20 is $2 \times 2 \times 3 \times 3 \times 5 \times 5 = 3600$

8. Total men = 335250

Left over men = 9

So, to arrange the other men in the form of square, we should take square root of $335250 - 9 = 335241$

Prime factors of $335241 = 3 \times 3 \times 193 \times 193$

Square root = $3 \times 193 = 579$

So, the men in each row = 579

Exercise 3C

1. (a)

	234	
2	54756	4
43	147	129
464	1856	1856
		×

(b)

	625	
6	390625	36
122	306	244
1245	6225	6225
		×

(c)

	222	4937284
2		4
42		93 84
442		972 884
4442		8884 8884
		×

(d)

	1213	1471369
1		1
22		47 44
241		313 241
2423		7269 7269
		×

(e)

	3107	9653449
3		9
61		65 61
6207		43449 43449
		×

(f)

	4545	20657025
4		16
85		465 425
904		4070 3616
9085		45425 45425
		×

(g)

	12351	152547201
1		1
22		52 44
243		854 729
2465		12572 12325
24701		24701 24701
		×

(h)

	9070	82264900
9		81
1807		12649 12649
		×

$$\begin{array}{r}
 \text{(i)} \quad 56804 \\
 5 \overline{) 3226694416} \\
 \underline{25} \\
 106 \overline{) 726} \\
 \underline{636} \\
 1128 \overline{) 9069} \\
 \underline{9024} \\
 113604 \overline{) 454416} \\
 \underline{454416} \\
 \times
 \end{array}$$

$$\begin{array}{r}
 \text{(j)} \quad 7708 \\
 7 \overline{) 59413264} \\
 \underline{49} \\
 147 \overline{) 1041} \\
 \underline{1029} \\
 15408 \overline{) 123264} \\
 \underline{123264} \\
 \times
 \end{array}$$

2. **Number** **Number of digits in the square root**

$$\text{(a)} \quad 441 = \frac{3+1}{2} = 2$$

$$\text{(b)} \quad 67600 = \frac{5+1}{2} = 3$$

$$\text{(c)} \quad 288369 = \frac{6}{2} = 3$$

$$\begin{array}{r}
 \text{3. (a)} \quad 48 \\
 4 \overline{) 2361} \\
 \underline{16} \\
 88 \overline{) 761} \\
 \underline{704} \\
 \overline{) 57}
 \end{array}$$

So, 57 should be subtracted.

$$\begin{array}{r}
 \text{(b)} \quad 50 \\
 5 \overline{) 2509} \\
 \underline{25} \\
 10 \overline{) 09} \\
 \underline{00} \\
 \overline{) 9}
 \end{array}$$

So, 9 should be subtracted.

$$\begin{array}{r}
 \text{(c)} \quad 87 \\
 8 \overline{) 7581} \\
 \underline{64} \\
 167 \overline{) 1181} \\
 \underline{1169} \\
 \overline{) 12}
 \end{array}$$

So, 12 should be subtracted

$$\begin{array}{r}
 \text{(d)} \quad 208 \\
 2 \overline{) 43379} \\
 \underline{4} \\
 408 \overline{) 3379} \\
 \underline{3264} \\
 \overline{) 95}
 \end{array}$$

So, 95 should be subtracted

(e)

$$\begin{array}{r}
 586 \\
 5 \overline{) 343500} \\
 \underline{25} \\
 108 \overline{) 935} \\
 \underline{884} \\
 1166 \overline{) 7100} \\
 \underline{6996} \\
 \hline
 104
 \end{array}$$

So, 104 should be subtracted.

4. (a)

$$\begin{array}{r}
 71 \\
 7 \overline{) 4931} \\
 \underline{49} \\
 141 \overline{) 31} \\
 \underline{141} \\
 \hline
 -110
 \end{array}$$

So, 110 must be added.

(b)

$$\begin{array}{r}
 79 \\
 7 \overline{) 6203} \\
 \underline{49} \\
 149 \overline{) 1303} \\
 \underline{1341} \\
 \hline
 -38
 \end{array}$$

So, 38 must be added.

(c)

$$\begin{array}{r}
 712 \\
 7 \overline{) 506900} \\
 \underline{49} \\
 141 \overline{) 160} \\
 \underline{141} \\
 1422 \overline{) 2800} \\
 \underline{2844} \\
 \hline
 -44
 \end{array}$$

So, 44 should be added.

(d)

$$\begin{array}{r}
 443 \\
 4 \overline{) 176201} \\
 \underline{16} \\
 84 \overline{) 362} \\
 \underline{336} \\
 883 \overline{) 2601} \\
 \underline{2649} \\
 \hline
 -48
 \end{array}$$

So, 48 should be added.

(e)

$$\begin{array}{r}
 2125 \\
 2 \overline{) 4515600} \\
 \underline{4} \\
 41 \overline{) 51} \\
 \underline{41} \\
 422 \overline{) 1056} \\
 \underline{844} \\
 4245 \overline{) 21200} \\
 \underline{21225} \\
 \hline
 -25
 \end{array}$$

So, 25 should be added.

5. Largest 5-digit number is = 99999

$$\begin{array}{r}
 316 \\
 3 \overline{) 99999} \\
 \underline{9} \\
 61 \quad 99 \\
 \underline{61} \\
 626 \quad 3899 \\
 \underline{3696} \\
 203
 \end{array}$$

So, $99999 - 203 = 99786$ is the perfect square.

6. Least 6-digit number is 100000

$$\begin{array}{r}
 317 \\
 3 \overline{) 100000} \\
 \underline{9} \\
 61 \quad 100 \\
 \underline{61} \\
 621 \quad 3900 \\
 \underline{4349} \\
 -419
 \end{array}$$

So, $100000 + 419 = 100419$ is the perfect square.

7.

$$\begin{array}{r}
 89 \\
 8 \overline{) 7912} \\
 \underline{64} \\
 169 \quad 1512 \\
 \underline{1521} \\
 -9
 \end{array}$$

So, $7912 + 9 = 7921$ is the perfect square and 79 will be the square root.

8.

$$\begin{array}{r}
 208 \\
 2 \overline{) 43379} \\
 \underline{4} \\
 408 \quad 3379 \\
 \underline{3264} \\
 115
 \end{array}$$

So, $43379 - 115 = 43264$ is the perfect square and 208 is the square root.

9. First we must subtract 10 from 120419 cause the general need 10 extra men.

So, $120419 - 10 = 120409$

$$\begin{array}{r}
 347 \\
 3 \overline{)120409} \\
 \underline{9} \\
 64 \overline{)304} \\
 \underline{256} \\
 687 \overline{)4809} \\
 \underline{4809} \\
 \times
 \end{array}$$

So, in front row 347 men were there.

10. Side of the square field is = $\sqrt{60025}$

$$\begin{array}{r}
 245 \\
 2 \overline{)60025} \\
 \underline{4} \\
 44 \overline{)200} \\
 \underline{176} \\
 485 \overline{)2425} \\
 \underline{2425} \\
 \times
 \end{array}$$

Side = 245m

Perimeter = $4 \times 245 = 980\text{m}$

Speed = 18km/hr *or*
= 5 m/sec

So, to cover 980 m the time he

will take $\frac{980}{5} = 196 \text{ sec}$

Exercise 3D

1. (a) $\sqrt{\frac{529}{841}} = \sqrt{\frac{529}{841}} = \sqrt{\frac{23 \times 23}{29 \times 29}} = \frac{23}{29}$
- (b) $\sqrt{\frac{81}{225}} = \sqrt{\frac{81}{225}} = \sqrt{\frac{9 \times 9}{15 \times 15}} = \frac{9}{15}$
- (c) $\sqrt{2\frac{7}{9}} = \sqrt{\frac{25}{9}} = \sqrt{\frac{5 \times 5}{3 \times 3}} = \frac{5}{3}$ or $1\frac{2}{3}$
- (d) $\sqrt{1\frac{56}{169}} = \sqrt{\frac{225}{169}} = \sqrt{\frac{15 \times 15}{13 \times 13}} = \frac{15}{13}$ or $1\frac{2}{13}$
- (e) $\sqrt{6\frac{115}{289}} = \sqrt{\frac{1849}{289}} = \sqrt{\frac{43 \times 43}{17 \times 17}} = \frac{43}{17}$ or $2\frac{9}{17}$
- (f) $25\frac{544}{729} = \sqrt{\frac{18769}{225}} = \sqrt{\frac{137 \times 137}{27 \times 27}} = \frac{137}{27}$

$$\begin{array}{r}
 137 \\
 1 \overline{) 18769} \\
 \underline{1} \\
 23 \overline{) 87} \\
 \underline{69} \\
 267 \overline{) 1869} \\
 \underline{1869} \\
 \times
 \end{array}$$

$$\begin{array}{r}
 27 \\
 2 \overline{) 729} \\
 \underline{4} \\
 47 \overline{) 329} \\
 \underline{329} \\
 \times
 \end{array}$$

$$(g) \sqrt{3 \frac{234}{3025}} = \sqrt{\frac{9409}{3025}} = \sqrt{\frac{97 \times 97}{55 \times 55}} = \frac{97}{55}$$

$$\begin{array}{r}
 97 \\
 9 \overline{) 9409} \\
 \underline{81} \\
 187 \overline{) 1309} \\
 \underline{1309} \\
 \times
 \end{array}$$

$$\begin{array}{r}
 55 \\
 5 \overline{) 3025} \\
 \underline{25} \\
 105 \overline{) 525} \\
 \underline{525} \\
 \times
 \end{array}$$

$$(h) \sqrt{42 \frac{583}{1369}} = \sqrt{\frac{58081}{1369}} = \sqrt{\frac{241 \times 241}{37 \times 37}} = \frac{241}{37}$$

$$\begin{array}{r}
 241 \\
 2 \overline{) 58081} \\
 \underline{4} \\
 44 \overline{) 180} \\
 \underline{176} \\
 401 \overline{) 481} \\
 \underline{481} \\
 \times
 \end{array}$$

$$\begin{array}{r}
 37 \\
 3 \overline{) 1369} \\
 \underline{9} \\
 67 \overline{) 469} \\
 \underline{469} \\
 \times
 \end{array}$$

$$2. (a) \sqrt{\frac{80}{405}} = \sqrt{\frac{16}{81}} = \sqrt{\frac{4 \times 4}{9 \times 9}} = \frac{4}{9}$$

$$(b) \sqrt{\frac{243}{867}} = \sqrt{\frac{81}{289}} = \sqrt{\frac{9 \times 9}{17 \times 17}} = \frac{9}{17}$$

$$(c) \sqrt{\frac{1.44}{2.25}} = \sqrt{\frac{144}{225}} = \sqrt{\frac{12 \times 12}{15 \times 15}} = \frac{12}{15}$$

$$(d) \sqrt{\frac{36.1}{102.4}} = \sqrt{\frac{361}{1024}} = \sqrt{\frac{19 \times 19}{32 \times 32}} = \frac{19}{32}$$

3. (a)

$$\begin{array}{r} 1.11 \\ 1 \overline{) 1.2321} \\ \underline{1} \\ 21 \\ \underline{21} \\ 221 \\ \underline{221} \\ \times \end{array}$$

(b)

$$\begin{array}{r} 2.22 \\ 2 \overline{) 4.9284} \\ \underline{4} \\ 42 \\ \underline{42} \\ 442 \\ \underline{442} \\ \times \end{array}$$

(c)

$$\begin{array}{r} 3.33 \\ 3 \overline{) 11.0889} \\ \underline{9} \\ 63 \\ \underline{63} \\ 663 \\ \underline{663} \\ \times \end{array}$$

(d)

$$\begin{array}{r} 0.85 \\ 8 \overline{) 0.7225} \\ \underline{64} \\ 165 \\ \underline{165} \\ \times \end{array}$$

(e)

$$\begin{array}{r} 0.222 \\ 2 \overline{) 0.049284} \\ \underline{4} \\ 42 \\ \underline{42} \\ 442 \\ \underline{442} \\ \times \end{array}$$

(f)

$$\begin{array}{r} 0.333 \\ 3 \overline{) 0.110889} \\ \underline{9} \\ 63 \\ \underline{63} \\ 663 \\ \underline{663} \\ \times \end{array}$$

$$\begin{array}{r}
 \text{(g)} \quad 3.767 \\
 3 \overline{) 14.190289} \\
 \underline{9} \\
 67 \\
 \underline{519} \\
 469 \\
 746 \\
 \underline{5002} \\
 4476 \\
 7527 \\
 \underline{52689} \\
 52689 \\
 \underline{ \times}
 \end{array}$$

$$\begin{array}{r}
 \text{(h)} \quad 12.35 \\
 1 \overline{) 152.5225} \\
 \underline{1} \\
 22 \\
 \underline{52} \\
 44 \\
 243 \\
 \underline{852} \\
 729 \\
 2465 \\
 \underline{12325} \\
 12325 \\
 \underline{ \times}
 \end{array}$$

$$4. \sqrt{\frac{3}{7}} = 0.42857142$$

(after dividing 3 by 7)

$$\begin{array}{r}
 0.6546 \\
 6 \overline{) 0.42857142} \\
 \underline{36} \\
 125 \\
 \underline{685} \\
 625 \\
 1304 \\
 \underline{6071} \\
 5216 \\
 13086 \\
 \underline{85542} \\
 78516 \\
 \underline{7026}
 \end{array}$$

So, 0.6546

5.

$$\begin{array}{r}
 125 \\
 1 \overline{) 15625} \\
 \underline{1} \\
 22 \\
 \underline{56} \\
 44 \\
 245 \\
 \underline{1225} \\
 1225 \\
 \underline{ \times}
 \end{array}$$

$$\therefore 15625 = 125$$

$$\text{So } \sqrt{156.25} = 12.5$$

$$\text{and } \sqrt{1.5625} = 1.25$$

$$\text{and } \sqrt{156.25} + \sqrt{1.5625}$$

$$12.50 + 1.25 = 13.75$$

$$\begin{array}{r}
 1 \overline{) 3.000000} \\
 \underline{1} \\
 27 \\
 \underline{200} \\
 189 \\
 \underline{343} \\
 1100 \\
 \underline{1029} \\
 3462 \\
 \underline{7100} \\
 6924 \\
 \underline{176}
 \end{array}$$

Ans. 1.732

$$\begin{array}{r}
 2 \overline{) 5.000000} \\
 \underline{4} \\
 42 \\
 \underline{100} \\
 84 \\
 \underline{443} \\
 1600 \\
 \underline{1329} \\
 4466 \\
 \underline{27100} \\
 26796 \\
 \underline{304}
 \end{array}$$

Ans. : 2.236

$$\begin{array}{r}
 3 \overline{) 10.000000} \\
 \underline{9} \\
 61 \\
 \underline{100} \\
 61 \\
 \underline{626} \\
 3900 \\
 \underline{3756} \\
 6322 \\
 \underline{14400} \\
 12644 \\
 \underline{1756}
 \end{array}$$

So, 30162

$$\begin{array}{r}
 1 \overline{) 237.615000} \\
 \underline{1} \\
 25 \\
 \underline{137} \\
 125 \\
 \underline{304} \\
 1261 \\
 \underline{1216} \\
 3081 \\
 \underline{4550} \\
 3081 \\
 \underline{30821} \\
 146900 \\
 \underline{123284} \\
 23616
 \end{array}$$

Ans. : 15.414

$$(e) 10 \frac{2}{3} = \frac{32}{3} = 10.666667$$

$$\begin{array}{r}
 3 \overline{) 10.666667} \\
 \underline{9} \\
 62 \\
 \underline{166} \\
 124 \\
 \underline{646} \\
 4266 \\
 \underline{3876} \\
 6525 \\
 \underline{39067} \\
 32625 \\
 \underline{6442}
 \end{array}$$

So, 3.265

7. $\sqrt{103.0225}$

$$\begin{array}{r}
 10.15 \\
 1 \overline{) 103.0225} \\
 \underline{1} \\
 201 \\
 \underline{201} \\
 2025 \\
 \underline{2025} \\
 \times
 \end{array}$$

$\therefore \sqrt{103.0225} = 10.15$

so, $\sqrt{10302.25} = 101.5$

and $\sqrt{1.030225} = 1.015$

8. Area of the square field = 325m^2
 Side of the square field = $\sqrt{325}$

$$\begin{array}{r}
 18.027 \\
 1 \overline{) 325.000000} \\
 \underline{1} \\
 28 \\
 \underline{225} \\
 224 \\
 3602 \\
 \underline{10000} \\
 7204 \\
 36047 \\
 \underline{279600} \\
 252329 \\
 \underline{27271}
 \end{array}$$

So, side = 18.027m

Check Your Mental Maths IQ

1. $63 = 3 \times 3 \times 7$

To make 63 a perfect square we should divide it by 7

2. $\sqrt{20\frac{1}{4}} = \sqrt{\frac{81}{4}} = \sqrt{\frac{9 \times 9}{2 \times 2}} = \frac{9}{2}$ or $4\frac{1}{2}$

$$\begin{array}{r}
 0.447 \\
 4 \overline{) 0.20000} \\
 \underline{16} \\
 84 \overline{) 400} \\
 \underline{336} \\
 887 \overline{) 6400} \\
 \underline{6209} \\
 \hline
 191
 \end{array}$$

$$\begin{aligned}
 4. (50)^2 - (49)^2 \\
 &= (50 + 49)(50 - 49) \\
 &= 99 \times 1 = 99
 \end{aligned}$$

5. No

$$\begin{array}{r}
 8 \\
 8 \overline{) 79} \\
 \underline{64} \\
 15
 \end{array}
 \quad \text{and} \quad
 \begin{array}{r}
 9 \\
 9 \overline{) 79} \\
 \underline{81} \\
 -2
 \end{array}$$

So, 2 must be added to make it perfect square.

$$7. \sqrt{0.81} = \sqrt{\frac{81}{100}} = \sqrt{\frac{9 \times 9}{10 \times 10}} = \frac{9}{10} = 0.9$$

Multiple Choice Questions

1. (c) $63 = 3 \times 3 \times 7$

To make it perfect square it must be divided by 7

2. (c) $\sqrt{5^2 \times 4^2 \times 36} = ?$

$$\sqrt{5^2 \times 4^2 \times 6 \times 6} = \sqrt{5^2 \times 4^2 \times 6^2} = 5 \times 4 \times 6 = 120$$

3. (d) We know sum of first 10 odd numbers $= (10)^2 = 100$

4. (b)

$$\begin{array}{r}
 15 \\
 1 \overline{) 250} \\
 \underline{1} \\
 25 \overline{) 150} \\
 \underline{125} \\
 25
 \end{array}$$

So, 25 must be added to make it a perfect square

5. (a) $25^2 - 24^2 = (25 + 24)(25 - 24) = 49 \times 1 = 49$

6. (d)

$$\begin{array}{r}
 25 \\
 2 \overline{) 600} \\
 \underline{4} \\
 200 \\
 \underline{225} \\
 25
 \end{array}$$

So, 25 must be added to make it a perfect square

7. (b) 121; \therefore Unit place is odd

8. (b) Smallest three-digit number which is a perfect square is 100

9. (c) Value of

$$\sqrt{49} + \sqrt{0.49} + \sqrt{0.0049} = 7 + 0.7 + 0.07 = 7.77$$

4

Cube and Cube Roots

Exercise 4A

1. (a) $(7)^3 = 7 \times 7 \times 7 = 343$

(b) $(12)^3 = 12 \times 12 \times 12 = 1728$

(c) $(25)^3 = 25 \times 25 \times 25 = 15625$

(d) $(30)^3 = 30 \times 30 \times 30 = 27000$

(e) $(45)^3 = 45 \times 45 \times 45 = 91125$

(f) $\left(\frac{3}{5}\right)^3 = \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} = \frac{27}{125}$

(g) $\left(\frac{-4}{9}\right)^3 = \frac{-4}{9} \times \frac{-4}{9} \times \frac{-4}{9} = \frac{-64}{729}$

(h) $\left(2\frac{5}{7}\right)^3 = \left(\frac{19}{7}\right)^3 = \frac{19}{7} \times \frac{19}{7} \times \frac{19}{7} = \frac{6859}{343} = 19\frac{342}{343}$

(i) $\left(1\frac{9}{10}\right)^3 = \left(\frac{19}{10}\right)^3 = \frac{19}{10} \times \frac{19}{10} \times \frac{19}{10} = \frac{6859}{1000} = 6\frac{859}{1000}$

$$(j) (0.03)^3 = \frac{3}{100} \times \frac{3}{100} \times \frac{3}{100} = \frac{27}{1000000} = 0.000027$$

2. (a)
$$\begin{array}{r|l} 2 & 108 \\ \hline 2 & 54 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

No

(c)
$$\begin{array}{r|l} 2 & 612 \\ \hline 2 & 306 \\ \hline 3 & 153 \\ \hline 3 & 51 \\ \hline & 17 \end{array}$$

No

(e)
$$\begin{array}{r|l} 2 & 2744 \\ \hline 2 & 1372 \\ \hline 2 & 686 \\ \hline 7 & 343 \\ \hline 7 & 49 \\ \hline & 7 \end{array}$$

Yes

(g)
$$\begin{array}{r|l} 3 & 9261 \\ \hline 3 & 3087 \\ \hline 3 & 1029 \\ \hline 7 & 343 \\ \hline 7 & 49 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$
 Yes

(b)
$$\begin{array}{r|l} 7 & 343 \\ \hline 7 & 49 \\ \hline & 7 \end{array}$$

Yes

(d)
$$\begin{array}{r|l} 2 & 5832 \\ \hline 2 & 2916 \\ \hline 2 & 1458 \\ \hline 3 & 729 \\ \hline 3 & 243 \\ \hline 3 & 81 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline & 3 \end{array}$$

Yes

(f)
$$\begin{array}{r|l} 2 & 4000 \\ \hline 2 & 2000 \\ \hline 2 & 1000 \\ \hline 2 & 500 \\ \hline 2 & 250 \\ \hline 5 & 125 \\ \hline 5 & 25 \\ \hline & 5 \end{array}$$

No

$$\begin{array}{r}
 \text{(h)} \quad 2 \overline{)13824} \\
 \underline{2 \quad 6912} \\
 2 \quad 3456 \\
 \underline{2 \quad 1728} \\
 2 \quad 864 \\
 \underline{2 \quad 432} \\
 2 \quad 216 \\
 \underline{2 \quad 108} \\
 2 \quad 54 \\
 \underline{3 \quad 27} \\
 3 \quad 9 \\
 \underline{3 \quad 3} \\
 1
 \end{array}$$

Yes

$$\begin{array}{r}
 \text{(i)} \quad 2 \overline{)74088} \\
 \underline{2 \quad 37044} \\
 2 \quad 18522 \\
 \underline{3 \quad 9261} \\
 3 \quad 3087 \\
 \underline{3 \quad 1029} \\
 7 \quad 343 \\
 \underline{7 \quad 49} \\
 7 \quad 7 \\
 \underline{\quad 1}
 \end{array}$$

Yes

3. 64, 512, 1000, 1728 and 13824

4. 125, 343, 1331, 3375 and 6859

$$\begin{array}{r}
 5. \quad 3 \overline{)675} \\
 \underline{3 \quad 225} \\
 3 \quad 75 \\
 \underline{5 \quad 25} \\
 5 \quad 5 \\
 \underline{\quad 1}
 \end{array}$$

$$3 \times 3 \times 3 \times 5 \times 5$$

So, it should be multiplied by 5 to make a perfect cube

$$\text{Required perfect cube} = 3 \times 5 = 15$$

$$\begin{array}{r}
 6. \quad 2 \overline{)2916} \\
 \underline{2 \quad 1458} \\
 3 \quad 729 \\
 \underline{3 \quad 243} \\
 3 \quad 81 \\
 \underline{3 \quad 27} \\
 3 \quad 9 \\
 \underline{3 \quad 3} \\
 1
 \end{array}$$

$$2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3$$

It must be divided by $2 \times 2 = 4$

$$\text{So perfect cube} = 3 \times 3 = 9$$

$$7. \text{ Volume of the cube} = (\text{side})^3 = (3.8)^3 \\ = 3.8 \times 3.8 \times 3.8 = 54.872$$

Exercise 4B

1. (a)

2	216	
2	108	
2	54	
3	27	$2 \times 2 \times 2 \times 3 \times 3 \times 3$
3	9	$2 \times 3 = 6$
3	3	
	1	

(b) $343 = 7 \times 7 \times 7$; So cube root = 7

(c)

2	1728	
2	864	
2	432	
2	216	$2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3$
2	108	$= 2 \times 2 \times 3 = 12$
2	54	
3	27	
3	9	
3	3	
	1	

(d)

2	2744	
2	1372	$2 \times 2 \times 2 \times 7 \times 7 \times 7$
2	686	$= 2 \times 7 = 14$
7	343	
7	49	
7	7	
	1	

$$\begin{array}{r|l}
 (e) & 2 \quad 10648 \\
 & \hline
 & 2 \quad 5324 \\
 & \hline
 & 2 \quad 2662 \\
 & \hline
 & 11 \quad 1331 \\
 & \hline
 & 11 \quad 121 \\
 & \hline
 & 11 \quad 11 \\
 & \hline
 & 1
 \end{array}
 \quad
 \begin{array}{l}
 2 \times 2 \times 2 \times 11 \times 11 \times 11 \\
 = 2 \times 11 = 22
 \end{array}$$

$$\begin{array}{r|l}
 (f) & 2 \quad 27000 \\
 & \hline
 & 2 \quad 13500 \\
 & \hline
 & 2 \quad 6750 \\
 & \hline
 & 3 \quad 3375 \\
 & \hline
 & 3 \quad 1125 \\
 & \hline
 & 3 \quad 375 \\
 & \hline
 & 5 \quad 125 \\
 & \hline
 & 5 \quad 25 \\
 & \hline
 & 5 \quad 5 \\
 & \hline
 & 1
 \end{array}
 \quad
 \begin{array}{l}
 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5 \times 5 \\
 = 2 \times 3 \times 5 = 30
 \end{array}$$

$$\begin{array}{r|l}
 (g) & 3 \quad 91125 \\
 & \hline
 & 3 \quad 30375 \\
 & \hline
 & 3 \quad 10125 \\
 & \hline
 & 3 \quad 3375 \\
 & \hline
 & 3 \quad 1125 \\
 & \hline
 & 3 \quad 375 \\
 & \hline
 & 5 \quad 125 \\
 & \hline
 & 5 \quad 25 \\
 & \hline
 & 5 \quad 5 \\
 & \hline
 & 1
 \end{array}
 \quad
 \begin{array}{l}
 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 5 \times 5 \times 5 \\
 = 3 \times 3 \times 5 = 45
 \end{array}$$

$$\begin{array}{r|l}
 (h) & 17 \quad 4913 \\
 & \hline
 & 17 \quad 289 \\
 & \hline
 & 17 \quad 17 \\
 & \hline
 & 1
 \end{array}
 \quad
 \begin{array}{l}
 17 \times 17 \times 17 = 17 \text{ (put - sign)} \\
 \text{So cube root} = -7
 \end{array}$$

$$\begin{array}{r|l}
 2 & 5832 \\
 \hline
 2 & 2916 \\
 \hline
 2 & 1458 \\
 \hline
 3 & 729 \\
 \hline
 3 & 243 \\
 \hline
 3 & 81 \\
 \hline
 3 & 27 \\
 \hline
 3 & 9 \\
 \hline
 3 & 3 \\
 \hline
 & 1
 \end{array}
 \begin{array}{l}
 \\
 \\
 \\
 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \\
 = 2 \times 3 \times 3 = 18 \text{ (put -ve sign)} \\
 = -18 \\
 \\
 \\
 \\
 \\
 \\
 \\
 \end{array}$$

$$\begin{array}{r|l}
 2 & 32768 \\
 \hline
 2 & 16384 \\
 \hline
 2 & 8192 \\
 \hline
 2 & 4016 \\
 \hline
 2 & 2048 \\
 \hline
 2 & 1024 \\
 \hline
 2 & 512 \\
 \hline
 2 & 256 \\
 \hline
 2 & 128 \\
 \hline
 2 & 64 \\
 \hline
 2 & 32 \\
 \hline
 2 & 16 \\
 \hline
 2 & 8 \\
 \hline
 2 & 4 \\
 \hline
 & 2
 \end{array}
 \begin{array}{l}
 \\
 \\
 \\
 \\
 \\
 \\
 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \\
 2 \times 2 \times 2 \times 2 \times 2 \\
 = 2 \times 2 \times 2 \times 2 \times 2 = 32 \text{ (put -ve sign)} \\
 -32 \\
 \\
 \\
 \\
 \\
 \\
 \\
 \\
 \\
 \end{array}$$

2. Show that

$$\begin{aligned}
 \text{(a) } \sqrt[3]{125 \times 64} &= \sqrt[3]{125} \times \sqrt[3]{64} \\
 \text{LHS } \sqrt[3]{125 \times 64} &= \sqrt[3]{5 \times 5 \times 5 \times 4 \times 4 \times 4} = 5 \times 4 = 20 \\
 \text{RHS } \sqrt[3]{125} &= \sqrt[3]{64} = 5 \times 4 = 20
 \end{aligned}$$

So, LHS = RHS (Hence proved)

$$(b) \sqrt[3]{216 \times (-343)} = \sqrt[3]{216} \times \sqrt[3]{-343}$$

$$\text{LHS } \sqrt[3]{6 \times 6 \times 6 \times (-7) \times (-7) \times (-7)} = 6 \times -7 = -42$$

$$\text{RHS } \sqrt[3]{216} \times \sqrt[3]{-343} = 6 \times -7 = -42$$

LHS = RHS (Hence proved)

$$(c) \sqrt[3]{(-216) \times 1728} = \sqrt[3]{-216} \times \sqrt[3]{1728}$$

$$\text{LHS } \sqrt[3]{(-216) \times 1728} = -6 \times 12 = -72$$

$$\text{RHS } \sqrt[3]{-216} \times \sqrt[3]{1728} = -6 \times 12 = -72$$

LHS = RHS (Hence proved)

3. Evaluate

$$(a) \sqrt[3]{1372} \times \sqrt[3]{1458}$$

$\begin{array}{r} 2 \overline{) 1372} \\ 2 \overline{) 686} \\ 7 \overline{) 343} \\ 7 \overline{) 49} \\ \hline 7 \end{array}$	$\begin{array}{r} 2 \overline{) 1458} \\ 3 \overline{) 729} \\ 3 \overline{) 243} \\ 3 \overline{) 81} \\ 3 \overline{) 27} \\ 3 \overline{) 9} \\ \hline 3 \end{array}$	$\begin{aligned} & \sqrt[3]{1372} \times \sqrt[3]{1458} \\ & 2 \times 2 \times 7 \times 7 \times 7 \times 2 \times 3 \times 3 \\ & \times 3 \times 3 \times 3 \times 3 \\ & = 2 \times 7 \times 3 \times 3 = 126 \end{aligned}$
---	--	---

$$(b) \sqrt[3]{392} \times \sqrt[3]{448}$$

$\begin{array}{r} 2 \overline{) 392} \\ 2 \overline{) 196} \\ 2 \overline{) 98} \\ 7 \overline{) 49} \\ 7 \overline{) 7} \\ \hline 1 \end{array}$	$\begin{array}{r} 2 \overline{) 448} \\ 2 \overline{) 224} \\ 2 \overline{) 112} \\ 2 \overline{) 56} \\ 2 \overline{) 28} \\ 2 \overline{) 14} \\ 7 \overline{) 7} \\ \hline 1 \end{array}$	$\begin{aligned} & \sqrt[3]{392} = 2 \times 2 \times 2 \times 7 \times 7 \\ & \sqrt[3]{448} = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 7 \\ & \text{So, } 2 \times 2 \times 2 \times 7 = 56 \end{aligned}$
---	--	---

(c) $\sqrt[3]{3375 \times 729}$

3	3375	3	729	
3	1125	3	243	$3 \times 3 \times 3 \times 5 \times 5 \times 5 \times 3 \times 3$
3	375	3	81	$\times 3 \times 3 \times 3 \times 3$
5	125	3	27	$= 3 \times 5 \times 3 \times 3 = 135$
5	25	3	9	
5	5	3	3	
	1		1	

4. (a) $\sqrt[3]{\frac{1331}{4096}} = \sqrt[3]{\frac{11 \times 11 \times 11}{16 \times 16 \times 16}} = \frac{11}{16}$

(b) $\sqrt[3]{\frac{-2197}{9261}} = \sqrt[3]{\frac{-13 \times -13 \times -13}{21 \times 21 \times 21}} = \frac{-13}{21}$

(c) $\sqrt[3]{\frac{4096}{-2197}} = \sqrt[3]{\frac{16 \times 16 \times 16}{-13 \times -13 \times -13}} = \frac{16}{-13}$

(d) $\sqrt[3]{\frac{-3375}{-2744}} = \sqrt[3]{\frac{15 \times 15 \times 15}{14 \times 14 \times 14}} = \frac{15}{14}$

5. $\sqrt[3]{0.001331} = \sqrt[3]{\frac{1331}{1000000}} = \sqrt{\frac{11 \times 11 \times 11}{100 \times 100 \times 100}} = \frac{11}{10} = 0.11$

6.

2	17496	
2	8748	
2	4374	
3	2187	
3	729	
3	243	
3	81	
3	27	
3	9	
3	3	
	1	

$2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3$
 $\times 3 \times 3$

So, to make it a perfect
we must multiply it by $3 \times 3 = 9$

So, cube root =
 $2 \times 3 \times 3 \times 3 = 54$

$$\begin{array}{r}
 7. \quad 3 \overline{)1323} \\
 \underline{3 \quad 441} \\
 3 \quad 147 \\
 \underline{7 \quad 49} \\
 7 \quad 7 \\
 \underline{7} \\
 1
 \end{array}$$

$$3 \times 3 \times 3 \times 7 \times 7$$

To make it a perfect cube it must be divided by $7 \times 7 = 49$

So, cube root of the number = 3

8. Volume of the cubical box = 13.824 cubic metres

$$\text{Length of each side of the box} = \sqrt[3]{13.824} = \sqrt[3]{\frac{13824}{1000}}$$

$$\sqrt[3]{\frac{13824}{1000}} = \sqrt{\frac{24 \times 24 \times 24}{10 \times 10 \times 10}} = \frac{24}{10} = 2.4 \text{ m}$$

Check Your Mental Math IQ

A. State True or False :

- | | | | |
|----------|---------|---------|----------|
| 1. True | 2. True | 3. True | 4. False |
| 5. False | | | |

- | | | | |
|----------|--------|----------------------|--------|
| B. 1. No | 2. 7 | 3. 2 | 4. 0.4 |
| 5. 6/7 | 6. -50 | 7. $4 \times 6 = 24$ | |

Multiple Choice Questions

- | | | | |
|--------|---------|--------|--------|
| 1. (a) | 2. (c) | 3. (b) | 4. (b) |
| 5. (a) | 6. (a) | 7. (c) | 8. (b) |
| 9. (b) | 10. (b) | | |

Exercise 5A

1. Which of the following expressions are polynomials?

Polynomials : An algebraic expression in which the variables involved have only non-negative integral powers is called a **polynomial**.

(a) So, for $5x^2 + 10x - 4 = \text{Yes}$

(b) $3x^{1/2} - 5x + 1 = \text{No}$

(c) $\frac{2}{3}x^3 + 7x^2 - 16 = \text{Yes}$

(d) $6x^3 - 3x^2 + 6\sqrt{x} + 2 = \text{No}$

(e) $7x^2y^2 + 3xy^2 + 5x^2y - 7x = \text{Yes}$

(f) $4x^2y^{1/2} - 3xy + 3x^{3/2}y = \text{No}$

2. (a) $4y - 5 + \frac{1}{2}y^2$

Degree is highest power of the variables, so degree = 2

(b) $5x^4 - 7x^2 + \frac{5}{9}$ Degree = 4

(c) $5x^3 - 2x^2y^2 + x^2 + 9y^2$; Degree = 4

(d) $5x^2y^3 - 3xy^2 + 6 - \sqrt{2}x^4$; Degree = 5

(e) $5x^5 - 7x^5y + 4xy^4 + 7y^8$

Sum of powers of first term = 5

Sum of powers of second term = $5 + 1 = 6$

Sum of powers of third term = 4

Sum of powers of fourth term = 8

So, degree of the polynomial = 8

3. (a) $5x^3 + 7x^4 - 8x + 3x^2 - 3$

In ascending order it is written as

$$-3 - 8x + 3x^2 + 5x^3 + 7x^4$$

(b) $6 + x^2 - 18x + 36x^3$

In ascending order,

$$6 - 18x + x^2 + 36x^3$$

(c) $\frac{1}{6}x^4 - x^5 + 2x - 5x^3 - 2$

In ascending order $-2 + 2x - 5x^3 + \frac{1}{6}x^4 - x^5$

4. (a) $-15x^8 + 3x^4y + 5xy^6 + 2x^3y^3$

In descending order,

$$-15x^8 + 5xy^6 + 2x^3y^3 + 3x^4y$$

(b) $-2x + 3 + 5x^2 - 3x^4 - x^5$

In descending order

$$-x^5 - 3x^4 + 5x^2 - 2x + 3$$

(c) $5xy^2 - 2x^3y - 15x^2 + 3x^4y$

In descending order,

$$3x^4y - 2x^3y + 5xy^2 - 15x^2$$

5. Add the following polynomials :

(a) $7a - 3b + 5c$

$$2a - 3b - 4c$$

$$+ 4a + b + c$$

$$\hline 13a - 5b + 2c$$

(b) $-7x^2 - 3xy + 10y^2$

$$2x^2 + 8xy - 11y^2$$

$$-3x^2 + 6xy + 8y^2$$

$$\hline -8x^2 + 11xy + 7y^2$$

(c) $3x^2 - 3xy + 5y^2$

$$7x^2 + 4xy - 2y^2$$

$$5x^2 \quad + 1y^2$$

$$\hline 15x^2 + 1xy + 4y^2$$

(d) $5x^2 - 7xy + 4y^2 - 3x$

$$4x^2 + 2xy - 1y^2 \quad + 1y$$

$$1x^2 + 5xy - 2y^2 + 3x - 1y$$

$$\hline 10x^2 + \quad + 1y^2$$

6. Subtract

(a) $25x^2 + 16xy - 3b^2 - 2$

$$-6x^2 + 13xy \quad -1 + 4a^2$$

$$+ \quad - \quad + \quad -$$

$$\hline 31x^2 + 3xy - 3b^2 - 1 + 4a^2$$

$$\begin{array}{r}
 \text{(b) } -x^2 + 2xy^2 - 3x^2y + y^3 \\
 \quad x^3 - 1xy^2 + 5x^2y - y^3 \\
 \quad - \quad + \quad - \quad + \\
 \hline
 -2x^3 + 3xy^2 - 8x^2y + 2y^3
 \end{array}$$

$$\begin{array}{r}
 \text{(c) } \frac{4}{3}x^2y + 5x^3 - \frac{2}{3}y^3 + 5xy^2 \\
 \quad 3x^2y + 4x^3 + 5y^3 - \frac{1}{2}xy^2 \\
 \quad - \quad - \quad - \quad + \\
 \hline
 \frac{5}{3}x^2y + 1x^3 - \frac{17}{3}y^3 + \frac{11}{2}xy^2
 \end{array}$$

$$\begin{array}{r}
 \text{(d) } \frac{1}{9}x^3 - \frac{3}{7}x^2 + \frac{2}{5}x + 5 \\
 \quad \frac{-8}{9}x^3 + \frac{4}{-7}x^2 - \frac{3}{5}x + 1 \\
 \quad + \quad - \quad + \quad - \\
 \hline
 x^3 - 1x^2 + 1x + 4
 \end{array}$$

7. $2x^3 - 8x^2 + 9x - 10$

$$\begin{array}{r}
 \mp 7x^3 \quad \pm 8x \mp 9 \\
 \hline
 9x^3 - 8x^2 + 1x - 1
 \end{array}$$

So, $9x^3 - 8x^2 + 1x - 1$ must be added

8. $x^4 - 6x^3 + x^2 - 3x + 1$

$$\begin{array}{r}
 x^5 - 7x^3 + x^2 - 6x + 8 \\
 - \quad + \quad - \quad + \quad - \\
 \hline
 -x^5 + x^4 + x^3 \quad + 3x - 7
 \end{array}$$

9. Multiply :

$$\begin{array}{r}
 \text{(a) } \quad 3x^3 \\
 \quad \times 4x^4 \\
 \hline
 12x^7
 \end{array}
 \qquad
 \begin{array}{r}
 \text{(b) } \quad 4a^2b \\
 \quad \times -6a^3b^2c \\
 \hline
 -24a^5b^4c
 \end{array}
 \qquad
 \begin{array}{r}
 \text{(c) } \quad -6/8x^4yz \\
 \quad \times 24x^2y^2z^3 \\
 \hline
 -18x^6y^3z^4
 \end{array}$$

$$\begin{array}{r}
 \text{(d) } \quad -5/8x^2y^3 \\
 \quad \times -16/15x^3y \\
 \hline
 2/3x^5y^4
 \end{array}$$

$$\begin{array}{r}
 10. \quad (a) \quad \begin{array}{r} 3x^2 - 2x + 5 \\ \times x - 3 \\ \hline -9x^2 + 6x - 15 \\ \hline 3x^3 - 2x^2 + 5x \\ \hline 3x^3 - 11x^2 + 11x - 15 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (b) \quad \begin{array}{r} x^2 + 2x + 1 \\ \times 2x + 3 \\ \hline 3x^2 + 6x + 3 \\ \hline 2x^2 + 4x^2 + 2x \\ \hline 2x^3 + 7x^2 + 8x + 3 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (c) \quad \begin{array}{r} 2x^2 + x - 5 \\ \times x^2 - 2x + 3 \\ \hline 6x^2 + 3x - 15 \\ \hline 4x^3 - 2x^2 + 10x \\ \hline 2x^4 + 1x^3 - 5x^2 \\ \hline 2x^4 + 5x^3 - 1x^2 + 13x - 15 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (d) \quad \begin{array}{r} 3x^2 - 5x + 6 \\ \times 3 - 5x^2 \\ \hline -15x^4 + 25x^3 - 30x^2 \\ \hline + 9x^2 - 15x + 18 \\ \hline -15x^4 + 25x^3 - 21x^2 - 15x + 18 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (e) \quad \begin{array}{r} 3x^5 - 7x^3 + 2x^2 - x + 4 \\ \times x^3 - 2x^2 + 3x - 1 \\ \hline -3x^5 + 7x^3 - 2x^2 + x - 4 \\ \hline 9x^6 + 6x^3 - 3x^2 + 12x - 21x^4 \\ \hline -6x^7 + 14x^5 - 2x^3 - 8x^2 - x^4 \\ \hline 8x^8 - 7x^6 + 2x^5 + 4x - 4x^4 \\ \hline 3x^8 - 6x^7 + 2x^6 + 13x^5 + 15x^3 - 13x^2 + 13x - 4 - 26x^4 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (f) \quad \begin{array}{r} 5x^2 - 7x + 2 \\ \times 2x^2 - 3x - 5 \\ \hline -25x^2 + 35x - 10 \\ \hline -15x^3 + 21x^2 - 6x \\ \hline 10x^4 - 14x^3 + 4x^2 \\ \hline 10x^4 - 29x^3 + 29x - 10 \end{array}
 \end{array}$$

$$\begin{array}{r}
 (g) \quad \begin{array}{r} (5x - 7) \\ \times (2x + 3) \\ \hline 15x - 21 \\ \hline 10x^2 - 14x \\ \hline 10x^2 + 1x - 21 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{r} (10x^2 + x - 21) \\ \times (7x - 8) \\ \hline -80x^2 - 8x + 168 \\ \hline 70x^3 + 7x^2 - 147x \\ \hline 70x^3 - 73x^2 - 155x + 168 \end{array}
 \end{array}$$

Exercise 5B

1. Divide

(a) $x^7 \div x^3 = x^{7-3} = x^4$

(b) $-56abc \div 7b = -8ac$

(c) $\frac{36xy^2z}{-4xy} = -9yz$

(d) $-75x^2y^5z \div 15xy^2z = 5x^{2-1}y^{5-2}z^{1-1}$
 $= 5xy^3z^0 = 5xy^3$

(e) $\frac{-63x^2y^3z^4}{9x^4y^2z^7} = -7x^{2-4}y^{3-2}z^{4-7}$
 $= -7x^{-2}yz^{-3}$
 $= \frac{-7y}{x^2z^3}$

2. (a)

$$\begin{array}{r} -4x^2 \overline{) 8x^4 - 32x^3 + 16x^2} \\ \underline{-8x^4} \\ -32x^3 \\ \underline{\pm 32x^3} \\ 16x^2 \\ \underline{-16x^2} \\ \times \end{array}$$

Ans. : $-2x^2 + 8x - 4$

(b) $(8a^2b^2 - 6ab^2 + 10a^2b^3)$ by $2ab$

First in descending order of its degree first, we will write the polynomial as $10a^2b^3 + 8a^2b^2 - 6ab^2$

$$\begin{array}{r} 5ab^2 + 4ab - 3b \\ 2ab \overline{) 10a^2b^3 + 8a^2b^2 - 6ab^2} \\ \underline{-10a^2b^3} \\ 8a^2b^2 \\ \underline{-8a^2b^2} \\ -6ab^2 \\ \underline{-6ab^2} \\ + \\ \times \end{array}$$

Ans. : $5ab^2 + 4ab - 3b$

$$\begin{array}{r}
 \text{(c)} \quad \frac{-8x^2 - 16x + 2}{-\frac{1}{2}x} \sqrt{\frac{4x^2 + 8x^2 - x}{-4x^2}} \\
 \hline
 8x^2 \\
 -8x^2 \\
 \hline
 -x \\
 +x \\
 \hline
 x
 \end{array}$$

Ans. : $-8x^2 - 16x + 2$

$$\begin{array}{r}
 \text{(d)} \quad \frac{2x^3 + 6x^2 - 1}{3x^2} \sqrt{\frac{6x^5 + 18x^4 - 3x^2}{-6x^5}} \\
 \hline
 18x^4 \\
 -18x^4 \\
 \hline
 -3x^2 \\
 +3x^2 \\
 \hline
 x
 \end{array}$$

Ans. : $2x^3 + 6x^2 - 1$

$$\begin{array}{r}
 \text{(e)} \quad \frac{10x^3 + 6xy - 5}{2xy} \sqrt{\frac{20x^3y + 12x^2y^2 - 10xy}{-20x^3y}} \\
 \hline
 12x^2y^2 \\
 -12x^2y^2 \\
 \hline
 -10xy \\
 +10xy \\
 \hline
 x
 \end{array}$$

Ans. : $10x^2 + 6xy - 5$

$$\begin{array}{r}
 \text{(f)} \quad \frac{-18ab + 9c - 27d}{-\frac{1}{3}ab} \sqrt{\frac{6a^2b^2 - 3abc + 9abd}{-6a^2b^2}} \\
 \hline
 -3abc \\
 +3abc \\
 \hline
 9abd \\
 9abd \\
 \hline
 x
 \end{array}$$

Ans. : $-18ab + 9c - 27d$

$$\begin{array}{r}
 \text{(e)} \quad 5y^2+3 \overline{) 10y^4+5y^3+y^2+4y-2} \\
 \underline{-10y^4 \quad \quad -6y^2} \\
 \quad \quad \quad +5y^3 - 5y^2 + 4y - 2 \\
 \quad \quad \quad \underline{+5y^3 + 0 \quad +3y} \\
 \quad \quad \quad \quad \quad -5y^2 + y - 2 \\
 \quad \quad \quad \quad \quad \underline{-5y \quad \quad +3} \\
 \quad \quad \quad \quad \quad \quad \quad y + 1
 \end{array}$$

Ans.: Q = $2y^2+y-1$
R = $y + 1$

$$\begin{array}{r}
 \text{(f)} \quad x^2+2-3x \overline{) x^4-x^3-3x^2+x+2} \\
 \underline{-x^4 \quad +3x^3 \quad -2x^2} \\
 \quad \quad \quad 2x^3 - 5x^2 + x + 2 \\
 \quad \quad \quad \underline{2x^3 \quad - 6x^2 + 4x} \\
 \quad \quad \quad \quad \quad x^2 - 3x + 2 \\
 \quad \quad \quad \quad \quad \underline{x^2 \quad - 3x + 2} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \times
 \end{array}$$

Ans. : x^2+2x+1

$$\begin{array}{r}
 \text{(g)} \quad 2x^2-6 \overline{) 6x^5-28x^3+3x^2+30x-9} \\
 \underline{-6x^5 \quad +18x^3} \\
 \quad \quad \quad -10x^3+3x^2+30x-9 \\
 \quad \quad \quad \underline{-10x^3 \quad \quad +30x} \\
 \quad \quad \quad \quad \quad 3x^2-9 \\
 \quad \quad \quad \quad \quad \underline{3x^2-9} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \times
 \end{array}$$

Ans. : $3x^3-5x + \frac{3}{2}$

$$\begin{array}{r}
 \text{(h)} \quad a^2-12a+13 \overline{) a^3-14a^2+37a-26} \\
 \underline{-a^3 \quad +12a^2 \quad -13a} \\
 \quad \quad \quad -2a^2+24a-26 \\
 \quad \quad \quad \underline{-2a^2+24a-26} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \times
 \end{array}$$

Ans. : $a - 2$

$$\begin{array}{r}
 \text{(i)} \quad \frac{3x^3+2x^2-9x-\frac{1}{2}}{2x^2-3} \sqrt{\frac{6x^5+4x^4-27x^3-7x^2+27x+\frac{3}{2}}{6x^5 \quad \mp 9x^3}} \\
 \hline
 \quad \quad \quad 4x^4-18x^3-7x^2 \\
 \quad \quad \quad \underline{4x^4 \quad \quad \quad \mp 6x^2} \\
 \quad \quad \quad \quad \quad \quad -18x^3-x^2+27x \\
 \quad \quad \quad \quad \quad \quad \underline{-18x^3 \quad \quad +27x} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad -x^2 + 3/2 \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \underline{-x^2 + 3/2} \\
 \text{Ans. : } 3x^3+2x^2-9x-\frac{1}{2} \quad \quad \quad \frac{\quad \quad \quad \times}{\quad \quad \quad \times}
 \end{array}$$

$$\begin{array}{r}
 \text{(j)} \quad \frac{y^3-4y^2+19y-65}{y^2+4y+2} \sqrt{\frac{y^5+5y^3+3y^2+5y+3}{y^5+2y^3+4y^4}} \\
 \hline
 \quad \quad \quad -4y^4+3y^3+3y^2 \\
 \quad \quad \quad \underline{\mp 4y^4 \quad \mp 16y^3 \quad \mp 8y^2} \\
 \quad \quad \quad \quad \quad \quad 19y^3+11y^2+5y \\
 \quad \quad \quad \quad \quad \quad \underline{19y^3+76y^2+38y} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad -65y^2-33y+3 \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \underline{\mp 65y^2 \quad \mp 260y \quad \mp 130} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad 227y+133
 \end{array}$$

Ans. :
Q = $y^3-4y^2+19y-65$
R = $227y + 133$

$$\begin{array}{r}
 \text{4. (a)} \quad \frac{x^3-x^2+3x-5}{x+5} \sqrt{\frac{x^4+4x^3-2x^2+10x-25}{x^4+5x^3}} \\
 \hline
 \quad \quad \quad -x^3-2x^2 \\
 \quad \quad \quad \underline{\mp x^3 \quad \mp 5x^2} \\
 \quad \quad \quad \quad \quad \quad 3x^2+10x \\
 \quad \quad \quad \quad \quad \quad \underline{3x^2+15x} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad -5x-25 \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \underline{-5x-25} \\
 \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \times \\
 \text{Ans. : } x^3-x^2+3x-5; \text{ Yes}
 \end{array}$$

$$\begin{array}{r}
 \text{(b)} \quad \frac{t^3-1}{t^3+1} \sqrt{\frac{t^6+3t^2+10}{\underline{t^6} + \underline{t^3}}} \\
 \hline
 -t^3+3t^3+10 \\
 \underline{-t^3} \quad \underline{-1} \\
 \hline
 3t^2+11
 \end{array}$$

Ans. : $t^3-1, 3t^2+11$; No

$$\begin{array}{r}
 \text{(c)} \quad \frac{3y^3-5y+3/2}{2y^2-6} \sqrt{\frac{6y^5-28y^3+3y^2+30y-9}{\underline{6y^5}-\underline{18y^3}}} \\
 \hline
 -10y^3+3y^2+30y \\
 \underline{-10y^3+30y} \\
 \hline
 3y^2-9 \\
 \underline{-3y^2-9} \\
 \hline
 \times
 \end{array}$$

Ans. : $3y^2-5y+\frac{3}{2}$, Yes

$$\begin{array}{r}
 5. \quad \frac{x^3+x^2-1}{2x-3} \sqrt{\frac{2x^4-x^3-3x^2-2x+a}{\underline{2x^4}-\underline{3x^3}}} \\
 \hline
 2x^3-3x^2 \\
 \underline{2x^3-3x^2} \\
 \hline
 -2x+a \\
 \underline{-2x+3} \\
 \hline
 a-3
 \end{array}$$

as, $a-3=0$; $a=3$

$$\begin{array}{r}
 6. \quad \begin{array}{r}
 \overline{) x^3+x^2-x+5} \\
 3x+2 \overline{) 3x^4+5x^3-x^2+13x+9} \\
 \underline{3x^4+2x^3} \\
 3x^3-x^2 \\
 \underline{3x^3+2x^2} \\
 -3x^2+13x+9 \\
 \underline{-3x^2-2x} \\
 + \\
 15x+9 \\
 \underline{15x+10} \\
 -1
 \end{array}
 \end{array}$$

$$\begin{aligned}
 \text{Dividend} &= \text{Divisor (Quotient) + Remainder} \\
 &= 3x+2(x^3+x^2+x+5)-1 \\
 &= 3x^4+3x^3-3x^2+15x+2x^2+2x^2-2x+10-1 \\
 &= 3x^4+5x^3-x^2+13x+9
 \end{aligned}$$

(Hence verified)

$$\begin{array}{r}
 7. \quad \begin{array}{r}
 \overline{) 2x^2+2x-1} \\
 4x^2+3x-2 \overline{) 8x^4+14x^3-2x^2+7x-8} \\
 \underline{8x^4+6x^3-4x^2} \\
 8x^3+2x^2+7x \\
 \underline{8x^3+6x^2-4x} \\
 -4x^2+11x-8 \\
 \underline{-4x^2-3x+2} \\
 + \\
 14x-10
 \end{array}
 \end{array}$$

So, $14x - 10$ should be subtracted.

Exercise 5C

1. (a) $(3x+5)^2$
 $(3x)^2 + (5)^2 + 2 \times 3x \times 5$
 $9x^2 + 25 + 30x$
- (b) $(y-9)^2$
 $(y)^2 + (9)^2 - 2y \times 9$
 $y^2 + 81 - 18y$
- (c) $(5x^2 - 4y^2)^2$
 $(5x^2)^2 + (4y^2)^2 - 2(5x^2)(4y^2)$
 $25x^4 + 16y^4 - 40x^2y^2$
- (d) $(7x - \frac{1}{2}y)^2$
 $(7x)^2 + (\frac{1}{2}y)^2 - 2 \times \frac{1}{2}y \times 7x$
 $49x^2 + \frac{1}{4}y^2 - 7xy$
- (e) $(2x + \frac{3}{2}x)^2$
 $(2x)^2 + \left(\frac{3}{x}\right)^2 + 2 \times 2x \times \frac{3}{x}$
 $4x^2 + \frac{9}{x^2} + 12$
- (f) $(5ab - 6cd)^2$
 $(5ab)^2 + (6cd)^2 - 2(5ab)(6cd)$
 $25a^2b^2 + 36c^2d^2 - 60abcd$
- (g) $\left(\frac{3x}{4} - \frac{4y}{5}\right)^2 \Rightarrow \left(\frac{3x}{4}\right)^2 + \left(\frac{4y}{5}\right)^2 - 2\left(\frac{3x}{4}\right)\left(\frac{4y}{5}\right)$
 $\Rightarrow \frac{9x^2}{16} + \frac{16y^2}{25} - \frac{6xy}{5}$
2. (a) $81a^2 + 9b^2 - 54ab$
 $\Rightarrow (9a)^2 + (3b)^2 - 2 \times 9a \times 3b$
 $\Rightarrow (9a - 3b)^2$; putting values

$$\Rightarrow [9 \times (-1) - 3(-4)]^2$$

$$\Rightarrow [-9 + 12]^2$$

$$\Rightarrow (+3)^2 = 9$$

(b) $36x^2 + 49y^2 + 84xy$

$$(6x)^2 + (7y)^2 + 2 \times 6x \times 7y$$

$$(6x+7y)^2 = [6 \times 3 + 7 \times 6]^2$$

$$= [18 + 42]^2$$

$$= [60]^2$$

$$= 360$$

(c) $25x^2 + 16y^2 - 40xy$

$$(5x)^2 + (4y)^2 - 2 \times 5x \times 4y$$

$$(5x-4y)^2$$

$$(5 \times 6 - 4 \times 7)^2$$

$$(30 - 28)^2$$

$$= 4$$

(d) $4x^2 + \frac{9}{x^2} - 12$

$$(4)x^2 + \left(\frac{3}{x}\right)^2 - 2 \times 2x \times \frac{3}{x}$$

$$\left(2x - \frac{3}{x}\right)^2$$

$$\left(2 \times 2 - \frac{3}{2}\right)^2$$

$$\left(4 - \frac{3}{2}\right)^2$$

$$\left(\frac{5}{2}\right)^2$$

$$= \frac{25}{4}$$

3. $x - \frac{1}{x} = 5$ Squaring both sides

$$x^2 + \left(\frac{1}{x}\right)^2 - 2 \times x \times \frac{1}{x} = 25$$

$$x^2 + \frac{1}{x^2} = 27$$

Squaring both side

4. $x^4 + \frac{1}{x^4} + 2 = 729$

(Adding & subtracting 2)

$$x^4 + \frac{1}{x^4} = 727$$

$$x^2 + \frac{1}{x^2} = 23$$

$$x^2 + \frac{1}{x^2} + 2 - 2 = 23$$

5. $\left(x + \frac{1}{x}\right)^2 = 25$ equation (i)

$$x + \frac{1}{x} = 5$$

(Add & Subtract 2) =

$$x^2 + \frac{1}{x^2} = 38 \quad = 36 \quad x^2 + \frac{1}{x^2} + 2 - 2 = 38$$

$$\left(x - \frac{1}{x}\right)^2 = 6$$

squaring eq. (i) $x - \frac{1}{x}$

$$= 1444$$

$$x^4 + \frac{1}{x^4} + 2 = 1442$$

$$x^4 + \frac{1}{x^4}$$

6. (a) $(103)^2 \Rightarrow (100 + 3)^2 \Rightarrow (100)^2 + (3)^2 + 2(100)(3) = 10609$
 (b) $(98)^2 \Rightarrow (100 - 2)^2 \Rightarrow (100)^2 + (2)^2 - 2(100)(2) = 9604$
 (c) $(10.3)^2 \Rightarrow (10 + 0.3)^2 \Rightarrow (10)^2 + (0.3)^2 - 2(10)(0.3) = 106.09$
 (d) $(99.5)^2 \Rightarrow (100 - 0.5)^2 \Rightarrow (100)^2 + (0.5)^2 - 2(100)(0.5) = 9900.25$
7. (a) $176 \times 176 - 124 \times 124 \Rightarrow (176)^2 - (124)^2 \Rightarrow (176 + 124)(176 - 124)$
 $\Rightarrow 15600$
 (b) $0.68 \times 0.68 - 0.32 \times 0.32 \Rightarrow (0.68)^2 - (0.32)^2$
 $(0.68 + 0.32)(0.68 - 0.32) \Rightarrow 0.36$
 (c) $1.06 \times 1.06 - 2 \times 1.06 \times 0.06 + 0.06 \times 0.06 \Rightarrow (1.06 - 0.06)^2 \Rightarrow 1$
 (d) $\frac{23.71 \times 23.74 - 16.29 \times 16.29}{0.742} = \frac{(23.71)^2 - (16.29)^2}{0.742}$
 $\frac{(23.71 + 16.29)(23.71 - 16.29)}{0.742} = 400$
8. (a) $(3x + 2y + 4z)^2 \Rightarrow (3x)^2 + (2y)^2 + (4z)^2 + 2(3x)(2y) + 2(2y)(4z) + 2(4z)(3x) \Rightarrow 9x^2 + 4y^2 + 16z^2 + 12xy + 16yz + 24xz$
 (b) $(2x - y + 3z)^2 \Rightarrow (2x)^2 + (y)^2 + (3z)^2 - 2(2x)(y) - 2(y)(3z) + 2(3z)(2x) \Rightarrow 4x^2 + y^2 + 9z^2 - 4xy - 6yz + 12xz$
 (c) $(x - 2y - 5z)^2 \Rightarrow (x)^2 + (2y)^2 + (5z)^2 - 2(x)(2y) + 2(2y)(5z) - 2(5z)(x) \Rightarrow x^2 + 4y^2 + 25z^2 - 4xy + 20yz - 10xz$
 (d) $(5 + 4a - 8b)^2 \Rightarrow (5)^2 + (4a)^2 + (8b)^2 + 2(5)(4a) - 2(4a)(8b) - 2(8b)(5) \Rightarrow 25 + 16a^2 + 64b^2 + 40a - 64ab - 80b$
 (e) $(x^2 + y^2 + z^2)^2 \Rightarrow (x^2)^2 + (y^2)^2 + (z^2)^2 + 2(x^2)(y^2) + 2(y^2)(z^2) + 2(z^2)(x^2) \Rightarrow x^4 + y^4 + z^4 + 2x^2y^2 + 2y^2z^2 + 2z^2x^2$
 (f) $(xy + yz + zx)^2 \Rightarrow (xy)^2 + (yz)^2 + (zx)^2 + 2(xy)(yz) + 2(yz)(zx) + 2(zx)(xy) \Rightarrow x^2y^2 + y^2z^2 + z^2x^2 + 2xy^2z^2 + 2yz^2x + 2zx^2y$

9. $(4)^2 + 4(5)^2 + 9(3)^2 + 4(4 \times 5) + 12(5 \times 3) + 2(3 \times 4)$ or
 $(x + 2y + 3z)^2$ or $(4 + 10 + 3 \times 3)^2 = 529$
10. $4x^2 + (y)^2 + 25z^2 + 4xy - 10yz - 20xz$
 $(2x + y - 5z)^2$
 $(2 \times 4 + 3 - 5 \times 2)^2$
 $(8 + 3 - 10)^2 = (1)^2 = 1$
11. $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$
 $x^2 + y^2 + z^2 + 2(xy + yz + zx)$
 as $(x + y + z) = 9$
 $xy + yz + zx = 23$

Substituting values

- $$(9)^2 = x^2 + y^2 + z^2 + 2(23)$$
- $$x^2 + y^2 + z^2 = 81 - 46 = 35$$
12. $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$
 $x^2 + y^2 + z^2 + 2(xy + yz + zx)$
 as $(x + y + z) = 15$
 $(x^2 + y^2 + z^2) = 77$
 $(15)^2 = 77 + 2(xy + yz + zx)$
 $\frac{225 - 77}{2} = xy + yz + zx$
 $xy + yz + zx = 74$

Exercise 5D

1. (a) $(5x + 9y)^3 = (5x)^3 + (9y)^3 + 3(5x)(9y)(5x + 9y)$
 $125x^3 + 729y^3 + 675x^2y + 1215xy^2$
- (b) $(3p - 2q)^3 = (3p)^3 - (2q)^3 - 3(3p)(2q)(3p - 2q)$
 $27p^3 - 8q^3 - 54p^2q^2 + 36pq^2$
- (c) $(x + 1)^3 = (x)^3 + (1)^3 + 3(x)(1)(x + 1)$
 $x^3 + 1 + 3x^2 + 3x$
- (d) $(x - 1)^3 = (x)^3 - (1)^3 - 3(x)(1)(x - 1)$
 $x^3 - 1 - 3x^2 + 3x$

$$(e) \left(\frac{2}{3}a + \frac{5}{3}b\right)^2 = \left(\frac{2}{3}a\right)^2 + \left(\frac{5}{3}b\right)^2 + 3\left(\frac{2}{3}a\right)\left(\frac{5}{3}b\right)$$

$$\left(\frac{2}{3}a + \frac{5}{3}b\right)$$

$$\frac{8}{27}a^3 + \frac{125}{27}b^3 + \frac{20a^2b}{9} + \frac{50ab^2}{9}$$

$$(f) \left(2x + \frac{3}{x}\right)^3 \Rightarrow (2x)^3 + \left(\frac{3}{x}\right)^3 + 3(2x)\left(\frac{3}{x}\right)\left(2x + \frac{3}{x}\right)$$

$$8x^3 + \frac{27}{x^3} + 36x + \frac{54}{x}$$

$$(g) \left(2x + \frac{1}{4y}\right)^3 \Rightarrow (2x)^3 + \left(\frac{1}{4y}\right)^3 + 3(2x)\left(\frac{1}{4y}\right)\left(2x + \frac{1}{4y}\right)$$

$$8x^3 + \frac{1}{64y^3} + \frac{3x^2}{y} + \frac{3x}{8y^2}$$

2. (a) $a^3 + 8b^3$, $ab = 15$, $(a + 2b) = 10$

$(a + 2b) = 10$, cubing both sides

$$(a + 2b)^3 = 1000$$

$$a^3 + 8b^3 + 6ab(a + 2b) = 1000$$

$$a^3 + 8b^3 + 6 \times 15(10) = 1000$$

$$a^3 + 8b^3 = 1000 - 900 = 100$$

(b) $a^3 - b^3$ if $a - b = -8$, $ab = -12$

$$a - b = -8, \text{ or } (a - b)^3 = (-8)^3$$

$$a^3 - b^3 - 3ab(a - b) = -512$$

$$a^3 - b^3 - 3 \times -12(-8) = -512$$

$$a^3 - b^3 = -512 + 288$$

$$a^3 - b^3 = -224$$

(c) $x^3 - y^3$, if $x - y = \frac{10}{9}$ and $xy = \frac{5}{3}$

$$x - y = \frac{10}{9}$$

$$x^3 - y^3 - 3 \times \frac{5}{3} \left(\frac{10}{9} \right) = \frac{1000}{729}$$

$$x^3 - y^3 = \frac{1000}{729} + \frac{50}{9} = \frac{5050}{729}$$

(d) $64a^3 - 125b^3$; $4a - 5b = 16$; $ab = 12$; $4a - 5b = 16$

$$(4a)^3 - (5b)^3 - 3 \times 4a \times 5b(4a - 5b) = 4096$$

$$64a^3 - 125b^3 - 60 \times 12 \times 16 = 4096$$

$$64a^3 - 125b^3 = 4096 + 11520 = 15616$$

(e) $27x^3 - 8y^3$; if $3x - 2y = 5$; $xy = 1$

$$(3x)^3 - (2y)^3 - 3(3x)(2y)(3x - 2y) = 125$$

$$27x^3 - 8y^3 - 18 \times 1(5) = 125$$

$$27x^3 - 8y^3 = 125 + 18 \times 5$$

$$27x^3 - 8y^3 = 215$$

(f) $a^3 - \frac{1}{a^3}$; as $a - \frac{1}{a} = 5$

$$a^3 - \frac{1}{a^3} - 3a \times \frac{1}{a} \left(a - \frac{1}{a} \right) = (5)^3 = a^3 - \frac{1}{a^3} = 125 + 15 = 140$$

(g) $a^3 + \frac{1}{a^3}$; if $a + \frac{1}{a} = 4$

$$a^3 + \frac{1}{a^3} + 3a \times \frac{1}{a} \left(a + \frac{1}{a} \right) = (4)^3 = a^3 + \frac{1}{a^3} = 64 - 12 = 52$$

(h) $a^3 + \frac{1}{a^3}$; if $a + \frac{1}{a} = 6$

$$a^3 + \frac{1}{a^3} + 3a \times \frac{1}{a} \left(a + \frac{1}{a} \right) = 216$$

$$\Rightarrow a^3 + \frac{1}{a^3} = 216 - 18 = 198$$

- (i) $8a^3 - 27b^3 - 18ab(2a - 3b)$ where $a = 8, b = 5$
 or $(2a - 3b)^3 = ? \implies (2 \times 8 - 3 \times 5)^3$
 $(16 - 15)^3 = (1)^3 = 1$
3. (a) $(1001)^3 = (1000 + 1)^3 = (1000)^3 + (1)^3 + 3(1000)(1000 + 1) = 1003003001$
- (b) $(97)^3 = (100 - 3)^3 = (100)^3 - (3)^3 - 3(100)(3)(100 - 3) = 912673$
- (c) $(598)^3 = (600 - 2)^3 = (600)^3 - (2)^3 - 3(600)(2)(600 - 2) = 213847192$
- (d) $(9.9)^2 = (10 - 0.1)^2 = (10)^2 - (0.1)^2 - 3(10)(0.1)(10 - 0.1) = 970.299$
- (e) $(10.2)^3 = (10 + .02)^3 = (10)^3 + (0.2)^3 + 3(10)(0.2)(10 + 0.2) = 1061.208$
4. (a) $(2x + 5)^3 - (2x - 5)^3$
 $[(2x)^3 + (573 + 3 \times 2x \times 5(2x + 5))] - [(2x)^3 - (5)^3 - 3(2x)(2x - 5)]$
 $120x^2 + 250$
- (b) $(3x)^3 + (8y)^3 + 3 \times 3x \times 8y(3x + 8y) - [(3x)^3 - (8y)^3 - 3 \times 3x \times 8y(3x - 8y)]$
 $27x^3 + 512y^3 + 72xy(3x + 8y) - 27x^3 + 512y^3 + 72xy(3x - 8y)$
 $1024y^3 + 216xy + 576xy^2 + 216xy - 576xy^2$
 $1024y^3 + 432xy$
- (c) $\left(\frac{x}{2} + \frac{y}{3}\right)^3 - \left(\frac{x}{2} - \frac{y}{3}\right)^3$
 $\left(\frac{x}{2}\right)^3 + \left(\frac{y}{3}\right)^3 + 3\left(\frac{x}{2}\right)\left(\frac{y}{3}\right)\left(\frac{x}{2} + \frac{y}{3}\right) -$
 $\left[\left(\frac{x}{2}\right)^3 - \left(\frac{y}{3}\right)^3 - 3\left(\frac{x}{2}\right)\left(\frac{y}{3}\right)\left(\frac{x}{2} - \frac{y}{3}\right)\right]$

$$\begin{aligned} & \left(\frac{x}{2}\right)^3 + \left(\frac{y}{3}\right)^3 + 3\left(\frac{x}{2}\right)^2\left(\frac{y}{3}\right) + 3\left(\frac{x}{2}\right)\left(\frac{y}{3}\right)^2 - \\ & \left(\frac{x}{2}\right)^3 - \left(\frac{y}{3}\right)^3 - 3\left(\frac{x}{2}\right)^2\left(\frac{y}{3}\right) + 3\left[\frac{x}{2}\right]\left[\frac{y}{3}\right]^2 = \frac{2y^3}{27} + \frac{x^2y}{2} \end{aligned}$$

$$\begin{aligned} \text{(d)} \quad & \left[\frac{p}{2} - \frac{q}{3}\right]^3 - \left(\frac{p}{2} + \frac{q}{3}\right)^3 \\ & \left[\left(\frac{p}{2}\right)^3 - \left(\frac{q}{3}\right)^3 - 3\left(\frac{p}{2}\right)\left(\frac{q}{3}\right)\left(\frac{p}{2} - \frac{q}{3}\right)\right] \\ & \quad - \left[\left(\frac{p}{2}\right)^3 + \left(\frac{q}{3}\right)^3 + 3\left(\frac{p}{2}\right)\left(\frac{q}{3}\right)\left(\frac{p}{2} + \frac{q}{3}\right)\right] \\ & \left(\frac{p}{2}\right)^3 - \left(\frac{q}{3}\right)^3 - 3\left(\frac{p}{2}\right)^2\left(\frac{q}{3}\right) + 3\left(\frac{p}{2}\right)\left(\frac{q}{3}\right)^2 - \\ & \quad \left[\left(\frac{p}{2}\right)^3 + \left(\frac{q}{3}\right)^3 + 3\left(\frac{p}{2}\right)^2\left(\frac{q}{3}\right)\right] = \frac{-p^2q}{2} \end{aligned}$$

Exercise 5E

1. (a) $(x+5)(x+3)$
 $x^2 + (5+3)x + 5 \times 3$
 $x^2 + 8x + 15$
- (b) $(x-3)(x-5)$
 $x^2 - (5+3)x + 5 \times 3$
 $x^2 - 8x + 15$
- (c) $(x-5)(x-3)$
 $x^2 - (5+3)x + 5 \times 3$
 $x^2 - 8x + 15$
- (d) $(x-2)(x+9)$
 $x^2 + (9-2)x + 9 \times -2$
 $x^2 + 7x - 18$
- (e) $(x+2)(x-9)$
 $x^2 + (-9+2)x - 9 \times 2$
 $x^2 - 7x - 18$
- (f) $(x-5)(x-7)$
 $x^2 - (5+7)x + 5 \times 7$
 $x^2 - 12x + 35$
- (g) $(3x+5)(3x-7)$
 $(3x)^2 - 7 \times 3x + 5 \times 3x - 7 \times 5$
 $9x^2 - 21x + 15x - 35$
 $9x^2 - 6x - 35$

$$(h) (2x-3)(2x-5)$$

$$4x^2 - 6x - 10x + 15$$

$$4x^2 - 16x + 15$$

$$(i) \left(a + \frac{4}{3}\right) + \left(a + \frac{1}{3}\right) \Rightarrow a^2 + \left(\frac{4}{3} + \frac{1}{3}\right)a + \frac{4}{3} \times \frac{1}{3}$$

$$\Rightarrow a^2 + \frac{5}{3}a + \frac{4}{9}$$

$$2. (a) (101 \times 103) = (100 + 1)(100 + 3)$$

$$(100)^2 + (1 + 3)100 + (1 \times 3) = 10403$$

$$(b) 97 \times 102 = (100 - 3)(100 + 2)$$

$$(100)^2 + (2 - 3)100 + (2 \times -3) = 9894$$

$$(c) 96 \times 105 = (100 - 4)(100 + 5)$$

$$(100)^2 + (-4 + 5)100 + (-4 \times 5) = 10080$$

$$(d) 51 \times 53 = (50 + 1)(50 + 3)$$

$$(50)^2 + (3 + 1)50 + (3 \times 1) = 2703$$

$$(e) 51 \times 48 = (50 + 1)(50 - 2)$$

$$(50)^2 + (1 - 2)50 + (1 \times -2) = 2448$$

$$(f) 103 \times 96 = (100 + 3)(100 - 4)$$

$$(100)^2 + (-4 + 3)100 + (-4 \times 3) = 9888$$

$$3. (a) (x - 4)(x^2 + 4x + 16)$$

$$x^3 - (4)^3 = x^3 - 64$$

$$(b) (5 - x)(25 + 5x + x^2)$$

$$(5)^3 - (x)^3 = 125 - x^3$$

$$(c) (2x - 5y)(4x^2 + 10xy + 25y^2)$$

$$(2x)^3 - (5y)^3 = 8x^3 - 125y^3$$

$$(d) (3z - 1)(9z^2 + 3z + 1)$$

$$(3z)^2 - (1)^3 = 27z^3 - 1$$

$$(e) (5x + 2y)(25x^2 - 10xy + 4y^2)$$

$$(5x)^3 + (2y)^3 = 125x^3 + 8y^3$$

$$(f) \left(2 + \frac{5}{x}\right) \left(4 - \frac{10}{x} + \frac{25}{x^2}\right)$$

$$(2)^3 + \left(\frac{5}{x}\right)^3 = 8 + \frac{125}{x^3}$$

$$(g) \left(3x - \frac{y}{2}\right) \left(9x^2 + \frac{3}{2}xy + \frac{1}{4}y^2\right)$$

$$(3x)^3 - \left(\frac{y}{2}\right)^3 = 27x^3 - \frac{y^3}{8}$$

4. (a) $(x+5)(x^2-5x+25) - (x+4)(x^2-4x+16)$

$$(x)^3 + (5)^3 - [(x)^3 - (4)^3]$$

$$+125 - (+64) = 125 - 64 = 61$$

(b) $(x+5)(x-4) + (x-4)(x-3) - (x+3)(x-2)$

$$x^2 + (5-4)x - 20 + x^2 - (4+3)x + 1^2 - x^2 - (3-2)x + 6$$

$$x^2 - 7x - 2$$

6. $a+b+c=9$; $ab+bc+ac=26$

squaring both sides

$$a^2 + b^2 + c^2 + 2(ab+bc+ac) = 81$$

$$a^2 + b^2 + c^2 + 2 \times 26 = 81$$

$$a^2 + b^2 + c^2 = 81 - 52 = 29$$

$$a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ac)$$

$$= 9(29 - 26)$$

$$= 9 \times 3 = 27$$

7. $a+b+c=15$

$$a^2 + b^2 + c^2 + 2(ab+bc+ca) = 225$$

$$83 + 2(ab+bc+ca) = 225$$

$$2(ab+bc+ca) = 225 - 83$$

$$2(ab+bc+ca) = 142$$

$$ab+bc+ca = 71$$

$$a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$(a+b+c)(a^2 + b^2 + c^2) - (ab+bc+ca)$$

$$(15)(83 - 71) = 180$$

8. $a+b+c=0$ and $3abc=27$

$$a^3 + b^3 + c^3 = 3abc$$

$$\therefore a+b+c=0$$

$$a^3 + b^3 + c^3 = 27$$

9. (a) $(28)^3 - (78)^3 + (50)^3 = 3 \times (28) \times (-78) \times (50)$
 $= -327600$

(b) $(55)^3 - (75)^3 + (20)^3 = 3 \times (55) \times (-75) \times (20)$
 $= -247500$

10. (a) $(a + b + c)(a^2 + b^2 + c^2 - ab - bc - ac)$
 $a^2 + b^2 - 3abc + c^3$

(b) $(2x + 3y + 4z)(4x^2 + 9y^2 + 16z^2 - 6xy - 12yz - 8xz)$
 $8x^3 + 27y^3 + 64z^3 - 72xyz$

Check Your Mental Maths IQ

- | | |
|--------------------------------------|----------------|
| 1. Degree of polynomial | 2. Highest |
| 3. 2 | 4. $x - y$ |
| 5. $(x - y)(x + y)(x^2 + y^2)$ | 6. $a^3 - b^3$ |
| $(x^2 - y^2)(x^2 + y^2) = x^4 - y^4$ | |
| 7. $P = 2(\ell + b)$ | |

$$\begin{aligned} \text{Perimeter} &= 2(4p^2 - 2r + 1 + 3p^2 - 2r + 2) \\ &= 2(7p^2 - 4r + 3) = 14p^2 - 8r + 3 \end{aligned}$$

8.
$$\begin{array}{r} 4x-3 \\ 4x-3 \overline{) 16x^2-24x+a} \\ \underline{-16x^2+12x} \\ -12x+a \\ \underline{-12x+9} \\ a-9 \end{array}$$

$$\begin{aligned} \therefore a - 9 &= 0 \\ a &= 9 \end{aligned}$$

Multiple Choice Questions

- | | | | |
|--------|--------|--------|--------|
| 1. (c) | 2. (a) | 3. (a) | 4. (c) |
| 5. (b) | 6. (c) | 7. (a) | 8. (a) |

6

Factorization of Algebraic Expressions

Exercise 6A

1. (a) $2x^2 + 5x$
 $x(2x + 5)$
- (b) $3x^2 - 6xy^2$
 $3x(x - 2y^2)$
- (c) $6x^2 + 8x^2y = 2x^2(3 + 4y)$
- (d) $12x^3y^4 + 16x^2y^5 - 4x^5y^2 = 4x^2y^2(3xy^2 + 4y^3 - x^3)$
- (e) $18a^3b^2 + 36ab^4 - 24a^2b^2 = 6ab^2(3a^2 + 6b^2 - 4ab)$
2. (a) $(7 + 3)(2x + 5) = 10(2x + 5)$
- (b) $(x + 2)y + (x + 2)x = (x + y)(x + 2)$
- (c) $5a(2x + 3y) - 2b(2x + 3y) = (5a - 2b)(2x + 3y)$
- (d) $8(5x + 9y)^2 + 12(5x + 9y) = 4(5x + 9y)[2(5x + 9y) + 3]$
- (e) $9(a - 2b)^2 + 6(2b - a) = 3(a - 2b)[3(a - 2b) + 2(-1)]$
 $= 3(a - 2b)[3(a - 2b) - 2]$
- (f) $(x - 2y)^2 - 4x + 8y = (x - 2y)\{(x - 2y) - 4\}$
- (g) $2a + 6b - 3(a + 3b)^2 = a + 3b\{2 - 3(a + 3b)\}$
3. (a) $(x + y)(2x + 3y) - (x + y)(x + 1)$
 $x + y(2x + 3y - x - 1)$
 $x + y(x + 3y - 1)$
- (b) $(x + y)(2a + b) - (3x - 2y)(2a + b)$
 $(2a + b)(x + y - 3x + 2y)$
 $(2a + b)(-2x + 3y)$
- (c) $x^2 + xy + 8x + 8y$
 $x(x + y) + 8(x + y)$
 $(x + y)(x + 8)$
- (d) $15ab + 15 + 9b + 25a$
 $15ab + 25a + 9b + 15$
 $5a(3b + 5) + 3(3b + 5)$
 $(5a + 3)(3b + 5)$

$$\begin{aligned} \text{(e)} \quad & ax^2 + by^2 + bx^2 + ay^2 \\ & ax^2 + bx^2 + by^2 + ay^2 \\ & x^2(a+b) + y^2(a+b) \\ & (x^2 + y^2)(a+b) \end{aligned}$$

$$\begin{aligned} \text{(f)} \quad & 3ax - 6ay - 8by + 4bx \\ & 3ax + 4bx - 6ay - 8by \\ & x(3a + 4b) - 2y(3a + 4b) \\ & (x - 2y)(3a + 4b) \end{aligned}$$

$$4. \quad \text{(a)} \quad 9a^2 - 16b^2 = (3a)^2 - (4b)^2 = (3a + 4b)(3a - 4b)$$

$$\text{(b)} \quad 36a^2 - (x - y)^2 = (6a)^2 - (x - y)^2 = (6a + x - y)(6a - x + y)$$

$$\text{(c)} \quad 80a^2 - 45b^2 = 5[16a^2 - 9b^2] = [(4a)^2 - (3b)^2] = 5(4a + 3b)(4a - 3b)$$

$$\text{(d)} \quad (3a - b)^2 - 9c^2 = (3a - b)^2 - (3c)^2 = (3a - b + 3c)(3a - b - 3c)$$

$$\text{(e)} \quad 16x^2 - 81 = (4x)^2 - (9)^2 = (4x - 9)(4x + 9)$$

$$\text{(f)} \quad 3a^4 - 48b^4 = 3[(a^2)^2 - (4b^2)^2] = 3[(a^2 + 4b^2)(a^2 - 4b^2)] = 3(a + 2b)(a - 2b)(a^2 + 4b^2)$$

$$\text{(g)} \quad 16a^2b - \frac{b}{16a^2} = b \left(16a^2 - \frac{1}{16a^2} \right)$$

$$b \left(4a + \frac{1}{4a} \right) \left(4a - \frac{1}{4a} \right)$$

$$\begin{aligned} \text{(h)} \quad & 100(x + y)^2 - 81(a + b)^2 \\ & \{10(x + y) + 9(a + b)\} \{10(x + y) - 9(a + b)\} \end{aligned}$$

$$5. \quad \text{(a)} \quad x^2 + 8x + 16$$

$$\text{(b)} \quad 4a^2 - 4a + 1$$

$$x^2 + 4x + 4x + 16$$

$$4a^2 - 2a - 2a + 1$$

$$x(x + 4) + 4(x + 4)$$

$$2a(2a - 1) - 1(2a - 1)$$

$$(x + 4)(x + 4)$$

$$(2a - 1)(2a - 1)$$

$$\text{(c)} \quad 4x^2 + 12xy + 9y^2$$

$$\text{(d)} \quad x^4 - 10x^2y^2 + 25y^4$$

$$4x^2 + 6xy + 6xy + 9y^2$$

$$x^4 - 5x^2y^2 - 5x^2y^2 + 25y^4$$

$$2x(2x + 3y) + 3y(2x + 3y)$$

$$x^2(x^2 - 5y^2) - 5y^2(x^2 - 5y^2)$$

$$(2x + 3y)(2x + 3y)$$

$$(x^2 - 5y^2)(x^2 - 5y^2)$$

$$\text{(e)} \quad a^4 - 2a^2b^2 + b^4$$

$$\text{(f)} \quad \frac{x^2}{64} + \frac{y^2}{9} + \frac{xy}{12}$$

$$\begin{array}{ll}
 a^4 - a^2b^2 - a^2b^2 + b^4 & \frac{x^2}{64} + \frac{xy}{24} + \frac{xy}{24} + \frac{y^2}{9} \\
 a^2(a^2 - b^2) - b^2(a^2 - b^2) & \frac{x}{8} \left(\frac{x}{8} + \frac{y}{3} \right) + \frac{y}{3} + \left(\frac{x}{8} + \frac{y}{3} \right) \\
 (a^2 - b^2)(a^2 - b^2) & \\
 (a+b)(a-b)(a+b)(a-b) & \left(\frac{x}{8} + \frac{y}{3} \right) \left(\frac{x}{8} + \frac{y}{3} \right)
 \end{array}$$

6. (a) $4x^2 + 9y^2 + z^2 + 12xy + 6yz + 4zx$
 $(2x)^2 + (3y)^2 + (z)^2 + 2 \times 2x \times 3y + 2 \times 3y \times z + 2 \times z \times 2x$
 $(2x + 3y + z)^2$
- (b) $x^2 + 4y^2 + z^2 - 4xy + 4yz - 2xz$
 $(-x)^2 + (2y)^2 + (z)^2 + 2 \times -x \times 2y + 2 \times 2y \times z + 2 \times -x \times z$
 $(-x + 2y + z)^2$
- (c) $a^2 + b^2 + c^2 - 2ab + 2bc - 2ca$
 $(-a)^2 + (b)^2 + (c)^2 + 2 \times -a \times b + 2 \times b \times c + 2 \times c \times -a$
 $(-a + b + c)^2$
- (d) $81x^2 + 4y^2 + z^2 + 36xy + 4yz + 18zx$
 $(9x)^2 + (2y)^2 + (z)^2 + 2 \times 9x \times 2y + 2 \times 2y \times z + 2 \times 9x \times z$
 $(9x + 2y + z)^2$
- (e) $8x^3 + 36x^2y + 54xy^2 + 27y^3$
 $(2x)^3 + (3y)^3 + 3 \times 2x \times 3y(2x + 3y)$
 $(2x + 3y)^3$
- (f) $8x^3 - 125 - 60x^2 + 150x$
 $(2x)^3 - (5)^3 - 3 \times 2x \times 5(2x - 5)$
 $(2x - 5)^3$
- (g) $27a^3 - 64 - 108a^3 + 144a$
 $(3a)^3 - (4)^3 - 3 \times 3a \times 4(3a - 4)$
 $(3a - 4)^2$

Exercise 6B

1. (a) $x^2 + 6x + 8$ (b) $x^2 + 4x - 21$
 $x^2 + 4x + 2x + 8$ $x^2 + 7x - 3x - 27$

- | | |
|--------------------------------|----------------------------------|
| $x(x+4)+2(x+4)$ | $x(x+7)-3(x+7)$ |
| $(x+2)(x+4)$ | $(x-3)(x+7)$ |
| (c) $x^2-7x+12$ | (d) $x^2-23x+132$ |
| $x^2-4x-3x+12$ | $x^2-12x-11x+132$ |
| $x(x-4)-3(x-4)$ | $x(x-12)-11(x-12)$ |
| $(x-3)(x-4)$ | $(x-11)(x-12)$ |
| (e) $x^2-21x+108$ | (f) $x^2+5x-36$ |
| $x^2-12x-9x+108$ | $x^2+9x-4x-36$ |
| $x(x-12)-9(x-12)$ | $x(x+9)-4(x+9)$ |
| $x-9)(x-12)$ | $(x-4)(x+9)$ |
| (g) $-x^2+3x+40$ | (h) $x^2-11x-42$ |
| $-x^2+8x-5x+40$ | $x^2-14x+3x-42$ |
| $-x(x-8)-5(x-8)$ | $x(x-14)+3(x-14)$ |
| $(-x-5)(x-8)$ | $(x+3)(x-14)$ |
| (i) $a^2+19a-150$ | |
| $a^2+25a-6a-150$ | |
| $a(a+25)-6(a+25)$ | |
| $(a-6)(a+25)$ | |
| 2. (a) $2x^2+5x+3$ | (b) $6x^2+5x-6$ |
| as $2 \times 3 = 6, [2, 3]$ | as $6 \times -6 = -36, [-4, 9]$ |
| $2x^2+2x+3x+3$ | $6x^2+9x-4x-6$ |
| $2x(x+1)+3(x+1)$ | $3x(2x+3)-2(2x+3)$ |
| $(2x+3)(x+1)$ | $(3x-2)(2x+3)$ |
| (c) $6x^2-13x+6$ | (d) $-2x^2-3+2$ |
| as $6 \times 6 = 36, [-9, -4]$ | as $2 \times -2 = -4, [-4, 1]$ |
| $6x^2-9x-4x+6$ | $-2x^2-4x+x+2$ |
| $3x(2x-3)-2(2x-3)$ | $-2x(x+2)+1(x+2)$ |
| $(3x-2)(2x-3)$ | $(1-2x)(x+2)$ |
| (e) $12x^2-23xy+10y^2$ | (f) $6x^2+35xy-6y^2$ |
| $12 \times 10 = 120, [8, 15]$ | as $6 \times -6 = -36, [36, -1]$ |
| $12x^2-15xy-8x+10y^2$ | $6x^2+36xy-xy-6y^2$ |
| $3x(4x-5y)-2(4x-5y)$ | $6x(x+6y)-y(x+6y)$ |

$$\begin{array}{ll}
 (3x-2)(4x-5y) & (6x-y)(x+6y) \\
 \text{(g) } 3x^2-4x-4 & \text{(h) } 11x^2-54x+63 \\
 4 \times 3 = 12, [6, 2] & 63 \times 11 = 693, [21, 33] \\
 3x^2-6x+2x-4 & 11x^2-33x-21x+63 \\
 3x(x-2)+2(x-2) & 11x(x-3)-21(x-3) \\
 (3x+2)(x-2) & (11x-21)(x-3) \\
 \text{(i) } 9x^2-22xy+8y^2 \text{ (product} = 9 \times 8 = 72, [18, 4]) & \\
 9x^2-18xy-4xy+8y^2 & \\
 9x(x-2y)-2y(x-2y) & \\
 (9x-2y)(x-2y) &
 \end{array}$$

Exercise 6C

$$\begin{array}{ll}
 1. \text{ (a) } 8x^3+125 & \text{(b) } y^3+512 \\
 (2x)^3+(5)^3 & (y)^3+(8)^3 \\
 (2x+5)(4x^2-10x+25) & (y+8)(y^2-8y+64) \\
 \text{(c) } 125a^3+34^3b^3 & \\
 (5a)^3+(7b)^3 & \\
 (5a+7b)(25a^2-35ab+49b^2) & \\
 \text{(d) } x^6+y^6 & \\
 (x^2)^3+(y^2)^3 & \\
 (x^2+y^2)(x^4-x^2y^2+y^4) & \\
 \text{(e) } 128x^3+54y^3 & \\
 2(64x^3+27y^3) & \\
 2(4x)^3+(3y)^3 & \\
 2(4x+3y)(16x^2-12xy+9y^2) & \\
 \text{(f) } 54a^6b+2a^3b^4 & \\
 2a^3b(27a^3+b^3) & \\
 2a^3b\{(3a)^3+(b)^3\} & \\
 2a^3b(3a+b)(9a^2-3ab+b^2) & \\
 \text{(g) } 1+27x^3 & \text{(h) } 64x^3+y^3 \\
 (1)^3+(3x)^3 & (4x)^3+(y)^3 \\
 (1+3x)(1+9x^2-9x) & (4x+y)(16x^2+y^2-4xy)
 \end{array}$$

2. (a) $8x^3 - 343$
 $(2x)^3 - (7)^3$
 $(2x - 7)(4x^2 + 49 + 14x)$
- (b) $64x^3 - y^3$
 $(4x)^3 - (y)^3$
 $(4x + y)(16x^2 + y^2 - 4xy)$
- (c) $1 - 27x^3$
 $(1)^3 - (3x)^3$
 $(1 - 3x)(1 + 9x^2 + 9x)$
- (d) $2x^4 - 128x$
 $2x\{(x)^3 - (64)\}$
 $2x\{x^3 - (4)^3\}$
 $2x(x - 4)(x^2 + 16 + 4x)$
- (e) $x - 8xy^3$
 $x(1 - 8y^3)$
 $x\{(1)^3 - (2y)^3\}$
 $x(1 - 2y)(1 + 4y^2 + 2y)$
- (g) $\frac{x^3}{64} - 8y^3$
 $\left(\frac{x}{4}\right)^3 - (2y)^3$
 $\left(\frac{x}{4} - 2y\right)\left(\frac{x}{16} + 4y^2 + \frac{x}{2}y\right)$
- (h) $a^4b - ab^4$
 $ab(a^3 - b^3)$
 $ab(a - b)(a^2 + b^2 + ab)$
3. (a) $(3x - 2y)^3 + (2y - 5z)^2 + (5z - 3x)^3$
 $3x - 2y = a, 2y - 5z = b, 5z - 3x = c$
Clearly $a + b + c = 0, a^3 + b^3 + c^3 = 3abc$
 $3(3x - 2y)(2y - 5z)(5z - 3x) = (3x - 2y)^3 + (2y - 5z)^3 + (5z - 3x)^3$
- (b) $p^3(q - r)^3 + q^3(r - p)^3 + r^3(p - q)^3$
 $(pq - pr)^3 + (qr - qp)^3 + (rp - rq)^3$
Clearly $a + b + c = 0, a^3 + b^3 + c^3 = 3abc$
So, $3(pq - pr)(qr - qp)(rp - rq)$
- (c) $a^3 + 8b^2 - 64c^3 + 24abc$
 $(a)^3 + (2b)^3 + (-4c)^3 - 3 \times a \times 2b \times -4c$
 $(a + 2b - 4c)(a^2 + 4b^2 + 16c^2 - 2ab + 8bc - 4ac)$

$$(d) \quad x^3 - 8y^3 - 64z^3 - 24xyz$$

$$(x)^3 + (-2y)^3 + (-4z)^3 - 3(-2y)(x)(-4z)$$

$$(x - 2y - 4z)(x^2 + 4y^2 + 16z^2 + 2xy - 8xz + 4zx)$$

$$(e) \quad 125 + 8x^3 - 27y^3 + 90xy$$

$$(5)^3 + (2x)^3 - (3y)^3 - 3 \times 5 \times 2x \times -3y$$

$$(5 + 2x - 3y)(25 + 4x^2 + 9y^2 - 10x + 6xy + 15y)$$

$$4. \quad \frac{73 \times 73 \times 73 + 27 \times 27 \times 27}{73 \times 73 - 73 \times 27 + 27 \times 27} \Rightarrow \frac{(73)^3 + (27)^3}{(73)^2 - 73 \times 27 + (27)^2}$$

$$\frac{a^3 + b^3}{a^2 - ab + b^2}, \quad \text{where } a = 73; b = 27$$

$$\Rightarrow \frac{(a+b)(a^2 - ab + b^2)}{(a^2 - ab + b^2)} = (a+b)$$

$$= (73 + 27) = 100$$

$$(b) \quad \frac{135 \times 135 \times 135 - 65 \times 65 \times 65}{135 \times 135 + 135 \times 65 + 65 \times 65} \Rightarrow \frac{(135)^3 - (65)^3}{(135)^2 + 135 \times 65 + (65)^2}$$

$$\frac{a^3 - b^3}{a^2 - ab + b^2}, \quad \text{where } a = 135; b = 65$$

$$\Rightarrow \frac{(a-b)(a^2 + ab + b^2)}{(a^2 + ab + b^2)} = (a-b)$$

$$= (135 - 65) = 70$$

$$(c) \quad \frac{0.87 \times 0.87 \times 0.87 + 0.13 \times 0.13 \times 0.13}{0.87 \times 0.87 - 0.87 \times 0.13 + 0.13 \times 0.13}$$

$$\Rightarrow \frac{(0.87)^3 + (0.13)^3}{(0.87)^2 - 0.87 \times 0.13 + (0.13)^2}$$

$$(0.87 + 0.13) = 1$$

$$(d) \quad \frac{27x^3 - 1000}{3x - 10} = \frac{(3x)^3 - (10)^3}{3x - 10} = \frac{(3x - 10)(9x^2 + 30x + 100)}{(3x - 10)}$$

$$= 9x^2 + 30x + 100$$

$$\begin{aligned}
 \text{(e)} \quad \frac{343x^3 - 64}{49x^2 + 36x + 16} &= \frac{(7x)^3 - (4)^3}{(7x)^2 + 7x \times 4 + (4)^2} \\
 &= \frac{(7x-4)(49x^2 + 28x + 16)}{(7x+4)(7x+4)}
 \end{aligned}$$

Mental Math I.Q.

- A.
- $$\begin{aligned}
 3(a-4b) - 9x(a-4b) &= (3-9x)(a-4b) \\
 &= 3(1-3x)(a-4b)
 \end{aligned}$$
 - $$3a(x+y) + 5b(x+y) - 7c(x+y) = (x+y)(3a+5b-7c)$$
 - $$9x^2 - 6xy + y^2 = (3x-y)^2 = (3x-y)(3x-y)$$
 - $$16x^2 - 9y^2 = (4x)^2 - (3y)^2 = (4x+3y)(4x-3y)$$
 - $$3a^3 - 3a = 3a(a^2 - 1) = 3a(a+1)(a-1)$$
 - $$\begin{aligned}
 \frac{1}{64}a^3 - \frac{1}{216}b^3 &\Rightarrow \left(\frac{1}{4}a\right)^3 - \left(\frac{1}{6}b\right)^3 \\
 &\Rightarrow \left(\frac{1}{4}a - \frac{1}{6}b\right) \left(\frac{a^2}{16} + \frac{b^2}{36} + \frac{ab}{24}\right)
 \end{aligned}$$
 - $$\begin{aligned}
 x^2 + 13x + 40 &= x^2 + 8x + 5x + 40 \\
 x(x+8) + 5(x+8) &= (x+5)(x+8)
 \end{aligned}$$
8. $a^4 - 81b^4$
- $$\begin{aligned}
 (a^2)^2 - (9b^2)^2 \\
 (a^2 + 9b^2)(a^2 - 9b^2) &= (a^2 + 9b^2)[(a^2 - (3b)^2)] \\
 &= (a^2 + 9b^2)(a+3b)(a-3b)
 \end{aligned}$$

Multiple Choice Questions

- (a) $(x-1)(x+1)$ 2. (c) $(a+b)(m+n)$
- (a) $4x$
- (b) 27; as, $x - \frac{1}{x} = 5 \Rightarrow x^2 + \frac{1}{x^2} = 25 + 2 = 27$
- (c) $(a-b)^2 = (5)^2 = a^2 + b^2 = 25 + 2(3) = 31$
- (c) $(4x-5y)(4x+5y)$
- (b) $81x^2 - 100$
 $(9x)^2 - (10)^2 = (9x+10)(9x-10)$
- (b) $\frac{(72)^2 - (38)^2}{(72-38)} \Rightarrow \frac{(72+38)(72-38)}{(72-38)} = 72+38 = 110$

7

Linear Equations in One Variable

Exercise 7A

1. $8x = 20 + 3x$

$8x - 3x = 20$

$5x = 20$

$x = 4$

3. $4x - 3 = 2x + 5$

$4x - 2x = 5 + 3$

$2x = 8$

$x = 4$

5. $5x - (3x - 1) = x - 4$

$5x - 3x + 1 = x - 4$

$5x - 3x - x = -4 - 1$

$x = -5$

2. $5x - 7 = 2x + 8$

$5x - 2x = 8 + 7$

$3x = 15$

$x = 5$

4. $8x - 11 - 5x + 3 = 2x + 4 - 3x$

$-11 + 3 - 4 = 2x - 3x + 5x - 8x$

$-12 = -4x$

$3 = x$

6. $10p - (3p - 4) = 4(p + 1)$

$10p - 3p + 4 = 4p + 4$

$10p - 3p - 4p = 4 - 4$

$3p = 0$

$p = 0$

7. $4(x + 3) - 2(x - 1) = 3x + 3$

$4x + 12 - 2x + 2 = 3x + 3$

$4x - 2x - 3x = 3 - 12 - 2$

$-x = -11$

$x = 11$

8. $\frac{2}{3}x + 1 = \frac{7}{3}$

$\frac{2}{3}x = \frac{7}{3} - 1$

$\frac{2}{3}x = \frac{7-3}{3} = \frac{4}{3}$

$\frac{2}{3}x = \frac{4}{3}$

$x = \frac{4 \times 3}{3 \times 2} = 2$

9. $\frac{1}{4}x + \frac{1}{6}x = x - 7$

$\frac{3x + 2x - 12x}{12} = -7$

$-7x = -7 \times 12 \Rightarrow x = 12$

10. $3x + \frac{2}{3}x = 2x + 1$

$3x - 2x = 1 - \frac{2}{3}$

$x = -\frac{1}{3}$

$$11. \frac{3x}{4} + \frac{x}{6} = 22$$

$$\frac{9x+2x}{12} = 22$$

$$11x = 22 \times 12$$

$$x = \frac{22 \times 12}{11}$$

$$x = 2 \times 12$$

$$x = 24$$

$$12. \frac{x-3}{5} + \frac{x-4}{7} = 6 - \frac{2x-1}{35}$$

$$\frac{7x-21+5x-20+2x-1}{35} = 6$$

$$14x-42=210$$

$$14x=252$$

$$x=18$$

$$13. \frac{4x+1}{3} + \frac{2x-1}{2} - \frac{3x-7}{5} = 6$$

$$\frac{40x+10+30x-15-18x+42}{30} = 6$$

$$52x+37=180$$

$$52x=143$$

$$x = \frac{143}{52} = \frac{11}{4} \text{ or } 2\frac{3}{4}$$

$$15. \frac{5x-3}{2x} = \frac{8}{9}$$

$$45x-27=16x$$

$$29x=27$$

$$x = \frac{27}{29}$$

$$17. \frac{19-3y}{1-9y} = \frac{8}{5}$$

$$95-15y=8-72y$$

$$87=-57y$$

$$-\frac{29}{19} = y$$

$$14. \frac{0.5y-4}{2.4y+6} = \frac{-5}{3}$$

$$1.5y-12=-12y-30$$

$$13.5y=-18$$

$$y = \frac{-18}{13.5} = \frac{-4}{3}$$

$$y = -1\frac{1}{3}$$

$$16. \frac{5+3x}{3-2x} = \frac{5}{3}$$

$$15+9x=15-10x$$

$$15-15=-19x$$

$$0=x$$

$$18. \frac{3x+4}{2x+5} = \frac{1}{2}$$

$$6x+8=2x+5$$

$$4x=-3$$

$$x = -\frac{3}{4}$$

$$19. \frac{z/4 - 3/5}{4/3 - 7z} = \frac{-3}{20}$$

$$5z - 12 = -4 + 21z$$

$$-8 = 16z$$

$$\frac{-1}{2} = z$$

$$21. 0.26x + 0.09x = 8 - 0.45x$$

$$0.35x + 0.45x = 8$$

$$0.8x = 8$$

$$x = 10$$

$$23. \frac{6x+7}{3x+2} = \frac{4x+5}{2x+3}$$

$$12x^2 + 14x + 18x + 21 = 12x^2 + 8x + 15x + 10$$

$$32x + 21 = 23x + 10$$

$$9x = -11$$

$$x = \frac{-11}{9}$$

$$24. \frac{2-7x}{1-5x} = \frac{3+7x}{4+5x}$$

$$8 + 10x - 28x - 35x^2 = 3 + 7x - 15x - 35x^2$$

$$-18x + 8 = 3 - 8x$$

$$10x = 5$$

$$x = \frac{1}{2}$$

$$26. (a) \frac{x^2 - 9}{5 + x^2} = \frac{-5}{9}$$

$$20. \frac{3x}{5x+2} = -4$$

$$3x = -20x - 8$$

$$23x = -8$$

$$x = \frac{-8}{23}$$

$$22. \frac{0.5y+4}{1.2y+8} = \frac{5}{3}$$

$$1.5y + 12 = 6y + 40$$

$$-28 = 4.5y$$

$$\frac{-28}{4.5} = y$$

$$\text{or } y = \frac{-56}{9}$$

$$25. \frac{(4+x)(5-x)}{(2+x)(7-x)} = 1$$

$$\frac{20 - 4x + 5x - x^2}{14 - 2x + 7x - x^2} = 1$$

$$20 + x - x^2 = 14 + 5x - x^2$$

$$6 = 4x$$

$$\frac{3}{2} = x$$

$$(b) \frac{2x^2 - 5}{x^2 + 2} = \frac{3}{2}$$

$$9x^2 - 81 = -25 - 5x^2$$

$$14x^2 = 56$$

$$x^2 = 4$$

$$x = 2$$

$$4x^2 - 10 = 3x^2 + 6$$

$$x^2 = 16$$

$$x = 4$$

Exercise 7B

1. Let the number be x

According to question

$$\frac{2}{3}x + 6 = 36$$

$$\frac{2}{3}x = 30$$

$$x = \frac{90}{2} = 45$$

$$x = 45$$

2. Let the numbers are $n, n+2, n+4$

According to question

$$n + n + 2 + n + 4 = 246$$

$$3n = 246 - 6$$

$$n = \frac{240}{3}$$

$$n = 80$$

So, the number are $n = 80, n + 2 = 82, n + 4 = 84$

3. Let the first part be x

According to question

$$\text{2nd part} = 2x - 32, \text{ 3rd part} = x + 18$$

$$\text{So, } x + 2x - 32 + x + 18 = 534$$

$$4x = 534 + 14$$

$$x = \frac{548}{4} = 137 = x$$

Ist part 137, 2nd = $2 \times 137 - 32 = 242$, 3rd = $137 + 18 = 155$

4. Let the numbers be $5x$ and $8x$

$$\text{So, } 5x + 8x = 182$$

$$13x = 182$$

$$x = \frac{182}{13}$$

$$x = 14$$

So numbers are :

$$5 \times 14 = 70; \quad 8 \times 14 = 112$$

5. Let the ten's digit be $= x$

$$\text{Unit's digit} = (15 - x)$$

$$\begin{aligned} \text{Original number} &= 10 \times \text{ten's digit} + \text{unit's digit} \\ &= 10 \times x + 15 - x = 9x + 15 \end{aligned}$$

On interchanging digits, new number

$$\begin{aligned} &= 10(15 - x) + x \\ &= 150 - 9x \end{aligned}$$

According to question

$$9x + 15 - 150 + 9x = 27$$

$$18x = 27 - 15 + 150 = 162$$

$$x = \frac{162}{18} = 9$$

So, Ten's digit $= 9$; ones digit $= 6$

$$\text{The number} = 9 \times 10 + 6 = 96$$

6. Let the numerator be x

According to question; Denominator $x + 3$

$$\begin{aligned} \text{As } \frac{x-3}{x+2+3} &= \frac{1}{5} \\ 5x-15 &= x+5 \\ 4x &= 20 \\ x &= 5 \end{aligned}$$

Numerator $= 5$, denominator $= 8$

$$\text{Required fraction} = \frac{5}{8}$$

7. Let the breadth be x

then length be $x + 9$

$$\text{Area of given rectangle is} = x^2 + 9x$$

Now, A.T.Q. Area of new rectangle is

$$(x+9+3)(x+3) = x^2 + 15x + 36$$

$$\text{As } x^2 + 9x + 84 = x^2 + 15x + 36$$

$$84 - 36 = 15x - 9x$$

$$48 = 6x$$

$$8 = x$$

So, length = $8 + 9 = 17$; breadth = 8

8. Let the ratio be x

as Rama age = $3x$; Namita age = $8x$

According to question

Rama age = $3x - 3$. Namita age = $8x + 2$

Then $(8x + 2) = 6(3x - 3)$

$$8x + 2 = 18x - 18$$

$$20 = 10x$$

$$2 = x$$

So, Rama age = $3 \times 2 = 6$; Namita age = $8 \times 2 = 16$

9. A purse has only 2-rupee and 5-rupee coins.

Let the 2 rupee coins be x and 5-rupee coins be y .

So, According to question

$$x + y = 48$$

and $2x + 5y = ₹132$

From eq. (i)

$$x = 48 - y$$

$$2(48 - y) + 5y = 132$$

$$96 - 2y + 5y = 132$$

$$3y = 36$$

$$y = 12$$

As, $x = 48 - 12$

$$x = 36$$

So, the 2 rupees coins are 36

10. The perimeter of a rectangle is 240 cm

Let the length and breadth be x , y

as $2(l + b) = 240$

$$2(x + y) = 240 \text{ or } x + y = 120 \quad \dots\dots\dots(i)$$

$$2 \left[\left(x - \frac{10x}{100} \right) + \left(y + \frac{20y}{100} \right) \right] = 240$$

$$x - \frac{10}{100}x + y + \frac{20}{100}y = 120$$

$$x + y - \frac{10x}{100} + \frac{20}{100}y = 120$$

$$9x + 12y = 1200, \quad \dots\dots\dots (i)$$

$$x + y = 120 \quad \dots\dots\dots (ii)$$

$$9x + 12y = 1200$$

$$\underline{-9x + 9y = 1080}$$

$$3y = 120$$

$$y = 40$$

$$x + y = 120$$

$$x + 40 = 120$$

$$x = 120 - 40 = 80$$

So, the length = 80 cm; the breadth = 40 cm

11. Given speed of the stream = 1.5 km/hr

Let the speed of motor boat = x km/hr

Speed of boat in the direction of stream = (x + 1.5) km/hr

Speed in opposite direction = (x - 1.5) km/hr

Distance travelling in the direction of stream in 5 hour

$$= 5(x + 1.5)$$

Distance travelled in opposite direction in $\frac{11}{2}$ hr

$$= \frac{11}{2}(x - 1.5)$$

As per question

$$5(x + 1.5) = \frac{11}{2}(x - 1.5)$$

$$2(5x + 7.5) = 11x - 16.5$$

$$10x + 15 = 11x - 16.5$$

$$15 + 16.5 = 11x - 10x$$

$$x = 31.5$$

So, speed of the stream in still water = x = 31.5 km/h

12. Let total work be = x

Gorav complete x work in 18 hours

$$\text{So, Gorav 1 hour work} = \frac{x}{18}$$

$$\text{Sorav 1 hour work} = \frac{x}{24}$$

$$\text{Sorav 2 hour work} = \frac{x}{24} \times 2 = \frac{x}{12}$$

$$\text{Remaining work} = \frac{x}{1} - \frac{x}{12} = \frac{11x}{12}$$

$$\text{Sorav and Gorav 1 hour work} = \frac{x}{18} + \frac{x}{24} = \frac{4x+3x}{72} = \frac{7x}{72}$$

$$\text{Both of them complete } \frac{7x}{72} \text{ work in 1 hour}$$

$$\text{Both of them complete 1 work in} = \frac{1 \times 72}{7x}$$

$$\text{Both of them complete } \frac{11x}{12} \text{ work} = \frac{1 \times 72}{7x} \times \frac{11x}{12} = \frac{66}{7} \text{ hrs.}$$

$$\text{or } 9\frac{3}{7} \text{ hours}$$

$$\text{So, they will complete the work in} = 9\frac{3}{7} + 2 = 11\frac{3}{7} \text{ hours}$$

Mental Math I.Q.

$$\begin{aligned} 1. \quad & \frac{2y+1}{y+2} = \frac{4}{5} \\ & 10y+5 = 4y+8 \\ & 6y = 3 \\ & y = \frac{1}{2} \end{aligned}$$

$$\begin{aligned} 2. \quad & 0.3(6+m) = 0.4(8-m) \\ & 1.8+0.3m = 3.2-0.4m \\ & 0.7m = 1.4 \\ & m = 2 \end{aligned}$$

3. Let the ratio be x

$$3x + 4x + 5x = 180^\circ \text{ (Angle sum property of triangle)}$$

$$12x = 180^\circ$$

$$x = \frac{180}{12}$$

$$x = 15$$

$$\text{So angles are } 3 \times 15 = 45$$

$$4 \times 15 = 60$$

$$5 \times 15 = 75$$

4. Let the ratio be x

According to question $23x + 7x = 60$

$$30x = 60$$

$$x = 2$$

So, numbers are $= 23 \times 2 = 46$; $7 \times 2 = 14$

Multiple Choice Questions

1. $2x + 7 = x + 9$

$x = 2$ (c)

2. $6(y - 3) - 3(y - 7) = 0$

$6y - 18 - 3y + 21 = 0$

3. $\frac{7m + 2}{5} = \frac{6m - 5}{11}$

$77m + 22 = 30m - 25$

$47m = -47$

$m = -1$ (b)

$3y - 3$

$y = -1$ (b)

4. Let the number be x .

$3x + 6 = 45$

$3x = 39$

$x = 13$ (a)

5. Let the number be $x, x + 2, x + 4$

$x + x + 2 + x + 4 = 24$

$3x = 18$

$x = 6$

Numbers are 6, 8, 10 (a)

6. Let the ratio be x

$5x + 11x = 160$

$x = 10$

So numbers are, $5 \times 10 = 50$; $11 \times 10 = 110$

7. Let the ratio be x

$5x - 2x = 60$

$3x = 60$

$x = 20$

So numbers are, 40, 100 (a)

8. Let the son age be x ; then Ajay age will be $3x$; after 12 years

$x + 12, 3x + 12$

A.T.Q. $2(x + 12) = (3x + 12)$

$2x + 24 = 3x + 12$

$12 = x$

So, Son age = 12; Ajay age = 36 (a)

Percentage and Its Application

Exercise 8A

1. (a) 30%

$$\frac{30}{100} = \frac{3}{10}$$

or 3 : 10

(b) 2.5%

$$\frac{25}{1000} = \frac{1}{40}$$

1 : 40

(c) 0.75%

$$\frac{75}{10000} = \frac{3}{4000}$$

3 : 4000

(d) 125%

$$\frac{125}{100} = \frac{5}{4}$$

5 : 4

(e) $12\frac{1}{2}\% = \frac{25}{2}\%$

$$\frac{25}{2 \times 100} = \frac{1}{8} \quad \text{or } 1 : 8$$

2. (a) $\frac{3}{4} = \frac{3}{4} \times 100 = 75\%$

(b) $\frac{13}{75} = \frac{13}{75} \times 100 = 17\frac{1}{3}\%$

(c) $0.18 = \frac{18}{100} \times 100 = 18\%$ (d) $0.275 = \frac{275}{1000} \times 100 = 27.5\%$

(e) $1.25\% = \frac{1.25}{100} \times 100 = 125\%$

3. (a) $\frac{12}{100} \times 1200 = ₹144$

(b) $\frac{13}{100} \times 6500 = ₹845$

(c) $\frac{20}{100} \times 800 = ₹160$

4. Decrease = $60 - 45 = 15$

$$\text{Decrease}\% = \frac{15}{60} \times 100 = 25\%$$

5. Let the cost be x

$$x + \frac{20}{100} \times x = 600 \quad \Rightarrow \quad \frac{x}{1} + \frac{x}{5} = 600$$

$$5x + x = 3000$$

$$x = \frac{3000}{5} = 600$$

6. Candidates are A and B, Let the votes be = 100

$$100 - 46 = 54\% \text{ votes will be got by B}$$

$$\text{As } 54 - 46 = 8$$

So the no of valid votes be

$$= \frac{100}{8} \times 1600$$

$$= 20,000 \text{ votes}$$

7. Let the total gunpowder is 100 g

Out of it 75 nitre and 10 sulphure and remaining were

$$= 100 - 85 = 15\text{g}$$

The amount of charcoal in 9000 g of given powder is

$$= \frac{15}{100} \times 9000$$

$$= 1350 \text{ g or } 1\text{kg } 35\text{gm}$$

8. Let the expenditure is ₹100

$$\text{So total be } 30 + 3 = 33$$

∴ Total salary for the month would be

$$= \frac{2310}{33} \times 100 = ₹7000$$

9. Let the total money the man had = ₹100

$$\text{Spent on children} = ₹40$$

$$\text{Remaining money} = ₹100 - ₹40 = ₹60$$

$$20\% \text{ of remaining} = ₹60 \times \frac{20}{100} = ₹12$$

$$\text{So, now balance} = ₹60 - ₹12 = ₹48$$

$$\text{So, actual money the man has} = \frac{100}{48} \times \frac{9600}{1} = ₹20000$$

10. Let the cost of sugar be = ₹ 100

$$\text{Increased cost} = ₹ 125$$

$$\text{So, consumption a housewife should decrease} = \frac{25}{125} \times 100 = 20\%$$

11. Let the maximum marks be = 100x

$$\text{Fist student got} = 25x \text{ marks}$$

So pass marks = $25x + 30$ (i)

Second student got = $50x$ marks

So, pass marks = $50x - 20$ (ii)

Comparing (i) and (ii)

$$25x + 30 = 50x - 20$$

$$25x = 50; x = 2$$

So, the maximum marks = $100 \times 2 = 200$ marks

So, minimum pass marks

$$= 25 \times 2 + 30$$

$$= 50 + 30 = 80 \text{ marks}$$

12. Let the original salary of the officer be = 100

Increased salary = $100 + 50 = 150$

So, the salary % to be decreased = $\frac{50}{150} \times 100 = 33\frac{1}{3}\%$

Exercise 8B

1. C.P. of CD player = ₹ 1500

$$\text{S.P.} = 1750$$

$$\text{Gain} = \text{S.P.} - \text{C.P.}$$

$$= 1750 - 1500$$

$$= 250$$

$$\text{Gain \%} = \left(\frac{\text{Gain}}{\text{C.P.}} \times 100 \right) \%$$

$$= \frac{250}{1500} \times 100 = 16\frac{2}{3}\%$$

2. C.P. = ₹ 2200; S.P. = ₹ 1980

$$\text{Loss} = ₹ 2200 - ₹ 1980$$

$$= ₹ 220$$

$$\text{Loss \%} = \left(\frac{\text{Loss}}{\text{C.P.}} \times 100 \right) \%$$

$$= \frac{220}{2200} \times 100 = 10\%$$

$$\begin{aligned}
 3. \quad \text{Total C.P.} &= ₹12000 + ₹2850 \\
 &= ₹14850 \\
 \text{S.P.} &= ₹13860
 \end{aligned}$$

As S.P. < C.P.

$$\begin{aligned}
 \text{Loss} &= ₹14850 - ₹13860 \\
 &= ₹90
 \end{aligned}$$

$$\text{Loss \%} = \frac{90}{14850} \times 100 = 6\frac{2}{3}\%$$

4. Let the C.P. of 18 mangoes be x

$$\text{The C.P. of 1 mango} = \frac{x}{18}$$

But, S.P. of 16 mangoes = x

$$\text{S.P. of 1 mango} = \frac{x}{16}$$

$$\text{Profit} = \frac{x}{16} - \frac{x}{18} = \frac{x}{144}$$

$$\text{P\%} = \frac{x \times 18}{144 \times x} \times 100 = 12\frac{1}{2}\%$$

5. Let the C.P. of 25 chairs be x

$$\text{Then C.P. of 1 chair} = \frac{x}{25}$$

But, S.P. of 30 chairs = x

$$\text{S.P. of 1 chair} = \frac{x}{30}$$

$$\text{Loss} = \frac{x}{25} - \frac{x}{30} = \frac{x}{150}$$

$$\text{Loss\%} = \frac{x \times 25}{150 \times x} \times 100 = \frac{50}{3} = 16\frac{2}{3}\%$$

6. As vendor brought orange at 20 for ₹ 56

$$\begin{aligned}
 \text{C.P. of 1 orange} &= \frac{56}{20} \\
 &= ₹2.8
 \end{aligned}$$

$$\text{S.P. of 12 oranges} = ₹35$$

$$\text{S.P. of 1 orange} = \frac{35}{12}$$

$$\text{Profit} = \frac{35}{12} - \frac{28}{10} = \frac{350 - 336}{12 \times 10} = \frac{14}{120} = \frac{7}{60}$$

$$\text{Profit \%} = \frac{7 \times 10 \times 100}{60 \times 28} = \frac{25}{6} = 4\frac{1}{6}\%$$

7. ₹400 = S.P. of article

Let the C.P. be x

$$\text{Profit is to be} = \frac{1}{4}x$$

$$\text{g\%} = \frac{1 \times x}{4 \times x} \times 100 = 25\%$$

8. Dress sold at = ₹960

Let the C.P. of = x

$$\text{The gain amount} = \frac{1}{9}x$$

G = S.P. - C.P. as,

$$\frac{1}{9}x = 960 - x$$

$$\frac{1 \times x}{9} + x = 960$$

$$10x = 960 \times 9$$

$$x = 864$$

$$\text{C.P.} = ₹864$$

$$\text{Profit\%} = \frac{1 \times x}{9 \times x} \times 100 = 11.11\%$$

9. C.P. = ₹3,00,000

S.P. of $\frac{1}{3}$ is at loss of 20%

$$\text{C.P. of } \frac{1}{3} = \frac{1}{3} \times 300000 = 1,00000$$

$$\text{Then 20\% of it} = \frac{20}{100} \times 100000 = 20000$$

$$\text{Loss} = 20000$$

S.P. of $\frac{2}{5}$ is at gain 25%

$$\frac{2}{5} \times 300000 = 120000$$

$$\text{Gain} = \frac{25}{100} \times 120000 = 30000$$

$$\text{Overall 10\% is gain then} = \frac{10}{100} \times 300000 = ₹30000$$

$$\text{And net gain} = 30000 - 20000 = 10000$$

So, we should have a gain = $30000 - 10000 = 20000$

$$\text{As the land remaining is} = 1 - \frac{1}{3} - \frac{2}{5} = \frac{15 - 5 - 6}{15} = \frac{4}{15}$$

$$\text{C.P. of } \frac{4}{15} \times 300000 = 80000$$

$$\text{The S.P. would be} = 80000 + 20000 = ₹100000$$

10. Let the C.P. of 1000 gm gold be x

$$\text{Then C.P. of 1 gm} = \frac{x}{1000}$$

$$\text{The S.P. of 980 gm} = x$$

$$\text{S.P. of 1 gm gold} = \frac{x}{980}$$

$$\begin{aligned} \text{Profit} &= \frac{x}{980} - \frac{x}{1000} \\ &= \frac{20x}{980 \times 1000} = \frac{x}{49000} \end{aligned}$$

$$P\% = \frac{x \times 1000}{49000 \times x} \times 100 = 2\frac{2}{49}\%$$

11. C.P. of two fans ₹ 2160

Let the C.P. of 1st fan be x

$$\text{C.P. of 2nd fan will be} = ₹(2160 - x)$$

$$\text{Profit on 1st fan} = 15\% \text{ of } x$$

$$= \frac{15x}{100}$$

$$\text{S.P. of 1st fan} = ₹ \left(x + \frac{15x}{100} \right)$$

$$\text{Loss on 2nd fan} = 9\% \text{ of } ₹ (2160 - x)$$

$$= ₹ \left(\frac{9}{100} \times (2160 - x) \right)$$

$$\text{S.P. of 2nd fan} = \text{C.P.} - \text{Loss}$$

$$= ₹ (2160 - x) - \frac{9(2160 - x)}{100}$$

$$= (2160 - x) \left(\frac{91}{100} \right)$$

It is given that S.P. of each fan is the same.

$$\frac{x}{1} + \frac{15x}{100} + (2160 - x) \left(\frac{91}{100} \right) = 2160$$

$$\frac{115x}{100} + \frac{91(2160 - x)}{100} = 2160$$

$$11x + 19650 - 91x = 216000$$

$$24x = 19440$$

$$x = \frac{19440}{24} = 810$$

$$\text{and cost of 2nd fan} = 2160 - 810$$

$$= ₹ 1350$$

12. Let C.P. of bucket be = ₹x

$$\text{Loss \%} = 8\%$$

$$\text{So, S.P.} = x - \left(\frac{x \times 8}{100} \right)$$

$$= \frac{92x}{100}$$

$$\text{No, again profit} = 8\%$$

$$\text{So, S.P.} = x + \left(\frac{x \times 8}{100} \right)$$

$$= \frac{108x}{100}$$

According to question

$$\frac{108x}{100} - \frac{92x}{100} = 28$$

$$108x - 92x = 2800$$

$$16x = 2800$$

$$x = 175$$

So, C.P. of the basket = ₹175

13. Cost of 50 chairs = ₹50,000

C.P. of 1 chair = ₹50000 ÷ 50

= ₹1000

So, S.P. of one damage chair = ₹1000 × $\frac{3}{4}$

S.P. of 20 damage chairs = ₹750 × 20 = ₹1500

To gain 35% overall profit, we should sell the chairs in

$$\left(50000 + 50000 \times \frac{35}{100} \right) = 67500$$

So, S.P. of 30 chairs = ₹67500 - ₹15000 = ₹52500

So, S.P. of 1 chair = ₹ $\frac{52500}{30}$ = ₹1750 each

14. Let the actual C.P. be = ₹x

$$\text{S.P. in first case} = x + \left(x \times \frac{5}{100} \right)$$

$$= \frac{x}{1} + \frac{x}{20} = \frac{21x}{20}$$

$$\text{S.P. in second case} = x - \left(x \times \frac{5}{100} \right)$$

$$= \frac{19x}{20}$$

According to question :

$$\frac{21x}{20} - 50 = \frac{19x}{20}$$

$$\frac{21x - 1000}{20} = 19x$$

$$21x - 19x = 1000$$

$$2x = 1000$$

$$x = 500$$

$$\text{So, S.P.} = \frac{21 \times 500}{20} = ₹525$$

15. Let C.P. be = $100x$

$$5\% \text{ of } 100x = 5x$$

$$\text{So, First S.P.} = 105x$$

$$\text{New C.P.} = 95x$$

$$10\% \text{ of } 95x = 9.5x$$

$$\begin{aligned} \text{New S.P.} &= 95x + 9.5x \\ &= 104.5x \end{aligned}$$

According to question

$$105x - 104.5x = 2$$

$$0.5x = 2$$

$$x = \frac{2}{0.5} = 4$$

$$\text{So, C.P. will be} = 4 \times 100 = 400$$

Exercise 8C

1. (i) MP = ₹650 and discount = 10%

$$\text{Discount\%} = \frac{D}{\text{M.P.}} \times 100$$

$$\frac{650 \times 10}{100} = D$$

$$D = ₹65$$

$$\text{S.P.} = (\text{M.P.} - D)$$

$$= (650 - 65)$$

$$= ₹585$$

(ii) MP = ₹ 5450 and discount = 5%

$$D\% = \frac{D}{M.P.} \times 100$$
$$\frac{5 \times 5450}{100} = D$$
$$D = ₹272.5$$
$$S.P. = (MP - D)$$
$$= (5450 - 272.5)$$
$$= ₹5177.5$$

2. (i) S.P. = ₹3430; D = 2%

$$\text{Let M.P.} = ₹100$$
$$\text{Discount} = ₹2$$
$$S.P. = ₹(100 - 2) = ₹98$$

So, Actual M.P. = $\frac{100}{98} \times \frac{3430}{1} = ₹3500$

(ii) S.P. = ₹9250; D = 7.5%

$$\text{Let M.P.} = ₹100$$
$$\text{Discount} = ₹7.50$$
$$S.P. = ₹(100 - 7.50) = ₹92.50$$

So, Actual M.P. = $\frac{100}{92.50} \times \frac{9250}{1}$

$$= ₹10,000$$

3. (i) $D\% = \frac{M.P. - S.P.}{M.P.} \times 100$

$$D\% = \frac{625 - 562.5}{62.5} \times 100$$
$$= \frac{6250.0}{625} = 10\%$$

(ii) $D\% = \frac{M.P. - S.P.}{M.P.} \times 100$

$$D\% = \frac{1600 - 1180}{1600} \times 100 = \frac{420 \times 100}{1600}$$

$$D\% = 26\frac{1}{4}\%$$

4. M.P. = ₹18500, D% = 12%

$$D\% = \frac{\text{Discount}}{\text{M.P.}} \times 100$$

$$\frac{12 \times 18500}{100} = \text{Discount}$$

$$2220 = \text{Discount}$$

So, S.P. = M.P. - Discount

$$= 18500 - 2220$$

$$= ₹ 16280$$

5. Let M.P. = ₹100; D = 12% or ₹ 12

So, S.P. = ₹100 - ₹12

$$= ₹88$$

So, M.P. = $\frac{100}{88} \times \frac{880}{1} = ₹ 1000$

6. C.P. = 3000; D = 10%; P = 20%

$$\text{S.P.} = \frac{CP(100 + P)}{100}$$

$$= \frac{3000(100 + 20)}{100}$$

$$= \frac{3000 \times 120}{100}$$

$$= ₹ 3600$$

Let, M.P. = ₹100; D = 10%

So, S.P. = ₹ 100 - ₹ 10 = ₹ 90

So, Actual M.P. = $\frac{100}{90} \times \frac{3600}{1}$

$$= ₹ 4000$$

7. Let C.P. = ₹100; Profit % = 20; Profit = ₹20

$$\text{S.P.} = ₹100 + ₹20 = ₹120$$

$$\text{Actual profit} = ₹360$$

$$\text{Actual S.P.} = \frac{120}{20} \times 360 = ₹2160$$

Now, Let M.P. be = ₹100

$$\text{Discount} = 25\%$$

So, S.P. = ₹75

$$\text{Actual M.P.} = \frac{100}{75} \times \frac{2160}{1} = ₹2880$$

8. Let the C.P. be ₹100; The gain required = 20%

$$\text{The S.P.} = ₹(100 + 20) = ₹120$$

$$\text{Discount allowed} = 25\%$$

Let the marked price be x

$$\text{Then discount} = 25\% \text{ of } x = ₹ \left(\frac{25}{100} \times x \right) = \frac{x}{4}$$

$$\text{S.P.} = \text{M.P.} - \text{Discount}$$

$$= ₹ \left(x - \frac{x}{4} \right) = \frac{3x}{4}$$

But S.P. = ₹120

$$\frac{3x}{4} = 120$$

$$x = \frac{120 \times 4}{3}$$

$$x = ₹160$$

Hence the shopkeeper should mark 60% more.

9. The C.P. = ₹450, The gain required = 20%

$$\frac{20}{100} \times 450 = 90$$

$$\text{S.P.} = ₹(450 + 90) = 540$$

$$\text{Discount} = 10\%$$

Let S.P. be = ₹x
Discount = 10% of x

$$= \frac{x}{10}$$
So, S.P. = $x - \frac{x}{10} = \frac{9x}{10} = 540$

$$x = \frac{540 \times 10}{9}$$

$$= ₹600$$

10. M.P. = ₹18500

$$\text{Ist Discount} = \frac{20}{100} \times 18500$$

$$= ₹3700$$

$$= 18500 - 3700 = ₹14800$$

$$\text{IInd Discount} = 5\% \text{ of } 14800$$

$$= \frac{5}{100} \times 14800 = 740$$

$$\text{Net Selling price} = (14800 - 740)$$

$$= ₹14060$$

11. Let the marked price be ₹100

Then the Ist discount given on it = ₹20

The price after discount = ₹(100 - 20) = ₹80

The next discount = 5% of 80

$$= \frac{5}{100} \times 80 = ₹4$$

The price after the second discount = ₹(80 - 4) = ₹76

The net S.P. = ₹76

The single discount equivalent to

$$\text{Discount} = (100 - 76) = 24\%$$

Check Your Mental Math IQ

$$1. \quad \frac{20}{100} \times x = 200$$
$$x = \frac{200 \times 10}{2}$$

$$x = 1000$$

$$2. \quad 100 = \frac{400 \times x}{100}$$

$$25\% = x$$

$$3. \text{ After 1 year salary will be increase} = \frac{10}{100} \times 500$$

$$\text{So it become} = ₹5500$$

$$\text{After 2 years} = \frac{10}{100} \times 5500$$

$$\text{i.e.} = 5500 + 550 = ₹6050$$

$$4. \quad \text{Total C.P.} = 5000 + 250 = 5250$$

$$\text{S.P.} = ₹4000$$

$$\text{Loss} = 5250 - 4000 = ₹1250$$

$$5. \quad P = \frac{20}{100} \times 3000$$

$$P = 600$$

$$\text{S.P.} = 3000 + 600 = ₹3600$$

$$6. \quad \text{M.P.} = \frac{100 \times \text{S.P.}}{100 - \text{Discount}}$$

$$D\% = 12\%; \text{S.P.} = ₹880$$

$$\text{M.P.} = \frac{100 \times 880}{(100 - 12)} \times 3000$$

$$= \frac{100 \times 880}{88}$$

$$\text{M.P.} = ₹1000$$

$$7. \text{ C.P. of 6 article} ₹5$$

$$\text{C.P. of 1 article} = ₹ \frac{5}{6}$$

S.P. of 5 article = ₹6

S.P. of 1 article = ₹ $\frac{6}{5}$

$$\text{Gain} = \frac{6}{5} - \frac{5}{6} = \frac{36 - 25}{30} = \frac{11}{30}$$

$$\text{Gain}\% = \frac{11 \times 6}{30 \times 5} \times 100 = 44\%$$

Multiple Choice Questions (M.C.Q.)

1. $50 \times ? = \frac{20}{100} \times 4000$
 $? = \frac{800}{50} = 16$ (b)

2. Let the original number be x

$$\text{as one increased } 20\% = \frac{20}{100} \times x = \frac{x}{5}$$

$$\text{New one is} = x + \frac{x}{5} = \frac{6x}{5}$$

$$\text{Then Increased } 20\% = \frac{20 \times 6x}{100 \times 5} = \frac{6x}{25}$$

$$\text{Newer one will be} = \frac{6x}{25} + \frac{6x}{5} = \frac{6x + 30x}{25} = \frac{36x}{25}$$

$$\text{So, total increased} = \frac{36x}{25} - x = \frac{11x}{25}$$

$$\% \text{ increased} = \frac{11x}{25 \times x} \times 100 = 44\% (d)$$

3. $\text{C.P.} = \frac{S.P. \times 100}{(100 + P\%)}$
 $\text{C.P.} = \frac{420 \times 100}{(100 + 5)} = \frac{420 \times 100}{105}$
 $= ₹400$ (a)

4. First chair = ₹600; Gain = 20%

$$\text{First C.P.} = \frac{S.P. \times 100}{(100 + P\%)}$$

$$= \frac{600 \times 100}{120} = ₹500$$

$$\text{Second C.P.} = \frac{600 \times 100}{75} = ₹800$$

$$\begin{aligned} \text{Total C.P.} &= ₹500 + ₹800 \\ &= ₹1300 \end{aligned}$$

$$\begin{aligned} \text{Total S.P.} &= ₹600 + ₹600 = ₹1200 \\ &= ₹1300 - ₹1200 \\ &= ₹100 \text{ (c)} \end{aligned}$$

5. Let C.P. be x

$$\text{S.P. of article} = \frac{3}{5} \times x$$

$$L = \text{C.P.} - \text{S.P.}$$

$$L = x - \frac{3}{5} \times x$$

$$= \frac{2x}{5}$$

$$L\% = \frac{2x}{5 \times x} \times 100$$

$$L = 40\% \text{ (a)}$$

6. S.P. = ₹4200; M.P. = ₹5000;

$$D = \text{M.P.} - \text{S.P.}$$

$$= 5000 - 4200 = ₹800$$

$$D\% = \frac{800}{5000} \times 100$$

$$D\% = 16\% \text{ (a)}$$

9

Compound Interest

$$\begin{aligned} 1. \quad \text{Amount} &= P \left(1 + \frac{r}{100} \right)^t \\ &= 2000 \left(1 + \frac{15}{100} \right)^3 \\ &= 2000 \times \frac{115}{100} \times \frac{115}{100} \times \frac{115}{100} \\ &= ₹3041.75 \end{aligned}$$

$$\begin{aligned} \text{So, compound interest} &= \text{Amount} - \text{Principal} \\ &= ₹3041.75 - ₹2000 = ₹1041.75 \end{aligned}$$

2. $P = ₹6000$; $R = 12\%$; $T = 2$ years

$$\begin{aligned} \text{Amount} &= 6000 \left(1 + \frac{12}{100} \right)^2 \\ &= 6000 \times \frac{112}{100} \times \frac{112}{100} = ₹7526.40 \end{aligned}$$

$$\text{Compound Interest} = ₹7526.40 - ₹6000 = ₹1526.40$$

3. Here, $P = ₹50000$, $T = 3$ years; Rate 10%

$$\begin{aligned} \text{Amount} &= 50000 \left(1 + \frac{10}{100} \right)^3 \\ &= 50000 \times \frac{110}{100} \times \frac{110}{100} \times \frac{110}{100} = ₹66550 \end{aligned}$$

$$\text{Compound interest} = ₹66550 - ₹50000 = ₹16550$$

4. Here, $P = ₹20000$; Time = 3 years; Rate = 5%

$$\text{Amount} = 20000 \left(1 + \frac{5}{100} \right)^3$$

$$= 20000 \times \frac{105}{100} \times \frac{105}{100} \times \frac{105}{100}$$

$$= ₹23150.50$$

5. P = ₹25000; Time = $1\frac{1}{2}$; years; Rate = 8% half yearly

As interest compound half yearly

$$\text{So, Time} = 1\frac{1}{2} \times 2 = 3 \text{ half years}$$

$$\text{And Rate} = \frac{8}{2} = 4\%$$

$$\text{So, Amount} = 25000 \left(1 + \frac{4}{100}\right)^3$$

$$= 25000 \times \frac{26}{25} \times \frac{26}{25} \times \frac{26}{25} = ₹28121.60$$

$$\text{So, Compound Int.} = ₹28121.60 - ₹25000 = ₹3121.60$$

6. Here, P = ₹2000, Time = $1\frac{1}{2}$ years ; R = 10%

As interest compounded half yearly

So, Time will be = 3 years and Rate 5%

$$\text{So, Amount} = 2000 \left(1 + \frac{5}{100}\right)^3$$

$$= 2000 \times \frac{21}{20} \times \frac{21}{20} \times \frac{21}{20} = ₹2315.25$$

$$\text{So, CI} = ₹2315.25 - ₹2000 = ₹315.25$$

7. Here P = ₹25000, Time = $1\frac{1}{2}$ years; Rate = 20%

As interest compounded half yearly

So, Time will be = 3 years and Rate = 10%

$$\text{So, Amount} = 25000 \left(1 + \frac{10}{100}\right)^3$$

$$= 25000 \times \frac{11}{10} \times \frac{11}{10} \times \frac{11}{10} = ₹33275$$

8. Here $P = ₹10000$; Time = 6 months; Rate = 12%

As interest compounded quarterly

So, Time will be = 2 quarters; Rate = $\frac{12}{4} = 3\%$

$$\begin{aligned}\text{So, Amount} &= 10000 \left(1 + \frac{3}{100}\right)^2 \\ &= 10000 \times \frac{103}{100} \times \frac{103}{100} \times \frac{103}{100} = ₹10609\end{aligned}$$

Exercise 9B

1. $P = ₹8500$; $R = 8\%$; $T = 2$ years

$$\begin{aligned}A &= P \left(1 + \frac{R}{100}\right)^T \\ &= 8500 \left(1 + \frac{8}{100}\right)^2 \\ &= 8500 \times \frac{108}{100} \times \frac{108}{100} = ₹9914.40\end{aligned}$$

$$\text{C.I.} = 9914.40 - 8500 = ₹1414.40$$

2. $P = ₹50000$; $R = 10\%$; $T = 2\frac{1}{2}$ years

$$\begin{aligned}A &= 50000 \left(1 + \frac{10}{100}\right)^2 \times \left(1 + \frac{10}{100} \times \frac{1}{2}\right)^1 \\ &= 50000 \times \frac{110}{100} \times \frac{110}{100} \times \frac{21}{20} = ₹635250\end{aligned}$$

$$\text{C.I.} = ₹635250 - ₹50000 = ₹135250$$

3. $P = ₹2500$; $R = 9\%$; $T = 2$ years

$$\begin{aligned}A &= 2500 \left(1 + \frac{9}{100}\right)^2 \\ &= 2500 \times \frac{109}{100} \times \frac{109}{100} = ₹2970.25\end{aligned}$$

$$\text{C.I.} = ₹(2970.25 - 2500) = ₹470.25$$

4. $P = ₹3200$; $R = 25\%$; $T = 3$

$$\begin{aligned} A &= 3200 \left(1 + \frac{25}{100} \right)^3 \\ &= 3200 \times \frac{5}{4} \times \frac{5}{4} \times \frac{5}{4} = ₹6250 \end{aligned}$$

$$\text{C.I.} = ₹(6250 - 3200) = ₹3050$$

5. $P = ₹15625$; $R = 4\%$; $T = 2$ years

$$\begin{aligned} A &= 15625 \left(1 + \frac{4}{100} \right)^2 \\ &= 15625 \times \frac{104}{100} \times \frac{104}{100} = ₹16900 \end{aligned}$$

$$\text{C.I.} = ₹16900 - ₹15325 = ₹1275$$

6. $P = ₹6400$; $R = 17.5\%$; $T = 2$ years

$$\begin{aligned} A &= 6400 \left(1 + \frac{17.5}{100} \right)^2 \\ &= 6400 \times \frac{117.5}{100} \times \frac{117.5}{100} = ₹8836 \end{aligned}$$

$$\text{C.I.} = ₹(8836 - 6400) = ₹2436$$

7. $P = ₹1000$; $T = 2$ years; $R = 20\%$

As. C.I. compounded half yearly

So, $T = 4$ half years; $R = 10\%$

$$\begin{aligned} A &= 1000 \left(1 + \frac{10}{100} \right)^4 \\ &= 1000 \times \frac{11}{10} \times \frac{11}{10} \times \frac{11}{10} \times \frac{11}{10} = ₹1464.10 \end{aligned}$$

$$\text{C.I.} = ₹(1464.10 - 1000) = ₹464.10$$

8. $P = ₹4016$; $T = 18$ months; $R = 12.5\%$

As, CI compounded half yearly

$$\text{So, Time} = 3 \text{ half years; } R = \frac{12.5}{2} = 6.25\%$$

$$\begin{aligned} A &= 4016 \left(1 + \frac{6.25}{100} \right)^3 \\ &= 4016 \times \frac{106.25}{100} \times \frac{106.25}{100} \times \frac{106.25}{100} = ₹4817.04 \end{aligned}$$

9. Let the principal be = ₹100

According to question,

$$\text{Interest} = \frac{100 \times 3 \times 6.25}{100} = ₹18.75$$

$$\text{Actual principal} = \frac{100}{18.75} \times 2400 = ₹12800$$

Now, P = ₹12800, Time = 3 years; Rate = 6.25%

$$\begin{aligned} A &= 12800 \left(1 + \frac{6.25}{100} \right)^3 \\ &= 12800 \times \frac{106.25}{100} \times \frac{106.25}{100} \times \frac{106.25}{100} \\ &= ₹15353.13 \end{aligned}$$

$$\text{C.I.} = ₹(15353.13 - 12800) = ₹2553.13$$

10. P = ₹320000; T = 1 year; R = 20%

As, CI is compound quarterly

$$\text{So, } T = 4 \text{ quarters, } R = \frac{20}{4} = 5\%$$

$$\begin{aligned} A &= 320000 \left(1 + \frac{5}{100} \right)^4 \\ &= 320000 \times \frac{105}{100} \times \frac{105}{100} \times \frac{105}{100} \times \frac{105}{100} \\ &= ₹388962 \end{aligned}$$

$$\text{So, CI} = ₹(388962 - 320000) = ₹68962$$

11. P = ₹ 80000; Time = 3 years; R = 4%, 5%, 10%

$$\begin{aligned}A &= 80000 \left(1 + \frac{4}{100}\right) \times \left(1 + \frac{5}{100}\right) \times \left(1 + \frac{10}{100}\right) \\&= 80000 \times \frac{104}{100} \times \frac{105}{100} \times \frac{110}{100} = ₹96096\end{aligned}$$

$$\text{C.I.} = ₹(96096 - 80000) = ₹16096$$

12. P = ₹8000; Time = 2 years; Rate = 5%, 15%

$$\begin{aligned}A &= 8000 \left(1 + \frac{5}{100}\right) \times \left(1 + \frac{15}{100}\right) \\&= 8000 \times \frac{105}{100} \times \frac{115}{100} = ₹9660\end{aligned}$$

13. P = ₹ 31250; T = 2 years 3 months or = $2\frac{1}{4}$ years; R = 16%

$$\begin{aligned}A &= 31250 \left(1 + \frac{16}{100}\right)^2 \times \left(1 + \frac{16}{100} \times \frac{1}{4}\right) \\&= 31250 \times \frac{116}{100} \times \frac{116}{100} \times \frac{104}{100} = ₹43732\end{aligned}$$

14. P = ₹ 24000; T = 9 months; R = 20p/100p or 20%

As the CI compounded quarterly

So, Time = 3 quarters; $R = \frac{20}{4} = 5\%$

$$\begin{aligned}A &= 24000 \left(1 + \frac{5}{100}\right)^3 \\&= 24000 \times \frac{105}{100} \times \frac{105}{100} \times \frac{105}{100} = ₹27783\end{aligned}$$

$$\text{C.I.} = ₹(27783 - 24000) = ₹3783$$

15. Let the principal be = ₹ 100; Time = 4 years; Rate 4%

$$\text{Interest} = \frac{100 \times 4 \times 4}{100} = ₹16$$

So, Actual principal = $\frac{100}{16} \times 1600 = ₹10000$

Now, Time = 4 years; Rate = 10%

$$\begin{aligned}A &= 10000 \left(1 + \frac{10}{100}\right)^4 \\&= 10000 \times \frac{110}{100} \times \frac{110}{100} \times \frac{110}{100} \times \frac{110}{100} \\&= ₹14641\end{aligned}$$

So,

$$\text{C.I.} = ₹(14641 - 10000) = ₹4641$$

Exercise 9C

1. Let the principal be = ₹100; Rate = 15%; Time = 2 years

$$\begin{aligned}\text{Amount} &= 100 \left(1 + \frac{15}{100}\right)^2 \\&= 100 \times \frac{115}{100} \times \frac{115}{100} = ₹132.25\end{aligned}$$

$$\text{C.I.} = ₹(132.25 - 100) = ₹32.25$$

If compound interest is ₹ 32.25 then principal be = ₹100

If compound interest is ₹ 1 then principal be = $\frac{100 \times 100}{3225}$

If compound interest is ₹ 1290 then principal be

$$= \frac{100 \times 100 \times 1290}{3225} = ₹4000$$

2. Let the principal be = ₹ 100; Time = 2 years; Rate = 5%

$$\begin{aligned}\text{Amount} &= 100 \left(1 + \frac{5}{100}\right)^2 \\&= 100 \times \frac{105}{100} \times \frac{105}{100} = ₹110.25\end{aligned}$$

Actual Principal will be = $\frac{100 \times 100}{11025} \times \frac{55125}{1} = ₹50000$

3. Principal = ₹ 10000; Time = 3 years; Rate = x%

$$\text{Amount} = 13310$$

$$\text{Amount} = P \left(1 + \frac{R}{100} \right)^T$$

$$13310 = 10000 \left(1 + \frac{R}{100} \right)^3$$

$$\frac{13310}{10000} = 10000 \left(1 + \frac{R}{100} \right)^3$$

$$\left(\frac{11}{10} \right)^3 = 10000 \left(1 + \frac{R}{100} \right)^3$$

$$\frac{11}{10} = 1 + \frac{R}{100} \Rightarrow \frac{R}{100} = \frac{11}{10} - 1 = \frac{1}{10} \Rightarrow R = 10\%$$

4. $R = x\%$; Time = $1\frac{1}{2}$ years or 3 half years; Principal = ₹ 800

$$\text{Amount} = ₹ 926.10$$

As interest compound half yearly, so rate will be = $\frac{x}{2}\%$

$$\frac{92610}{100} = 800 \left(1 + \frac{x}{2 \times 100} \right)^3$$

$$\frac{92610}{80000} = \left(1 + \frac{x}{200} \right)^3$$

$$\left(\frac{21}{20} \right)^3 = \left(1 + \frac{x}{200} \right)^3$$

$$1 + \frac{x}{200} = \frac{21}{20}$$

$$\frac{x}{200} = \frac{21}{20} - 1 = \frac{1}{20}$$

$$x = \frac{1}{20} \times 200 = 10\%$$

So, Rate = 10%

5. Time = x years; Rate = 5%; Principal = ₹800; Amount = ₹882

$$882 = 800 \left(1 + \frac{5}{100} \right)^x$$

$$\frac{882}{800} = \left(\frac{105}{100}\right)^x$$

$$\frac{441}{400} = \left(\frac{21}{20}\right)^x$$

$$\left(\frac{21}{20}\right)^3 = \left(\frac{21}{20}\right)^2$$

$$x = 2$$

6. Time = x years; Principal = ₹ 64000; Rate = 5%

Amount = ₹ 68921

As interest compounded half yearly

So time will be = 2x and Rate will be = $\frac{5}{2}\%$

$$68921 = 64000 \left(1 + \frac{5}{2 \times 100}\right)^{2x}$$

$$\frac{68921}{64000} = \left(\frac{41}{40}\right)^{2x}$$

$$\left(\frac{41}{40}\right)^3 = \left(\frac{41}{40}\right)^{2x}$$

$$2x = 3$$

$$x = \frac{3}{2} = 1\frac{1}{2} \text{ years}$$

7. Principal = ₹ 1800; Rate = 10%; Time = x years

Compound interest = ₹ 378

Amount = ₹(1800 + 378) = ₹ 2178

$$\text{Amount} = \text{Principal} \left(1 + \frac{R}{100}\right)^T$$

$$2178 = 1800 \left(1 + \frac{10}{100}\right)^x$$

$$\frac{2728}{1800} = \left(\frac{11}{10}\right)^x$$

$$\frac{121}{100} = \left(\frac{11}{10}\right)^x$$

$$\left(\frac{11}{10}\right)^2 = \left(\frac{11}{10}\right)^x$$

$$x = 2$$

So, Time = 2 years

8. Let the principal be = ₹ 100; Rate = 5%; Time = 3 years

$$\text{Simple interest} = \frac{100 \times 5 \times 3}{100} = ₹15$$

$$\text{Amount} = P \left(1 + \frac{R}{100}\right)^T$$

$$\begin{aligned} A &= 100 \left(1 + \frac{5}{100}\right)^3 \\ &= 100 \times \frac{21}{20} \times \frac{21}{20} \times \frac{21}{20} = \frac{9261}{80} \end{aligned}$$

$$\text{Compound Interest} = \frac{9261}{80} - \frac{100}{1} = \frac{9261 - 8000}{80} = \frac{1261}{80}$$

Difference between compound interest and simple interest

$$= \frac{1261}{80} - \frac{15}{1} = \frac{1261 - 1200}{80} = ₹ \frac{61}{80}$$

$$\text{Actual principal will be} = \frac{100 \times 80 \times 61}{61 \times 1} = ₹8000$$

9. Let the principal be = ₹ 100; Time = 3 years; Rate = $6\frac{2}{3} = \frac{20}{3}\%$

$$\text{Simple interest} = \frac{100 \times 3 \times 20}{3 \times 100} = ₹20$$

$$\begin{aligned} \text{Amount} &= 100 \left(1 + \frac{20}{3 \times 100}\right)^3 \\ &= 100 \times \frac{16}{15} \times \frac{16}{15} \times \frac{16}{15} = \frac{409600}{3375} \end{aligned}$$

$$\text{C.I.} = \frac{409600}{3375} - \frac{100}{1} = \frac{409600 - 337500}{3375}$$

$$= ₹ \frac{72100}{3375}$$

Difference between C.I. and S.I.

$$= \frac{72100}{3375} - \frac{20}{1} = \frac{72100 - 67500}{3375} = \frac{4600}{3375}$$

$$\text{Actual principal will be} = \frac{100 \times 3375}{4600} \times 184 = ₹13500$$

10. Amount after 2 years = ₹ 2205

Amount after 3 years = ₹2315.25

$$\text{Difference} = ₹(2315.25 - 2205) = ₹110.25$$

This difference is interest on ₹ 2205 for 1 year

$$\text{So Rate} = \frac{11025}{100} \times \frac{100}{2205} = 5\%$$

Exercise 9D

1. Present population = 80000; Time = 2 years; Rate = 7.5%

$$\begin{aligned} \text{Population after 2 years} &= 80000 \left(1 + \frac{7.5}{100}\right)^2 \\ &= 80000 \times \frac{107.5}{100} \times \frac{107.5}{100} = 92450 \end{aligned}$$

2. Present population = 40000; Rate of birth = 4%;

Rate of death = 2%

$$\text{Nett Rate of Birth} = 4 - 2 = 2\%$$

$$\begin{aligned} \text{Population after 2 years} &= 40000 \left(1 + \frac{2}{100}\right)^2 \\ &= 40000 \times \frac{51}{50} \times \frac{51}{50} = 41616 \end{aligned}$$

3. Population before 3 years = 160000; Rate of increase = 3%, 2.5%, 5%

$$\text{Present population} = 160000 \left(1 + \frac{3}{100}\right) \left(1 + \frac{2.5}{100}\right) \left(1 + \frac{5}{100}\right)$$

$$= 160000 \times \frac{103}{100} \times \frac{102.5}{100} \times \frac{105}{100} = 177366$$

4. Population before 2 years = 62500; Rate of decrease = 4%

$$\begin{aligned} \text{Present population} &= 62500 \left(1 - \frac{4}{100}\right)^2 \\ &= 62500 \times \frac{24}{25} \times \frac{24}{25} = 57600 \end{aligned}$$

5. Present value of refrigerator = ₹ 9680; Time = 2 years;

Rate of depreciation = 12%

Let the cost before 2 years be = x

So,

$$\begin{aligned} 9680 &= x \left(1 - \frac{12}{100}\right)^2 \\ 9680 &= x \times \frac{88}{100} \times \frac{88}{100} \\ x &= \frac{9680 \times 100 \times 100}{88 \times 88} = ₹12500 \end{aligned}$$

6. Cost of new car = ₹ 360000; Rate of depreciation = 10% and 20%

$$\text{Cost of car after 3 years} = 360000 \left(1 - \frac{10}{100}\right)^2 \times \left(1 - \frac{20}{100}\right)$$

$$360000 \times \frac{9}{10} \times \frac{9}{10} \times \frac{4}{5} = ₹ 233280$$

Check Your Mental Maths (I.Q.)

- | | |
|----------------------|--------------|
| 1. Compound interest | 2. Principal |
| 3. ₹ 630.50 | 4. 97.20 |
| 5. ₹ 18300 | 6. 10% |

Multiple Choice Questions (M.C.Q.)

- | | | | |
|--------|--------|--------|--------|
| 1. (b) | 2. (c) | 3. (c) | 4. (b) |
| 5. (b) | 6. (b) | | |

10 Direct and Inverse Variation

Exercise 10A

1. (i)

a	4	7	21	28
b	12	21	63	84

$$\frac{4}{12} = \frac{1}{3}, \quad \frac{7}{21} = \frac{1}{3}, \quad \frac{21}{63} = \frac{1}{3}, \quad \frac{28}{84} = \frac{1}{3}$$

as direct variation.

(ii)

a	1.25	2.5	5	7.5
b	5	10	20	30

$$\frac{1.25}{5} = .25, \quad \frac{2.5}{10} = .25, \quad \frac{5}{25} = .25, \quad \frac{7.5}{30} = .25$$

as direct vari

(iii)

a	1	2	3	4
b	2	1	6	3

$$\text{as } \frac{1}{2} \neq \frac{2}{1} \neq \frac{3}{6} \neq \frac{4}{3} \quad \text{indirect variation}$$

2. (i)

x	2.5	a	b	c	17
y	5	8	18	30	d

$$\frac{2.5}{5} = .5,$$

$$\frac{a}{8} = .5, \quad a = 4$$

$$\frac{b}{18} = .5 \quad b = 9$$

$$\frac{c}{30} = .5, \quad c = 15$$

$$\frac{17}{d} = .5 \quad d = \frac{17}{.5} = 34$$

(ii)

x	3	4	b	25	d
y	a	48	84	c	1860

$$\frac{4}{48} = \frac{1}{12}$$

$$\frac{3}{a} = \frac{1}{12}, a = 36$$

$$\frac{25}{c} = \frac{1}{12}, c = 300$$

$$\frac{b}{84} = \frac{1}{12} \quad b = \frac{84}{12} = 7$$

$$\frac{d}{1860} = \frac{1}{12} \quad d = \frac{1860}{12} = 155$$

3. If 20 men assemble, 8 machines

Men	20	—
Machine	8	12

$$\frac{20}{8} = \frac{a}{12}$$

$$\frac{20 \times 12}{8} = a$$

$$a = 30$$

So, 30 men are required.

4.

Hours	5	20
Tools	120	a

$$\frac{5}{120} = \frac{20}{a}$$

$$a = \frac{20 \times 120}{5}$$

$$a = 480$$

5.

Steps	150	360
Distance	125	b

$$\frac{150}{125} = \frac{360}{b}$$

$$b = \frac{360 \times 125}{150}$$

$$b = 300 \text{ steps it moves}$$

6.

Copies	136	c
Self length	3.4	5.1

$$\frac{136}{3.4} = \frac{c}{5.1}$$

$$c = \frac{5.1 \times 136}{3.4}$$

$c = 204$ copies we required

7.

Meter	40	a
Cost	1940	727.50

$$\frac{40}{1940} = \frac{a}{727.50}$$

$$a = \frac{4 \times 7275}{1940}$$

$$a = 15 \text{ m}$$

So, 15 m of cloth is required.

8.

Charge	520	559
Journey	200	a

$$\frac{520}{200} = \frac{559}{a}$$

$$a = \frac{559 \times 200}{520}$$

$$a = 215 \text{ km}$$

at ₹ 529 it moves 215 km

9.

Thickness	35	c
Number	12	294

$$\frac{35}{12} = \frac{c}{294}$$

$$\frac{35 \times 294}{12} = c$$

$$c = 857.5 \text{ mm}$$

So, 294 cardboard has 857.5 mm thickness

10.

Weight	150	a
expansion	2.9	17.4

$$\frac{150}{2.9} = \frac{a}{17.4}$$

$$a = \frac{150 \times 17.4}{1.9}$$

$$a = 900 \text{ gm}$$

Exercise 10B

1. (i)

x	9	18	2	12
y	8	4	30	6

$$9 : 18 = 4 : 8, \quad \frac{1}{2} = \frac{1}{2}$$

But $2 : 12 \neq 6 : 30, \quad \frac{1}{6} \neq \frac{1}{5}$ No.

(ii)

x	2	16	8	4
y	40	5	10	20

$$2:16 = \frac{1}{8} \qquad 5:40 = \frac{1}{8}$$

$$16:8 = 2 = 10:5 = 2$$

$$8:4 = 2 = 20:10 = 2 \qquad \text{Yes.}$$

(iii)

x	8	16	32	256
y	32	16	8	1

$$8:16 = \frac{1}{2}, \quad 16:32 = \frac{1}{2}, \quad 32:256 = \frac{1}{8}$$

$$16:32 = \frac{1}{2}, \quad 8:16 = \frac{1}{2} \qquad 1:8 = \frac{1}{8}$$

Yes, True

2. (i)

a	8	2	b	5	1
b	10	a	20	c	80

$$8:2 = a:10 \quad 40 = a$$

$$2:b = 20:40$$

$$\frac{2}{b} = \frac{20}{40} \Rightarrow b = 4$$

$$4:5 = c:20 \Rightarrow c = 16$$

(ii)

a	16	32	8	128
b	4	a	b	0.5

$$16:32 = a:4$$

$$32:8 = b:2$$

$$\frac{1}{2} = \frac{a}{4}$$

$$\frac{32}{8} = \frac{b}{2}$$

$$a = 2$$

$$b = 8$$

3. Total expenditure = $52 \times 1050 = ₹54600$

$$\text{New cost} = 1050 + 42 = 1092$$

Cycle	52	x
Cost	1050	1092

$$\frac{52}{x} = \frac{1092}{1050}$$

$$\frac{52 \times 1050}{1092} = x$$

$$x = 50$$

So 50 cycle is to be purchased now.

4.

Men	56	a
Days	42	14

$$\frac{56}{a} = \frac{14}{42}$$

$$a = 168$$

So, 168 men do work in 14 days.

5.

Speed	18	a
Time	30	20

$$\frac{18}{a} = \frac{20}{30}$$

$$\frac{18 \times 30}{20} = a$$

$$a = 27 \text{ km/hour}$$

6.

Person	1800	x
Days	40	24

$$\frac{1800}{x} = \frac{24}{40}$$

$$\frac{1800 \times 40}{24} = x$$

$$x = 3000$$

So, 3000 persons required to to work in 24 days

7.

Soldiers	1000	a
Days	20	25

$$\frac{1000}{a} = \frac{25}{20}$$

$$\frac{1000 \times 20}{25} = a$$

$$a = 800$$

For 800 soldiers food lasted for 25 days

So, $1000 - 800 = 200$

So, 200 soldiers will transfer.

8. 120 men has food provision for 200 days

After 5 days $(200 - 5) = 195$

As 30 died, so $= 120 - 30 = 90$ left

Men	120	90
Days	195	a

$$\frac{120}{90} = \frac{a}{195}$$

$$\frac{120 \times 195}{90} = a$$

$$a = 260$$

So, 260 days

9. 60 days for 500 students

Days left $= 60 - 12 = 48$

as $500 + 300 = 800$ students

Students	500	800
Days	48	a

$$\frac{500}{800} = \frac{a}{48}$$

$$\frac{500 \times 48}{800} = a$$

$$a = 30 \text{ days}$$

10. (i) $x = 6$ when $y = 16$ find

x	6	8
y	16	?

$$\frac{6}{8} = \frac{y}{16}$$

$$12 = y$$

(ii) $x = 10$ when $y = 30, y = 24$

x	10	?
y	30	24

$$\frac{10}{y} = \frac{24}{30}$$

$$\frac{300}{24} = a$$

$$y = 12.5$$

Check Your Mental Maths I.Q.

1. Inverse proportion
2. Direct proportion
3. Direct proportion
4. Inverse proportion

5.

Meter	5	70
Shirt	2	a

$$\frac{5}{2} = \frac{70}{a}$$

$$a = \frac{70 \times 2}{5} = 28 \text{ shirts}$$

We

6.

Days	27	a
Employee	4	12

$$\frac{27}{a} = \frac{12}{4}$$

$$a = 9 \text{ days}$$

Multiple Choice Questions (M.C.Q.)

1.

Books	20	b
Cost	280	700

$$\frac{20}{280} = \frac{b}{700}$$

$$\frac{20 \times 700}{280} = b$$

b = 50 books (c)

2. 24 boards = 60 books

40 boards = a

$$a = \frac{60 \times 40}{24} = 100 \text{ books}$$

100 books are required. (a)

3. 20 oranges = ₹70

x oranges = ₹175

$$x = \frac{20 \times 175}{70} = 50 \text{ oranges (a)}$$

4.

Cost	144	x
Men	12	24

$$\frac{144}{12} = \frac{x}{24}$$

$$144 \times 2 = x$$

$$x = ₹288 \text{ (d)}$$

5.

Student	500	600
Day	30	a

$$\frac{500}{600} = \frac{a}{30} \Rightarrow \frac{500 \times 30}{600} = a$$

a = 25 days (a)

6.

Oxen	6	9
Days	30	a

$$\frac{6}{9} = \frac{a}{30}$$

$$\frac{6 \times 30}{9} = a$$

$$a = 20 \quad (\text{b})$$

7. (c) The speed of a bus and time taken to cover a distance

11

Time and Work

1. Time taken by 1st boy = 5 days

Time taken by 2nd boy = 4 days

$$\text{Work done by 1st in 1 day} = \frac{1}{5}$$

$$\text{Work done by 2nd in 1 day} = \frac{1}{4}$$

$$\text{Total} \Rightarrow \frac{1}{5} + \frac{1}{4} = \frac{9}{20}$$

So, both can do the work in = $\frac{20}{9}$ days.

2. Time taken by A and B to do the work = 10 days

Time taken by A alone to do the work = 15 days

$$\text{Work done by A and B in 1 day} = \frac{1}{10}$$

$$\text{Work done by A in 1 day} = \frac{1}{15}$$

$$\text{Work done by B in 1 day} = \frac{1}{10} - \frac{1}{15} = \frac{3-2}{30} = \frac{1}{30}$$

So, B can do work in 30 days.

3. 'x', 'y' and 'z' work together can do piece of works = 8 hour

$$x \text{ alone can done work in 1 day} = \frac{1}{20}$$

$$y \text{ can done work in 1 day} = \frac{1}{24}$$

$$\text{So, z can done work in 1 day} = \frac{1}{8} - \frac{1}{20} - \frac{1}{24} = \frac{1}{30}$$

So, z can do work alone in 30 days

4. Together they take 8 days

$$\text{Kriti can do work in 1 day} = \frac{1}{24}$$

$$\text{Naman can do work in 1 day} = \frac{1}{20}$$

$$\text{Riya can done work in 1 day} = \frac{1}{8} - \frac{1}{20} - \frac{1}{24} = \frac{1}{30}$$

Riya can do work in 30 days.

5. Amit can do work in 1 day = $\frac{1}{12}$

$$\text{Megha can do the alone in 1 day} = \frac{1}{20}$$

$$\text{They together do} = \frac{1}{12} + \frac{1}{20} = \frac{5+3}{60} = \frac{8}{60} = \frac{2}{15}$$

$$\text{As for 3 day they work together} = 3 \times \frac{2}{15} = \frac{2}{5}$$

$$\text{Remaining work} = 1 - \frac{2}{5} = \frac{3}{5}$$

The remaining work is completed in 20 days

$$\therefore \text{Megha doing } \frac{1}{20} \text{ work} = \left(20 \times \frac{3}{5}\right) = 12 \text{ days}$$

remaining work in 12 days.

6. L and M = 10 days

M and N = 12 days

L and N = 15 days

$$\text{(L and M)'s 1 day work} = \frac{1}{10}$$

$$\text{(M and N)'s 1 day work} = \frac{1}{12}$$

$$(L \text{ and } N)\text{'s 1 day work} = \frac{1}{15}$$

Adding, we get $2(L + M + N)$'s 1 day work

$$\Rightarrow \frac{1}{10} + \frac{1}{12} + \frac{1}{15} = \frac{6+4+5}{60} = \frac{15}{60}$$

$$L + M + N\text{'s in 1 day} = \frac{15}{60} \times \frac{1}{2} = \frac{15}{120} = \frac{1}{8}$$

Together L, M, N can finish the work in 8 days.

As 1 day work =

$$\begin{aligned} & (L + M + N)\text{'s 1 day work} - (L + N)\text{'s 1 day work} \\ &= \frac{1}{8} - \frac{1}{15} = \frac{7}{120} \end{aligned}$$

M alone take $17\frac{1}{7}$ days

$$L \text{ alone 1 day} = \frac{1}{8} - \frac{1}{12} = \frac{1}{24} \text{ or 24 days}$$

$$N \text{ 1 day works} = \frac{1}{8} - \frac{1}{10} = \frac{1}{40} \text{ or 40 days to complete.}$$

7. 1 man work in 6 hours.

2nd man work in 4 hours.

$$\text{For 1 hour it work} = \frac{1}{6}$$

$$\text{For 2 hour} = \frac{1}{3}$$

$$\text{And both also} = \frac{1}{6} + \frac{1}{4} = \frac{2+3}{12} = \frac{5}{12}$$

$$\text{Remaining work} = 1 - \frac{1}{3} = \frac{2}{3}$$

$$\text{So } \frac{2}{3} \text{ work} = \frac{3}{2} \times \frac{5}{12} = \frac{5}{8}$$

$$\text{So remaining work will be completed in} = \frac{8}{5} = 1\frac{3}{5} \text{ days}$$

8. Three men P, Q, R

P work = 9 hour

Q work = 18 hour

R work = 12 hour

$$\text{Their together work for 1 hour} = \frac{1}{9} + \frac{1}{18} + \frac{1}{12} = \frac{1}{4}$$

It took 4 hours.

9. A, B and C together do work in 10 days

A alone can do it in 40 days

B alone can do it = 30 days

$$\begin{aligned}\text{For C} &= \frac{1}{10} - \frac{1}{40} - \frac{1}{30} = \frac{12 - 3 - 4}{120} \\ &= \frac{5}{120} = \frac{1}{24}\end{aligned}$$

C can do it in 24 days.

10. By one tap in 4 hour

Another tap in 3 hour

$$\text{Both opened then} = \frac{1}{4} + \frac{1}{3} = \frac{7}{12}$$

Or, by $\frac{12}{7}$ hour or $1\frac{5}{7}$ hour

11. Work done by A tank in 1 hour = $\frac{1}{6}$

Work done by B tank in 1 hour = $\frac{1}{8}$

$$\text{Both can do} = \frac{1}{6} + \frac{1}{8} = \frac{14}{48} = \frac{7}{24}$$

$$\text{But in 2 hour A and B can do} = \frac{2 \times 7}{24} = \frac{7}{12}$$

$$\text{Remaining} = 1 - \frac{7}{12} = \frac{5}{12}$$

$$\text{By B} = 8 \times \frac{5}{12} = \frac{10}{3} = 3\frac{1}{3} \text{ hours}$$

12. Tank is filled at the rate of = 6 hour

$$\text{In 1 hour} = \frac{1}{6}$$

Completed by = 7 hour

$$\text{In 1 hour} = \frac{1}{7}$$

$$\text{Then overall work in 1 hour will be} = \frac{1}{6} - \frac{1}{7} = \frac{1}{42} \text{ hours}$$

So in 42 hour it will complete.

13. Time taken by tap 1st to fill = 12 min

Time taken by 2nd to fill = 15 min

Time taken by 3rd to empty = 10 min

$$\begin{aligned} \text{Thus in 1 minute the overall work will be} &= \left(\frac{1}{12} + \frac{1}{15} - \frac{1}{10} \right) \\ &= \left(\frac{5+4-6}{60} \right) = \frac{1}{20} \end{aligned}$$

So 20 minutes will required.

14. Work done by tap A in 1 hour = $\frac{1}{10}$

$$\text{By tap B in 1 hour} = \frac{1}{15}$$

$$\text{Both in 1 hour} = \frac{1}{10} + \frac{1}{15} = \frac{3+2}{30} = \frac{1}{6}$$

$$\text{In 4 hour} = \frac{4}{6} = \frac{2}{3}$$

$$\text{Remaining} = 1 - \frac{2}{3} = \frac{1}{3}$$

$$\text{By A} = 10 \times \frac{1}{3} = \frac{10}{3}$$

$$3\frac{1}{3} \text{ hour it take}$$

15. Work done by tap in 1 hour = $\frac{1}{4}$

$$\text{Work done by pipe in 1 hour} = \frac{1}{6}$$

$$\text{Work done by both in 1 hour} = \frac{1}{4} - \frac{1}{6} = \frac{3-2}{12} = \frac{1}{12}$$

So, time taken to fill the tank by these two = 12 hours

Check Your Mental Math I.Q.

1. Less.

2. Negative

$$3. \text{ In 1 day work done} = \frac{1}{20}$$

$$\text{In 4 days} = \frac{4}{20} = \frac{1}{5}$$

$$4. \text{ Together} = \frac{1}{15} + \frac{1}{10} = \frac{2+3}{30} = \frac{5}{30} = \frac{1}{6}$$

So both can work in 6 hour.

$$5. \text{ A can do} = \frac{1}{8} - \frac{1}{10} = \frac{5-4}{40} = \frac{1}{40} \text{ in 40 days}$$

$$6. \frac{1}{12} + \frac{1}{16} - \frac{1}{8} = \frac{4+3-6}{48} = \frac{1}{48}$$

Or in 48 hour it can empty the whole tank.

Multiple Choice Questions (M.C.Q.)

1. Complete work in 12 days

$$1 \text{ day} = \frac{1}{12}$$

$$\text{In 9 day} = \frac{9}{12} = \frac{3}{4} \quad (\text{b})$$

$$2. \text{ Ruchi alone can do} = \frac{1}{20} - \frac{1}{30} = \frac{3-2}{60} = \frac{1}{60} \quad 60 \text{ days } (\text{b})$$

$$3. \text{ All three} = \frac{2}{3} + \frac{1}{2} + \frac{1}{3} = \frac{4+3+2}{6} = \frac{9}{6}$$

$$= \frac{3}{2} \text{ hour} \Rightarrow \frac{2}{3} \text{ hours } (\text{a})$$

4. 60 men work in 8 hours, build shed in 30 days

If there were 120 men work for 6 hour then same work is to be done in

$$= \frac{60 \times 8 \times 30}{120 \times 6} = 20 \text{ days } (\text{b})$$

$$5. \frac{1}{12} - \frac{1}{18} = \frac{3-2}{36} = \frac{1}{36} = 36 \text{ hours } (\text{b})$$

Exercise 12

1. (a) 4, PQ, QR; QR, RS; RS, SP; SP, PQ
 (b) 2: PQ, SR; PS, QR
 (c) 2; $\angle P, \angle Q; \angle Q, \angle R; \angle R, \angle S; \angle S, \angle P$
 (d) 2; $\angle P, \angle R; \angle Q, \angle S$

2. Let the two equal angles be x

$$\text{So, } 60 + 100 + x + x = 360^\circ$$

$$2x = 200$$

$$x = 100^\circ$$

Angle are 100, 100

3. Let the ratio be x

$$\text{Then } 2x + 3x + 5x + 8x = 360$$

$$18x = 360$$

$$x = 20$$

So, angles are $40^\circ, 60^\circ, 100^\circ, 160^\circ$

4. (i) $120 + 50 + 130 + x = 360^\circ$

$$x = 360^\circ - 300$$

$$x = 60^\circ$$

- (ii) $72 + 25 + 30 + x = 360^\circ$

$$x = 233^\circ$$

- (iii) $180^\circ - 120^\circ = x$

$$60^\circ = x$$

$$y = 180 - 80 = 100^\circ$$

$$z = 180 - 60 = 120^\circ$$

$$80^\circ + 120^\circ + 60^\circ + (180 - w) = 360^\circ$$

$$w = 80^\circ$$

So, $x = 60^\circ, y = 120^\circ, z = 120^\circ, w = 80^\circ$

5. Let the angle be $= x$

$$4x = 360^\circ$$

$$x = 90^\circ$$

$$6. \quad 130 + 65 + 65 + x = 360^\circ$$

$$x = 100^\circ$$

$$7. \quad \angle A + \angle B + 100 + 50 = 360^\circ$$

$$\angle A + \angle B = 360^\circ - 150 = 210$$

$$\frac{\angle A + \angle B}{2} = 105^\circ = \frac{210}{2} = 105^\circ$$

$$\text{So,} \quad \angle APB = 180^\circ - \left(\frac{\angle A + \angle B}{2} \right)$$

$$\angle APB = 180^\circ - 105^\circ = 75^\circ$$

Check Your Mental Math I.Q.

1. Let the angle be x

$$4x = 360^\circ$$

$$x = 90^\circ$$

2. Let the ratio be x the

$$\text{then } 3x + 5x + 7x + 9x = 24x = 360^\circ$$

$$x = 15^\circ$$

So the angles are $= 45^\circ, 75^\circ, 105^\circ, 135^\circ$

3. Let the ratio be x

$$4x + 6x + 3x + 100 = 360^\circ$$

$$13x = 260^\circ$$

$$x = 20^\circ$$

$$4 \times 20 = 80; \quad 6 \times 20 = 120 \quad 3 \times 20 = 60$$

4. Let the equal angle be $x =$ then

$$3x + 120^\circ = 360^\circ$$

$$3x = 240^\circ$$

$$x = 80^\circ$$

5. $2x^\circ + 10, 3(x + 2)^\circ, (7x - 10)^\circ, 6(x + 5)^\circ$

$$2x + 10 + 3x + 6 + 7x - 10 + 6x + 30 = 360^\circ$$

$$18x = 360 - 36 = 324$$

$$x = 324 \div 18 = 18$$

$$2 \times 18 + 10 = 46^\circ$$

$$3(18 + 2) = 60^\circ$$

$$(7 \times 18 - 10) = 116^\circ$$

$$6(x + 5) = 6(18 + 5)$$

$$= 6 \times 23 = 138^\circ$$

Multiple Choice Questions (M.C.Q.)

- (b) 360° 2. (b) 60° 3. (b)
- (a) $2x + 3x + 4x + 6x = 360^\circ$, then $x = 24$. So angles are 48, 72, 96, 144
- $5x + x = 360^\circ$
 $x = 60^\circ$ (b)

13

Special Types of Quadrilaterals

Exercise 13A

- A quadrilateral which has exactly one pair of parallel sides, in an isosceles trapezium non parallel sides are equal.
- $60 + \angle B = 180^\circ$
 $\angle B = 120^\circ$
 $\angle A = \angle C$
 $\angle C = 60^\circ$
 $\angle B = \angle D$
 $\angle D = 120^\circ$
- If two angles are equal then
 $x + x = 180^\circ$
 $2x = 180^\circ$
 $x = 90^\circ$
- $\angle y = 180 - 100$
 $= 80^\circ$
 $\angle x = \angle 100^\circ$
 $\angle y = \angle z$ *i.e.* $\angle z = 80^\circ$
- $\angle c = \angle A = 75^\circ$
 $\angle CDB = 180^\circ - 75^\circ - 60^\circ = 45^\circ$
 $\angle ADB = \angle CBD = 60^\circ$

$$6. \quad 25+25+x+x = 150^\circ$$

$$2x = 100$$

$$x = 50^\circ$$

So, the sides are 25, 50, 25, 50

7. Let the ratio of x

$$x + 3x = 180^\circ$$

$$4x = 180^\circ$$

$$x = 45^\circ$$

or $3x = 45 \times 3 = 135^\circ$

Angles are $= 45^\circ, 135^\circ, 45^\circ, 135^\circ$

$$8. \quad x + x + 30 + x + x + 30 = 180$$

$$4x = 180 - 60$$

$$4x = 120$$

$$x = 30; \text{ So sides are } 30, 60, 30, 60$$

$$9. \quad \angle 40 + \angle C = 70^\circ$$

$$\angle C = 30^\circ$$

$$\angle a + 70^\circ = 180^\circ$$

$$\angle a = 110^\circ$$

In WYX

$$\angle C + \angle B =$$

$$\angle B = 70 - 30^\circ$$

$$\angle B = 40^\circ$$

Exercise 13B

$$1. \quad a = 5 \text{ cm} \quad b = 12 \text{ cm}$$

$$c^2 = 5^2 + 12^2 = 169; c = 13 \text{ cm}$$

$$2. \quad BO = \frac{1}{2} BD$$

i.e.

$$BO = 8$$

$$AO = \sqrt{(10)^2 - (8)^2}$$

$$AO = \sqrt{100 - 64}$$

$$AO = \sqrt{36}$$

$$AO = 6$$

$$AO = \frac{1}{2} \times AC$$

$$6 \times 2 = AC$$

$$AC = 12 \text{ cm}$$

$$3. \quad \begin{aligned} \angle DBC &= 90 - \angle BAC \\ &= 90 - 28 = 62^\circ \end{aligned}$$

$$4. \quad \begin{aligned} \angle ABD &= \frac{1}{2} \angle AC \\ \angle ABD &= \frac{1}{2} \times 126 = 63 \\ \angle ACD &= 90 - 63 = 27 \end{aligned}$$

$$5. \quad \angle DCA = \frac{90}{2} = 45^\circ$$

$$6. \quad \begin{aligned} \text{(i)} \quad \angle DAO &= \angle CBO \\ \angle DAO &= 90 - 21^\circ = 69^\circ \\ 69^\circ &= x^\circ \end{aligned}$$

$$\text{(ii)} \quad \angle b = \frac{180 - 102}{2} = \frac{78}{2} = 39^\circ$$

$$\angle a + \angle b = 90^\circ$$

$$\angle a = 90 - b = 90^\circ - 39^\circ = 51^\circ$$

$$\text{(iii)} \quad \begin{aligned} 180 - 140 &= 2x \\ 20^\circ &= x \end{aligned}$$

$$7. \quad \begin{aligned} \angle A = \angle C &= 60^\circ \\ \angle B = \angle D &= 120^\circ \end{aligned} \quad 8. \quad \angle ODA = \frac{180 - 60}{2} = \frac{120}{2} = 60^\circ$$

Check Your Mental Math I.Q.

1. Let the ratio be x

$$5x + 3x + 3x + 5x = 360^\circ$$

$$16x = 360^\circ$$

$$x = 22.5^\circ$$

$$3x = 3 \times 22.5 = 67.5$$

$$5x = 22.5 \times 5 = 112.5$$

$$2. \quad 3x + 5x + 3x + 5x = 48$$

$$16x = 48 \Rightarrow x = 3$$

16

Area of a Trapezium and a Polygon

1. Area of Trapezium =

$$= \frac{1}{2} \times (15 + 8) \times 10$$
$$= 23 \times 5 = 115 \text{cm}^2$$

2. $\frac{1}{2} \times (40 + 22) \times 12$

Area of garden = $\frac{1}{2} \times (62) \times 12$

$$= 62 \times 6 = 372 \text{m}^2$$

3. $240 = \frac{1}{2} \times (25 + x) \times 10$

$$\frac{2 \times 240}{10} = 25 + x$$
$$48 - 25 = x$$
$$x = 23 \text{cm}$$

4. $500 = \frac{1}{2} \times (50) \times h$

$$\frac{1000}{50} = h$$
$$h = 20 \text{ cm}$$

5. $210 = \frac{1}{2} (x + 2x) \times 14$

$$\frac{210 \times 2}{14} = 3x$$
$$x = 10 \text{ and } 3x = 30$$

6. The length of the parallel sides of a trapezium ratio be x as 5x, 6x

$$330 = \frac{1}{2} \times (5x + 6x) \times 12$$

$$\frac{660}{12 \times 11} = x$$

$$x = 5$$

So, sides are $5 \times 5 = 25$

$$6 \times 5 = 30$$

7.
$$192 = \frac{1}{2} \times (8 + x) \times 16$$

$$\frac{192 \times 2}{16} = x + 8$$

$$x = 24 - 8$$

$$x = 16$$

So, Other side is 16

8. Let one is x then other is $7 + x$

$$138 = \frac{1}{2} \times (x + 7 + x) \times 12$$

$$\frac{138 \times 2}{12} = 7 + 2x$$

$$16 = 2x$$

$$8 = x$$

So one is 8 and the other is $8 + 7 = 15$

10.
$$180 = \frac{1}{2} \times (x + x + 6) \times 9$$

$$\frac{180 \times 2}{9} = 2x + 6$$

$$40 - 6 = 2x$$

$$\frac{34}{2} = 2x$$

$$x = 17$$

17, $17 + 6 = 23$

11.
$$\text{Area} = \frac{1}{2} \times (10 + 25) \times 15$$

$$= \frac{35 \times 1}{2} \times 15$$

$$\text{Cost} = \frac{35 \times 1}{2} \times 15 \times 4$$

$$= ₹ 1050$$

12. Perimeter of Trapezium = 52 cm

Sum of unparallel sides = 10 + 10 = 20

Sum of parallel sides = 52 - 20 = 32 cm

$$\begin{aligned}\text{So, Area of Trapezium} &= \frac{1}{2} \times (32) \times 8 \\ &= 128 \text{ cm}^2\end{aligned}$$

Exercise 16B

1. Area of polygon A = $\frac{1}{2} \times \text{perimeter} \times \text{in radius}$

$$\text{Perimeter} = na$$

$$\text{radius} = r$$

$$A = \frac{1}{2} nar$$

$$\begin{aligned}A &= \frac{1}{2} \times 5 \times 10 \times 9 \quad \{\text{as pentagon so } n = 5\} \\ &= 225 \text{ cm}^2\end{aligned}$$

2.
$$\begin{aligned}A &= \frac{1}{2} \times na \times \sqrt{R^2 - \frac{a^2}{4}} \\ &= \frac{1}{2} \times 7 \times 8 \times \sqrt{(6)^2 - \frac{(8)^2}{4}} \\ &= 28\sqrt{36 - 16} \\ &= 28 \times \sqrt{20} \\ &= 125.22 \text{ cm}^2\end{aligned}$$

3.
$$\begin{aligned}A &= \frac{1}{2} \times na \times \sqrt{R^2 - \frac{a^2}{4}} \\ &= \frac{1}{2} \times 9 \times 6 \times \sqrt{(4)^2 - \frac{(6)^2}{4}} \\ &= 9 \times 3 \times \sqrt{16 - 9} = 27\sqrt{7} = 71.435 \text{ cm}^2\end{aligned}$$

4. Area of regular hexagon

$$= \frac{3\sqrt{3}}{2} (\text{side})^2 \text{ sq unit}$$

$$= \frac{3\sqrt{3}}{2} \times (7)^2 = \frac{3\sqrt{3}}{2} \times 49 = 127.302 \text{ cm}^2$$

$$(b) \frac{3\sqrt{3}}{2} \times (9)^2 = \frac{3\sqrt{3}}{2} \times 81 = 210.438 \text{ cm}^2$$

5. Area of regular octagon = $2a^2(1 + \sqrt{2})$

$$= 2 \times (8)^2(1 + \sqrt{2})$$

$$= 2 \times 64(1 + \sqrt{2}) = 308.992$$

$$(b) = 2 \times (5)^2(1 + \sqrt{2})$$

$$= 2 \times 25(1 + \sqrt{2})$$

$$= 120.7 \text{ cm}^2$$

6. (a) Area of $\triangle AFB = \left(\frac{1}{2} \times B \times h\right) = \frac{1}{2} \times 20 \times 10$

$$= 10 \times 10 = 100 \text{ cm}^2$$

$$\text{Area of square} = (s)^2 = (20)^2 = 400 \text{ cm}^2$$

Area of $\triangle ECD =$

$$OD^2 = (20)^2 - (10)^2$$

$$OD^2 = (400 - 100)$$

$$OD = 10\sqrt{3}$$

$$= \left(\frac{1}{2} \times 20 \times 10\sqrt{3}\right) = 100\sqrt{3} \text{ cm}^2$$

$$\text{Total Area} = 100\sqrt{3} + 100 + 400$$

$$= 673.20 \text{ m}^2$$

$$(b) \quad PD = \sqrt{(8)^2 - (4)^2} \qquad \sqrt{(12)^2 - (4)^2}$$

$$= \sqrt{64 - 16} \qquad \sqrt{144 - 16}$$

$$= \sqrt{48} \qquad \sqrt{128}$$

$$= 4\sqrt{3}$$

$$\text{Area of FDA} = \left(\frac{1}{2} \times 4 \times 4\sqrt{3}\right) + \left(\frac{1}{2} \times 4 \times \sqrt{128}\right)$$

$$= 8\sqrt{3} + 2\sqrt{128}$$

$$\text{DQ} = \sqrt{(12)^2 - (5)^2} \quad \sqrt{(12)^2 - (5)^2}$$

$$= \sqrt{144 - 25}$$

$$= \sqrt{119}$$

$$\text{Area } \nabla \text{AB} = \left(\frac{1}{2} \times 5 \times \sqrt{119}\right) \times 2$$

$$= 5\sqrt{119}$$

$$\text{DR} = \sqrt{(12)^2 - (5)^2} = \sqrt{119}$$

$$= \sqrt{(10)^2 - (5)^2} = \sqrt{100 - 25} = \sqrt{75}$$

$$\text{So area of DBC} = \left(\frac{1}{2} \times \sqrt{119} \times 5\right) + \left(\frac{1}{2} \times \sqrt{75} \times 5\right)$$

$$= \frac{5\sqrt{119}}{2} + \frac{5\sqrt{75}}{2}$$

$$\text{Total area} = 8\sqrt{3} + 2\sqrt{128} + 5\sqrt{119} + \frac{5\sqrt{119}}{2} + \frac{5\sqrt{75}}{2}$$

$$= 134.29\text{cm}^2$$

$$7. \text{MO} = \sqrt[2]{(13^2 - 5^2)} = \sqrt[2]{(169 - 25)} = 2 \times 12 = 24\text{m}$$

$$\text{Area of figure} = 2\left(\frac{1}{2} \times 24 \times 5\right) + 13 \times 24$$

$$= 120 + 312 = 432 \text{ sqm}$$

8. Area of pentagon ABCDE

Area of EHD + Area of trapezium HDCF + Area of Δ CFB + area of Δ AEB.

$$\frac{1}{2} \times \overset{\text{As}}{(EH \times HD)} + (DH + CF) \times HF + \frac{1}{2} \times CP \times FB + \frac{1}{2} (EB \times AG)$$

$$EH = BE - BH = 120 - 80 = 40$$

$$HF = BH - BF = 80 - 20 = 60$$

$$\begin{aligned} & \frac{1}{2} \times (40 \times 25) + \frac{1}{2} (25 \times 30) \times 60 + \frac{1}{2} \times 30 \times 20 + \frac{1}{2} (120 \times 70) \\ & = 6650\text{m}^2 \end{aligned}$$

9. Area of ABCDEFG =

Area of AGL + Area of Trapezium GLFN + Area of GNE +
Area of Trapezium ABCU + Area of Irpism UCDN + Area
of ODE

$$LN = AO - AL = 110 - 30 = 80, NE = AE - AO = 25$$

$$\begin{aligned} & \frac{1}{2} \times AL \times LG + \frac{1}{2} (GL + FN) LN + \frac{1}{2} \times (FN) \times (NE) \\ & + \frac{1}{2} \times AU \times (AB + UC) + \frac{1}{2} \times MO \times (MC + OD) + \frac{1}{2} \times (OE) \times (a) \\ & \frac{1}{2} \times 30 \times 40 + \frac{1}{2} (40 + 42) \times 80 + \frac{1}{2} \times 42 \times 25 + \\ & \frac{1}{2} \times 90 \times (36 + 54) + \frac{1}{2} \times (54 + 46) \times 20 + \frac{1}{2} \times 25 \times 40 \\ & = 93730\text{m}^2 \end{aligned}$$

Check Your Mental Math I.Q.

1. Area = $\frac{1}{2} (9 + 19) \times 11 = 154\text{m}^2$

2. $340 = \frac{1}{2} \times 8 \times (8 + x)$

$$\frac{340 \times 2}{8} = 8 + x$$

$$85 = 8 + x$$

$$x = 77$$

3. $22 = \frac{1}{2} \times 11 \times h$

$$\frac{22 \times 2}{11} = h$$

$$h = 4\text{ cm}$$

4. Let the ratio be x

So, the sides are = 3x, 5x

$$240 = \frac{1}{2} \times (3x + 5x) \times 12$$

$$\frac{240 \times 2}{12 \times 8} = x$$

$$x = 5$$

$$3 \times 5 = 15 \text{ cm}; 5 \times 5 = 25 \text{ cm}$$

5. Area of square = (s)²

Area of rectangle = (l × b)

Perimeter of square = 4 × s

Perimeter of rectangle = 2(l + b)

$$\frac{(s)^2}{15 \times 9} = \frac{3}{5}$$

$$(s)^2 = 27 \times 3$$

$$S = \sqrt{81}$$

$$S = 9$$

$$\text{Perimeter of square} = 4 \times 9 = 36 \text{ cm}$$

Multiple Choice Question (M.C.Q.)

1. $A = \frac{1}{2} \times 10 \times 7 = 35 \text{ cm}^2$ (c)

2. $36 = \frac{1}{2} \times 18 \times D_1$

$$4 = D_1$$

$$\text{Perimeter} = 4 \times 4 = 16 \text{ cm (a)}$$

3. $475 = \frac{1}{2} \times (2x + 3x) \times 10$

$$\frac{475 \times 2}{5 \times 10} = x$$

$$x = 19$$

$$\text{Larger side} = 3 \times 19 = 57 \text{ cm (b)}$$

4. $A = \frac{1}{2} \times (80 + 60) \times 20 = 1400 \text{ cm}^2$ (a)

$$\begin{aligned}
 1. \text{ C.S.A. of cylinder} &= 2 \times \pi \times r \times h \\
 &= 2 \times \frac{22}{7} \times 7 \times 15 \\
 &= 660 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{T.S.A. of cylinder} &= 2 \pi r (h + r) \\
 &= 2 \times \frac{22}{7} \times 7 (15 + 7) \\
 &= 968 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 2. \text{ C.S.A. of cylinder} &= 2 \times \pi r h \\
 88 &= 2 \times \frac{22}{7} \times r \times 14
 \end{aligned}$$

$$\frac{88 \times 7}{22 \times 14} = 2r$$

$$D = 2 \text{ cm} \quad \{ \therefore D = 2r \}$$

$$\begin{aligned}
 3. \quad \text{Volume} &= \pi r^2 h \\
 &= \frac{22}{7} \times 3.5 \times 3.5 \times 8 \\
 &= 308 \text{ cm}^3
 \end{aligned}$$

$$\begin{aligned}
 4. \quad \text{Volume} &= \pi r^2 h \\
 3080 &= \frac{22}{7} \times r^2 \times 20 \\
 \frac{3080 \times 7}{20 \times 22} &= r^2 \\
 r^2 &= 49; \Rightarrow r = 7 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 5. \quad \text{Volume} &= \pi r^2 h \\
 \text{Given } D = 14 \text{ m; So radius} &= \frac{14}{2} = 7 \text{ m} \\
 2156 &= \frac{22}{7} \times (7)^2 \times h
 \end{aligned}$$

$$\frac{2156}{7 \times 22} = h$$

$$h = 14\text{m}$$

$$\begin{aligned} 6. \quad \text{C.S. of roller} &= 2\pi rh \\ &= 2 \times \frac{22}{7} \times 60 \times 84 \\ &= 31680 \text{ cm}^2 \end{aligned}$$

1000 revolutions then area

$$\begin{aligned} &= 31680 \times 1000 = 31680000 \text{ cm}^2 \\ &= 3168 \text{ m}^2 \end{aligned}$$

$$7. \text{ Original cylinder volume} = \pi r^2 h$$

$$\text{Reduced cylinder volume} = \pi \times \left(\frac{r}{2}\right)^2 h$$

$$\text{Ratio} = \frac{\pi \times r^2 \times h}{4(\pi \times r^2 \times h)} \quad \text{i.e. } \frac{\text{reduce}}{\text{original}}$$

$$= 1 : 4, \text{ Ans}$$

$$\begin{aligned} 8. \quad \text{1 pillar C.S.A.} &= 2\pi \times r \times h \\ &= 2 \times \frac{22}{7} \times \frac{0.48}{2} \times 7 \end{aligned}$$

$$= 22 \times 0.48 \text{ m}^2$$

$$\text{1 pillar cost of painting} = 22 \times 0.48 \times 5$$

$$\text{12 pillar cost of painting} = 22 \times 0.48 \times 5 \times 12$$

$$\text{i.e.} \quad = ₹ 633.60$$

$$9. \quad h = 22.5\text{m}; d = 7\text{m or } r = \frac{7}{2}$$

$$\text{Inner C.S.A.} = 2\pi \times r \times h$$

$$\text{Area dug} = \text{Volume} = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 22.5$$

$$= 866.25 \text{ cm}^3$$

$$\text{C.S.A.} = 2 \times \frac{22}{7} \times \frac{7}{2} \times 22.5$$

$$\text{C.S.A. of} = 22 \times 22.5 \text{ m}^2 = 495 \text{ m}^2$$

$$\text{Cost of plastering} = 3 \times 495 = ₹1485$$

10. Volume of 1 coin = $\pi r^2 h$

$$= \frac{22}{7} \times \frac{1.5}{2} \times \frac{1.5}{2} \times 0.2 \text{ cm}^3$$

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{4.5}{2} \times \frac{4.5}{2} \times 10$$

$$\text{No. of Coins} = \frac{\text{Volume of cylinder}}{\text{Volume of cone}}$$

$$= \frac{22 / 7 \times 4.5 \times 4.5 \times 10}{22 / 7 \times 1.5 \times 1.5 \times 0.2}$$

$$= 450 \text{ coins are required}$$

11. Volume of cylinder = $\pi r^2 h$

$$= \frac{22}{7} \times \frac{20}{2} \times \frac{20}{2} \times 9$$

$$= 2828.60 \text{ cm}^3$$

$$\text{Volume of cube} = (8 \text{ cm})^3$$

$$= 512 \text{ cm}^3$$

$$\text{height} = \frac{\text{Volume of cylinder}}{\text{Volume of cube}}$$

$$= \frac{2828.6}{512}$$

$$= 5.52 \text{ cm}$$

12. C.S.A. of pipe = $2 \times \frac{22}{7} \times \frac{70}{2} \times 21 \times \frac{1}{100}$

$$= 46.2 \text{ cm}^2$$

$$\text{Cost} = 46.2 \times 10 = ₹462$$

13. as height is same

Volume of hollow cylinder = volume of solid cylinder

$$\pi(R^2 - r^2) \times h = \pi \times R_1 \times h$$

$$\frac{\pi(R^2 - r^2) \times h}{\pi \times h} = R_1^2$$

$$R^2 = (20)^2 - (15)^2$$

$$R_1^2 = 175$$

$$R_1 = 13.3 \text{ cm approx.}$$

So radius of solid cylinder is 13.3 cm

14. (i) Volume of roof = $l \times b \times h$

$$= 70 \times 44 \times \frac{1}{10}$$

$$= 308 \text{ cm}^3$$

(ii) Volume of tank = $\pi r^2 h$

$$= \frac{22}{7} \times 14 \times 14 \times h$$

$$= 61.6 h \text{ m}^3$$

$$\text{Rise in volume} = \frac{308}{61.6} = 5 \text{ m}$$

15. $2\pi r = 22$ or $r = \frac{22 \times 7}{22 \times 2}$

$$r = \frac{7}{2}$$

Now volume of cylinder = $\pi r^2 h$

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 12$$

$$= 462 \text{ cm}^3$$

Check Your Mental Math I.Q.

1. Volume of cuboid = $6 \times 3 \times 4 = 72 \text{ cm}^3$

2. $24 = 4 \times 3 \times h$

$$\frac{24}{4 \times 3} = h$$

$$h = 2 \text{ m}$$

3. Volume of 5 small cubes = volume of cube

Let edge be x then

$$x^3 = \frac{135}{5}$$

$$x^3 = 27$$

$$x = 3$$

$$\begin{aligned} 4. \text{ No of cubical block} &= \frac{\text{Volume of block}}{\text{Volume of small block}} \\ &= \frac{(6)^3}{(2)^3} \\ &= \frac{6 \times 6 \times 6}{2 \times 2 \times 2} \end{aligned}$$

27 cubical block.

5. Volume of cylinder = volume of 2nd cylinder

$$\pi \times R^2 \times H = \pi \times r^2 \times h$$

$$\frac{H}{h} = \frac{\pi \times (r)^2}{\pi \times (R)^2}$$

$$\frac{H}{h} = \left(\frac{3}{5}\right)^2$$

$$\frac{H}{h} = \frac{9}{25}$$

$$\text{So, } \frac{h}{H} = \frac{25}{9} \text{ or } 25 : 9$$

Multiple Choice Questions (M.C.Q.)

1. (c)

2.

$$\text{S.A.} = 486$$

$$6a^2 = 486$$

$$a^2 = 81$$

$$a = 9 \text{ (b)}$$

3.

$$\text{S.A.} = 6a^2$$

$$= 6 \times (5)^2$$

$$= 150 \text{ (b)}$$

4.

$$\text{No. of cubes} = \frac{\text{Volume of block}}{\text{Volume of small block}}$$

$$= \frac{(8)^3}{(2)^3}$$

$$= (4)^3 = 64 \quad (\text{a})$$

5. Length = $4 \times 3 = 12\text{m}$
 Breadth = 4 cm
 S.A. = $4(12 \times 4) + 2(4 \times 4)$
 $192 + 32 = 224\text{ cm}^2$ (b)

6. as of $= \frac{\pi r^2 \times h}{\pi R_2^2 \times H}$
- $$= \left(\frac{r}{R}\right)^2 \left(\frac{h}{H}\right)$$
- $$= \left(\frac{2}{3}\right)^2 \left(\frac{5}{3}\right)$$
- $$= \frac{4}{9} \times \frac{5}{3} = \frac{20}{27} \quad (\text{c})$$

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Data Handling

Check Your Mental Math I.Q.

- | | |
|-------------------|-------------|
| 1. data | 2. raw data |
| 3. grouped | 4. range |
| 5. class interval | |

Multiple Choice Questions (M.C.Q.)

- | | |
|-----------|-------------|
| 1. (a) 15 | 2. (b) 30 |
| 3. (c) 5 | 4. (d) 32.5 |
| 5. (c) 6 | |

19

Graphical Representation of Data

Exercise 19A

4. (a) It depicts the height of 20 students of a class.
(b) 155 cm (c) 11 students
(d) 3 students
5. (a) 12 (b) 13 matches
(c) 8 matches (d) 4 matches
6. (a) 30 - 35 (b) 6
(c) 5
(d) 20 - 25; 25 - 30; 30 - 35; 35 - 40; 40 - 45; 45 - 50

Exercise 19B

3. (a) In steel = $\frac{540000 \times 45}{360} = ₹ 67500$
Cement = $\frac{540000 \times 75}{360} = ₹ 112500$
- (b) Timber = $\frac{540000 \times 50}{360} = 135000$
Bricks = $\frac{540000 \times 50}{360} = 75000$
Difference = $135000 - 75000 = 60000$
4. (a) Wheat = $\frac{81000 \times 120}{360} = 27000$ tonnes
(b) Sugar = $\frac{81000 \times 100}{360} = 22500$ tonnes
(c) Rice = $\frac{81000 \times 60}{360} = 13500$ tonnes
(d) Grain = $\frac{81000 \times 50}{360} = 11250$ tonnes
(e) Maiza = $\frac{81000 \times 30}{360} = 6750$ tonnes

Check Your Menatl Math I.Q.

1. Histogram
2. One dimensional
3. pie chart
4. 360°

Multiple Choice Questions

1. (b) $\frac{24 \times 60}{360} = 4$
2. (b) $\frac{60 \times 60}{360} = 10$
3. (b) $\frac{36 \times 60}{360} = 6$
4. (b) $\frac{360 \times 30}{360} = \frac{210 \times 60}{360} = \frac{30}{210}$
 $\frac{1}{7} = 1:7$

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Probability

1. Total number of event = 6
 - (a) an even number face favourable = 2, 4, 6 i.e. 3
Probability = $\frac{3}{6} = \frac{1}{2}$
 - (b) a multiple of 3
favourable = 3, 6 i.e. 2
Probability = $\frac{2}{6} = \frac{1}{3}$
 - (c) an odd number favourable = 1, 3, 5, i.e. 3
Probability = $\frac{3}{6} = \frac{1}{2}$
 - (d) a number between 3 and 6
favourable = 4, 5 i.e. 2
Probability = $\frac{2}{6} = \frac{1}{3}$
2. Total number of events = $2^3 = 8$

(a) All head

Favourable = 1

$$\text{Probability} = \frac{1}{8}$$

HHH

(b) two head

favourable = 3

$$\text{Probability} = \frac{3}{8}$$

HTH

HTT

(c) one head

Favourable = 3

$$\text{Probability} = \frac{3}{8}$$

THH

TTH

(d) at least two heads = 4

Favourable = 4

$$\text{Probability} = \frac{4}{8} = \frac{1}{2}$$

THT

TTT

3. Total number of possibility = 25

Favourable event = 1, 3, 5, 7, 11, 13, 17, 19, 23 = 9

$$\text{Probability} = \frac{9}{25}$$

4. Total number of events = 52

(a) an ace

Favourable event = 4

$$\text{Probability} = \frac{4}{52} = \frac{1}{13}$$

(b) Black

Favourable event = 26

$$\text{Probability} = \frac{26}{52} = \frac{1}{2}$$

(c) either black card or king

$$\text{Favourable event} = 28 = 26 + 2 \quad \text{Probability} = \frac{7}{13}$$

(d) a face card

$$\text{Favourable event} = 3 \times 4 = 12 \quad \text{Probability} = \frac{12}{52} = \frac{3}{13}$$

(e) a red face card = 6

$$\text{Favourable event} = 6 \quad \text{Probability} = \frac{6}{52} = \frac{3}{26}$$

5. Total number of events = 16

$$\text{Favourable event} = 7 \qquad \text{Probability} = \frac{7}{16}$$

6. Total number of ball = 20

Favourable event for getting white = 5

$$\text{Probability of white} = \frac{5}{20}$$

$$\text{Probability of getting non white} = \frac{20-5}{20} = \frac{15}{20}$$

7. Total number of events = $6 \times 6 = 36$

(a) outcome for odd

Favourable events = (1, 6), (3, 6), (5, 6), (2, 5), (4, 5),
(6, 5), (1, 4), (3, 4), (5, 4), (2, 3), (4, 3), (6, 3), (1, 2),
(3, 2), (5, 2), (2, 1), (4, 1), (6, 1)

$$(b) \frac{18}{36} \text{ or } \frac{1}{2}$$

(c) (2, 6), (3, 5), (4, 4), (5, 3), (6, 2)

(d) Probability of total 8

$$\text{Favourable event} = 5 \qquad \text{Probability} = \frac{5}{36}$$

8. Total number of event = 10

(a) odd number

$$\text{Favourable} = 5 \text{ i.e. } 1, 3, 5, 7, 9 \text{ Probability} = \frac{5}{10} = \frac{1}{2}$$

(b) getting a prime number

$$\text{favourable} = 2, 3, 5, 7, 2 \qquad \text{Probability} = \frac{4}{10} = \frac{2}{5}$$

(c) Events multiple of 2

$$\text{favourable} = 5 \qquad \text{Probability} = \frac{5}{10} = \frac{1}{2}$$

Check Your Mental Math I.Q.

1. Total number of event = 52

(a) a diamond choosen

$$\text{Favourable} = 13 \qquad \text{Probability} = \frac{13}{52} = \frac{1}{4}$$

(b) a king choosen

$$\text{Favourable} = 4 \qquad \text{Probability} = \frac{4}{52} = \frac{1}{13}$$

(c) a black 6 choosen

$$\text{favourable} = 2 \qquad \text{Probability} = \frac{2}{52} = \frac{1}{26}$$

(d) a 8 of heart is choosen

$$\text{Favourable} = 1 \qquad \text{Probability} = \frac{1}{52}$$

2. Total number of event = 6

(a) Prime number

$$\text{Favourable event} = 3, 2, 5 \text{ i.e. } 3 \qquad \text{Probability} = \frac{3}{6} = \frac{1}{2}$$

(b) a number between 3 and 6

$$\text{Varourable} = 4, 5 \text{ i.e. } 2 \qquad \text{Probability} = \frac{2}{6} = \frac{1}{3}$$

(c) odd numbr between 4 and 6

$$\text{Favourable } 5 \text{ i.e. } 1 \qquad \text{Probability} = \frac{1}{6}$$

3. Total number of marbles = $5 + 7 = 12$

(a) a red marbel

$$\text{Favourable} = 5 \qquad \text{Probability} = \frac{5}{12}$$

(b) a blue marble

$$\text{Favourable} = 7 \qquad \text{Probability} = \frac{7}{12}$$

4. Total bulbs = 1200

$$\text{remaining} = 1200 - 24 = 1176$$

$$\text{probability of remaining (good)} = \frac{1176}{1200} = \frac{147}{150}$$

Multiple Choice Questions (M.C.Q.)

1. (a) Total event 6

Favourable = 1

$$\text{Probability} = \frac{1}{6}$$

2. (b) Total events = 12

Favourable = 7

$$\text{Probability} = \frac{7}{12}$$

3. (c) Total event = 52

Favourable = 4

$$\text{Probability} = \frac{4}{52} = \frac{1}{13}$$

4. (d) black ball

Total event = 15

Favourable = 9

$$\text{Probability} = \frac{9}{15} = \frac{3}{5}$$

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Introduction to Graph

Check Your Mental Math I.Q.

- A.** 1. True 2. True 3. True
4. False 5. True
- B.** 1. different 2. second
3. (0, 0) 4. four
5. x-axis

Multiple Choice Question (M.C.Q.)

1. (b) and (c) 2. (b) (4, 0) 3. (a) Origin
4. (a) (0, 3) 5. (a) origin